

ADVANCED PATTERN ANALYSIS

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Introduction.

This text is an advanced one, meant to follow the SAT (Subpattern Analysis Textbook), so the reader is urged to acquire an understanding of the material in the earlier text first. The information in this introduction is little more than a commentary and list of observations, intended to add to and reinforce that earlier text. It is assumed the reader will already have read the earlier text and grasped the essence of it prior to reading this.

The pattern of candidates for a particular digit, 1-9, is derived from a completely annotated sudoku in the following manner:

A separate blank sudoku form, called the pattern form (a copy of which is made available to the reader in the appendix) is used to construct the pattern, and in which:

- 1) For every square of the sudoku in which the solved digit appears, a large X is placed in the center of the corresponding square of the pattern form.
- 2) For every square of the sudoku in which the candidate digit appears, a large version of the digit, of the same size as an established value, is placed in the corresponding square of the pattern form.
- 3) All other squares of the pattern form are left blank.

For a more complete description of the pattern form, as well as the use of it, see the section on pages 16-17 in the SAT.

The sudokus which are solved are always partially solved, the degree to which is shown by the squares containing the givens, the original clues. The average sudoku puzzle generally has a minimum of 27 givens, the least number of which can be as few as 17-18, else not be solvable.

The nomenclature used in this text will be an extension of that defined in the SAT, Chapter 1, Initial Information, pages 1-14.

Every subpattern is a possible completion of the partial pattern of already existing established values. The correct subpattern is the one which solves the particular sudoku puzzle you are working on. The same, already established pattern, might be coupled with a different subpattern in another sudoku puzzle. It is conceivable that zillions of potential sudoku puzzles are solved by every subpattern. This text does not concern itself with finding **the** correct subpattern for a sudoku. It concerns itself with finding **all** the correct subpatterns. Then they may be tested, one by one, until the one that works is found, **but** we cannot count on success unless the one that works is discovered by our analysis. Success relies on **completion**. Pattern analysis has to do with formally identifying and subscripting **all** the members of **every** subpattern of a particular digit pattern.

I have made one small change to that advocated in SAT. Instead of assigning a zero subscript to a pending square, I use a small p. When more than one pending square occurs, the second one gets a q subscript, the next an r, and so forth.

When a preceding subpattern has led to a pending situation, and then come to a conclusion without creating a further pending situation, then a new subpattern must be started in the same square of the starting box, and then proceed, box by box, sharing the

same squares, until the pending box is reached. Then it takes possession of the pending square, after which the fledgling subpattern takes off on its own.

Some comments on the amount of territory being amassed by the developing subpattern – it is impressive how quickly it takes possession of the sudoku. Together with the boxes already under the domination of the established subpattern (the ones with large X's in them), the sudoku eventually becoming blanketed by their control. (See the pictorial displays of subpattern development in chapters 1 and 3.) Every subpattern must behave in this manner, else it fails as a subpattern.

This is what happens at Blind Alleys, which occur when there is no extension of a developing subpattern in the next box, no square which is not already possessed by the subpattern. At such a point, one must backtrack, box by box, upstream, and on arriving at each previous box, have its membership revoked by the removal of the abandoned subpattern number, until the starting box is reached, where the subpattern number is retired from the starting box, and its starting square disallowed as the starting square of any future subpattern. The discontinued subpattern number is now available for use with any remaining unclaimed squares in the starting box.

If you chose a starting box, and then chose any random sequence of boxes, there would be no problem, but if you ran into a pending box, it would be vital for you to remember how you got there, because you will need to follow that same box order for the next subpattern. This is one of the rules of pattern evaluation, in addition to the rule about choosing the starting box and returning to it whenever a subpattern has been completed, in order to begin the next subpattern there as well. You may never, under any circumstance, change the starting box. If you want to try another starting box, you must begin the pattern analysis anew.

If you started at the starting box and didn't decide on the box order in advance, there wouldn't be any problem. You simply need to travel backwards through time to the starting box and specify the arbitrary box order you actually followed. You need to know that box order however, whenever you run into a pending box. Then you must follow the procedure outlined in the paragraph above. Time travel doesn't help when you have a bad memory.

As long as a pending box has not been encountered, you may change the box order for every subpattern, but you must make such a change at the starting box. As soon as a pending situation has occurred, you **must** follow the same order of boxes up to the pending box over and over, until the pending situation no longer exists, with subpattern after subpattern, until no pending squares remain. A pending box will spawn a new pattern for every pending square in the pending box. Normally, there is only one pending square, but multiple pending squares will occur from time to time, and you must be ready for them.

When more than one pending situation occurs, it is vital that you always resolve the highest pending box first. This means that you must slavishly return to the starting box and begin a new subpattern for every pending square in the highest pending box, and keep returning until the pending squares have all given rise to a new subpattern for every

one of them, until a return to the starting box determines that the pending situation in that highest pending box no longer exists, which is signalled by the pending P in the pending box being removed when the last pending square is assigned to a subpattern. Once the highest pending box has been resolved, the next highest pending box becomes the highest pending box. This is always the pending box most immediately upstream.

As soon as the analysis is beyond the highest pending box, the box order is allowed to be changed before the present subpattern is completed, but must be resumed again at the starting box until all pending situations are resolved.. Note that just being beyond the highest pending box does not mean that it is no longer pending. Sister subpatterns must share the same squares with their sisters until they reach the common pending box, and then they are allowed to leave the family breeding bground (the pending box) and set out on their own. Just because one of them has reached the jumping off place does not mean that the next one has yet arrived at that point.

Let us call the subpattern which creates the pending situation the "pender," and the subpattern which follows it the "pendee."

A) If the pending box immediately follows the starting box, then the pendee need not share any further squares with the pender.

B) If there are boxes between the starting box and the pending box, then in all these boxes the pendee must share the same pattern squares with the pender.

C) If the pending square is last, then the pender and pendee share a square in every box except the last. (The last box is the one immediately preceding the starting box.)

Philosophy of Patterns

It is necessary to limit the neighborhood of a square to not include itself.

The subpattern and the neighborhood of the subpattern are developing in tandem. when the subpattern is complete, the neighborhood of the subpattern includes the entire sudoku, except for the members of the subpattern and the members of the established pattern.

Members of a subpattern are not in the neighborhoods of each other, but the neighborhood of the entire subpattern includes every square of the sudoku, except for the squares of the subpattern members and the established pattern members

After testing all the subpatterns, the winning subpattern becomes merged with the established pattern members to create a completed set of pattern members. The combined neighborhood of all the members of the completed set of pattern members includes every square of the sudoku except for the members of the completed set themselves.

The neighborhood of a subpattern, at any stage of its development, is the collection of the members of all the neighborhoods of all of its members.

In the solved sudoku, every square is a member of the neighborhood of the pattern of the unique value of every other square.

In the beginning, the only knowns are the givens. The complete list of the unknowns for each square are the ungivens. They are the candidates. The collection of givens is a complete set of clues as to the identity of every blank square in the sudoku. Even when a particular value does not appear as a given, its exact locations are known in advance, in the form of the solution to the sudoku, and encoded by the identity and location of the givens.

Sudoku puzzles are as difficult or easy as the puzzlemasters choose for them to be. There is a certain art to the creation of sudokus which cannot be fully explained by the puzzlemaster, but there is certainly a great deal of intention which can. We are at the mercy of the puzzlemasters. We do not outwit them. They guide us through the very design of their puzzles. They frequently intend the direction our thoughts must go in order to arrive at a solution. They boast about such matters in language carefully chosen so as to mask their egotism and exalt their creativity, but pride must be there, lurking behind the scenes. It is difficult not to be proud of the difficulties of one's creations, and sudokus are not easy to create, even poor ones. The poverty or richness of a sudoku is the relationship between the givens and the solution, the kind of thinking which is promoted. Ultimately it is the expression of a philosophical attitude towards the solving of sudokus, even as to the proper frame of mind for the puzzler to foster, which are the domain of the puzzlemaster. The "wraparound" nature of sudokus themselves becomes the basis for their solution. But it is important for the solver not to be too preening of his abilities, since it is only because the puzzlemaster has chosen to offer a puzzle capable of being solved by the majority of solvers, or even by a select few. It has always been possible to create close to unsolvable puzzles, if not downright unsolvable ones. But it takes art to make them challenging, while solveable and enjoyable as well.

I call candidates the *ungivens*, because it is so critical that every conceivable value be assigned to them from the very start, if only to avoid that one really fatal mistake of omitting the correct value from a candidate list. If I think I've wrongfully omitted the inclusion of a possible value for a candidate, I add it immediately, even if unnecessarily. With candidates, it is the act of omission, rather than that of commission, which is the fatal error.

What are these strange creatures, the ones we are allowed to delete on the basis of n-wing evidence, or by their being "killer" candidates? In either case, they can only be called "geometric" deletions, provided, of course, that the evidence is accurate. Geometry, interestingly enough, with both n-wings and subpatterns, overrides the excesses of annotation.

Outside of the error of including a digit as a candidate when its established value is already possessed by a square in its neighborhood, there is the lack of knowledge about "non-inclusion," which is responsible for including all the candidates whose "real values" haven't yet been "realized" in their neighborhoods. I wonder how many pattern digits I later deleted shouldn't have been there in the first place. But that can't possibly be responsible for the large numbers of candidates I've been able to erase en masse on occasion with n-wings. I remember how many of these innocents proved to have the characteristics of killer candidates, in their capability, on being hypothetically realized, of destroying parts of the subpattern to the point of rendering it meaningless, while, at other

times, they simply fell to the wayside, others seem to be incredibly un-sudoku-social. Perhaps it's the method of finding them. Perhaps it's finding the right subpattern. If it's really the right one, it'll cut to the quick.

The most solid characteristic of a winning subpattern is that it arises from the dregs of a successful n-wing deletion. I have found no comparable wisdom, no clue with such a winning record.

My personal passport to solving sudokus was using a "blank" sudoku form for testing for n-wings and subpatterns. Had I not, I would've continued "drawing a blank." I originally started copying newspaper sudokus onto blank forms on normal 8 ½ by 11 sheets with room for two on each side, and then the left-side copy started getting used to test hypotheses, and I never went back to saving paper, except when it was one of those puzzles that solves itself while you sit back and watch while you rapidly scribble out the answer, realizing disappointedly that there wasn't going to be an endgame after all that work. Just another fill-in puzzle.

Killer Candidates

Let us suppose you had just completed the analysis of a pattern, and one of the squares didn't get included in a subpattern. You know that such a square is supposed to be a killer, but maybe you made a mistake. How can you verify that a square harbors a killer? Simple. Just write out the pattern on a blank sudoku form and promote that candidate to an established value. Remember that an established value cancels all the candidates in its neighborhood. If the candidate is valid, all the pattern boxes will end up having at least one candidate at the end.

If one or more of the pattern boxes ends up with no candidates, or if two boxes have a single candidate each, and those two boxes end up in a standoff (i.e. one candidate in each box with the two candidates opposing one another in the same row or column, so if one of them is eliminated, its box is then devoid of candidates), then you know that the candidate which was promoted is the culprit. An easy test you can always count on. It is also the reason I chose for calling it a killer, as it always kills all the candidates in at least one of the pattern boxes.

Killers were never known as such until pattern analysis came on the scene. They seem to be similar to the pattern squares eliminated by n-wings. When you encounter one, it is important to keep it in the pattern, but given the subscript K, for "killer." The reason for keeping in in the pattern, even though it isn't a valid candidate, it is important when you go to test the pattern to know that the candidate in the sudoku corresponding to the killer position should not be a member of the pattern and must be removed. In this case, the K stands for "kaput," so it is a reminder to get rid of that candidate before proceeding further with the solving process, but don't get rid of it until the pattern is put into use.

Let's promote the killer 2 in square (48) of the example below, the underlined 2-candidate. It eliminates all the candidates in its row, column, and box, leaving box C without a candidate, and resulting in a standoff between the 2's in column 5.

	1	2	3	4	5	6	7	8	9
1					2			2	
2									
3				2				2	
4				2	2		2	<u>2</u>	
5									
6					2		2		
7									
8									
9									

	1	2	3	4	5	6	7	8	9
1					2				
2									
3				2					
4								<u>2</u>	
5									
6					2				
7									
8									
9									

A Simple Subpattern Analysis

An interesting analysis can be made using the same method as above, but for a different purpose. Let's look again at the same subpattern:

	1	2	3	4	5	6	7	8	9
1					2			2	
2									
3				2				2	
4				2	2		2	2	
5									
6					2		2		
7									
8									
9									

Instead of using this diagram for proving that the 2 in (48) is a killer, let's use that same diagram to analyze the subpatterns.

Promote the 2 in square (18), and see what happens to the sudoku pattern. We first eliminate all the 2's in its row, column, and box:

	1	2	3	4	5	6	7	8	9
1	2							2	
2									
3				2				2	
4				2	2		2	2	
5									
6					2		2		
7									
8									
9									

	1	2	3	4	5	6	7	8	9
1								2	
2									
3				2					
4				2	2		2		
5									
6					2		2		
7									
8									
9									

We have already isolated two of the 2's. Next, we'll eliminate all the 2's in the vicinity of the second isolated 2, the one in (34).

	1	2	3	4	5	6	7	8	9
1								2	
2									
3				2					
4				2	2		2		
5									
6					2		2		
7									
8									
9									

	1	2	3	4	5	6	7	8	9
1								2	
2									
3				2					
4					2		2		
5									
6					2		2		
7									
8									
9									

We have now run into the equivalent of a pending situation in boxes E and F, so we'll choose square (45) as the next 2 to isolate, by eliminating all the squares in its neighborhood.

	1	2	3	4	5	6	7	8	9
1								2	
2									
3				2					
4					2		2		
5									
6					2		2		
7									
8									
9									

	1	2	3	4	5	6	7	8	9
1								2	
2									
3				2					
4					2				
5									
6							2		
7									
8									
9									

This action isolates the fourth member. We have now isolated our first subpattern, the 2's in the diagram on the upper right, in squares **(18), (34), (45), and (67)**.

On the next page, we'll do the same for the candidate in square (38), the remaining square of our starting box C.

This action isolates the two in square (15), the first member of subpattern-2, which isolates the second member of subpattern-2, square (15).

	1	2	3	4	5	6	7	8	9
1					2			2	
2									
3				2				2	
4				2	2		2	2	
5									
6					2		2		
7									
8									
9									

	1	2	3	4	5	6	7	8	9
1					2			2	
2									
3				2				2	
4				2	2		2	2	
5									
6					2		2		
7									
8									
9									

Next, we eliminate all the 2's in the neighborhood of square (15), which isolates the third member of subpattern-2, namely (44):

	1	2	3	4	5	6	7	8	9
1					2			2	
2									
3				2				2	
4				2	2		2	2	
5									
6					2		2		
7									
8									
9									

	1	2	3	4	5	6	7	8	9
1					2				
2									
3								2	
4				2			2	2	
5									
6							2		
7									
8									
9									

The last action for this second subpattern is to eliminate all the 2's in the neighborhood of square (44).

Eliminating the 2's in the neighborhood of this third square, (67), isolates the fourth and final member of subpattern-2, which consists of the set of squares (38), (15), (44) and (67).

	1	2	3	4	5	6	7	8	9
1					2				
2									
3								2	
4				2			2	2	
5									
6							2		
7									
8									
9									

	1	2	3	4	5	6	7	8	9
1					2				
2									
3								2	
4				2					
5									
6							2		
7									
8									
9									

To isolate the last subpattern, we return to the "pending" situation two pages back, and this time we isolate the square (65), below, revealing the third subpattern below:

	1	2	3	4	5	6	7	8	9
1								2	
2									
3				2					
4					2		2		
5									
6					2		2		
7									
8									
9									

	1	2	3	4	5	6	7	8	9
1								2	
2									
3				2					
4							2		
5									
6					2				
7									
8									
9									

Subpattern-3 = (18), (34), (47), and (65). We can encapsulate these subpatterns by giving their squares the subscripts 1, 2, and 3. See the next page.

The three subpatterns are:

Subpattern-1: (18), (34), (45), and (67)

Subpattern-2: (38), (15), (44), and (67).

Subpattern-3: (18), (34), (47), and (65)

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					2_2			2_{13}	
row2									
row3				2_{13}				2_2	
row4				2_2	2_1		2_3	2_K	
row5									
row6					2_3		2_{12}		
row7									
row8									
row9									

The Pattern Project

I began collecting successful subpatterns five or six years ago, with the vague notion of doing a study on them. It was clear that every pattern had a high probability of occurring in another sudoku, but unlikely that the same subpattern would be successful in solving it, but a pattern study reserved to be done, and on what better group?

An attempt has been made to preserve the large X's in the patterns even though they play no role in the study or use of them. It does seem likely that if two sudokus were identical except for the positions of the established values, a successful subpattern in one would be successful in the other. But the X's remind the reader that the situation arose in the context of a real problem involving a real sudoku, so I have kept them.

The only records I had saved for this study were the successful subpatterns and the patterns which had spawned them, the original sudokus lost under the graphiti of scribbles and erasures.

Because I had accumulated such a treasure trove, I was then faced with the daunting project of solving all of them. After all, I had intended this to be a complete pattern analysis. This focussed my attention on the raw data, the hope being to find a meaningful grouping,

Before I even considered abstract reasons for groupings, I had early on realized the futility of breaking up sudokus into sizeable hunks and then just doing a survey on hunks. Sudokus are too wraparound, too holographic. The relationship itself had to be relational, and the relationship had to be the addition of something new. Once it was incorporated, it was part of the new whole, the new new, and this growing monster had a passion for all, until all became one, when every square in the part that didn't have members to represent it was gone. Then all the subpatterns were complete, which really means recognized, and there were nine of them; one member in every box, one box for every member, which was what the puzzlemaker, in all his sudoku-wisdom, had intended.

The strange kind of ***relational*** that this idea of a subpattern of equals depends upon is the relationship of non-membership. The new cannot become a member of the old unless it is not one of them. The pattern square which survives is the next king of the hill, where hill means box, and it cannot even share a square in its own neighborhood with its neighboring reigning candidate. The set of squares of the subpattern is a set of sociopaths, each with its separate domain, one for each of the nine boxes, one of the up-to-nine unclaimed, that is.

With this idea in mind, I set out to divvy up what I had into six groups, one for each digit, which referred to subscripts rather than candidate digits. This lent some orderliness to the groups, that order generally implying simplicity. It also arranged the orderliness to the comparisons of sudokus of the same size, size referring to the largeness of squares due to so many candidates at their tops, as well as being of sufficient size to clearly display the subscripts of their candidates.

All in all, it proved to be a wise choice. The number of subscripts roughly related to the number of candidates, as well as to the complexity of patterns. So there are six groups of

patterns, separated by the maximum number of subscripts. A little cheating goes on at the borders of these groups, where only one candidate has three subscript, and all the rest have one or two, and they are together as a 2-group.

It didn't take long to discover the uncomfortable truth that the box code wasn't going to cut it. As long as the number of subscripts was three or less, all almost went well. With just nine squares in a box, there aren't many arrangements of three, especially when two arrangements are the same when a nine-perfect transformation turns one into the other. With three, for example, there are only three arrangements of three squares within a box: three in a row, two in a row with the third sharing a column with one of the other two, and two in a row with the third not sharing a column with either of the other two.

So up to three candidates in a box could be catalogued. I called them horizontal (including vertical and diagonal), small ells, and large ells. The three subgroups couldn't be transformed into one another 9-perfectly, but there were exactly three kinds of candidate arrangement, and two kinds of relationships between two boxes, so there were equivalence classes, which is what I wanted.

But it all fell apart with four squares in a box, because the number of interactions was so great that analysis was unhelpful. But the picture codes at least afforded a means of doing it. At least it was that. Do-able. So I stuck with the box codes and lumped patterns together according to the box codes. In most cases I am willing to argue that the situations in the analysis are analogous, like alleles in organic chemistry.

This is the irrational rationale to my selection of patterns to solve.

We'll proceed on to a short discussion of 9-perfect transformations of patterns, followed by a brief foray into the files of the Pattern System, their contents and interconnections

Pattern Codes

Permutations of rows, columns, bands and stacks:

Any permutation of the 3 rows of a band results in a sudoku. The proof is intuitively clear, since the rows maintain their integrity as rows, the columns undergo only a reordering of the values within them, and the boxes undergo only a shuffling of the rows within them. Hence every row, column, and box which is affected by the permutation does not have its elements altered, only rearranged, so that 9-perfection is maintained.

Any permutation of the 3 columns of a stack results in a sudoku. The proof is similar to that above.

Any permutation of the bands of a sudoku results in a sudoku. The proof is obvious, since the integrity of rows is unaffected, the boxes are not altered, and the columns suffer no more than an alteration in the sequence of their values.

Any permutation of the stacks of a sudoku results in a sudoku. The proof is similar to the argument above.

Any combination of the above permutations results in a sudoku. The proof is an iteration of what has already been said.

Rotations and reflections:

Any rotation of a sudoku by an angle which is any multiple of ninety degrees results in a sudoku. The proof is visually clear. The digits will still be recognizable, and their relationships are not changed.

Any reflection of a sudoku about a vertical, horizontal, or diagonal axis results in a sudoku. Again, the proof is visually clear.

What is the point of all these transformations? That any pattern of boxes within a sudoku is essentially unaltered by them. Rows and columns retain their status, or are converted into columns and rows. Squares in the same row either end up in a different row together, or the row they are in is converted into a column in which those boxes end up being together. Rows maintain their integrity, as do columns. Even the intersections of rows and columns are still the intersections of the rows and columns or columns and rows into which they have been converted. Boxes sharing rows remain boxes sharing rows, or are converted into boxes sharing columns. Relationships between specific squares are transformed into similar relationships between the transformations of those squares.

The important conclusion is that patterns of boxes, including the patterns of candidates within them, are not altered by such transformations. Moreover, except for orientation, they remain the same patterns. Upside down or backwards, the relationships of boxes and their candidates remain unaltered.

This was my reason for choosing patterns of boxes as a code for classifying sudoku patterns. These codes, since they don't take into consideration the orientation of the squares within the boxes, are not precise. It was one of my initial intentions to make it precise, but but I discovered that to take classification to the level of exactness required too much claim on my time.

I needed a way, however, of reducing the sheer number of sudoku candidate patterns I had collected, because to present solutions of all of them would be sheer insanity. I was hoping that if I could make the pattern codes precise, then I could group the codes by the pattern code, in which case the solution to one would be the solution to a whole bunch of them. That would cut down on the job I had undertaken, to write a text on sudoku pattern analysis. I needed a classification system, and it had to be abstract rather than visual, and it had to do with candidates. The squares they were in and their own individual digits

The elements of these **box codes** are the boxes in which the pattern exist, and the identification of those boxes by the number of pattern squares inside them. The digit "3" represents a box with 3 candidate squares. 3-4-2 represents three boxes in the same row or column with a 3-pattern-square box followed by a 4-pattern-square box, followed by a 2-pattern-square box. Two boxes are related if they possess pattern squares in their shared rows or columns. The fact of that relationship is shown by a short vertical or horizontal line segment connecting the two. They resemble a flow chart, except that there is no flow, and therefore no arrows, the line segments joining them showing

organizational relationship rather than causal. The order of boxes (the box order used in analysing subpatterns) is closely related to the box code, except that the order of boxes is allowed to connect two boxes not physically adjacent. The box code reminds me a little of organic chemistry, in its architectural look.

The major distinction between the box code I employ and a simple diagram of the boxes is that unrelated boxes in the box codes are never placed in the same row or column, even when there is no line segment joining them, just to avoid seeing relationships when they are not there.

I did discover a way to compare patterns on the level of squares within boxes, by means of what I call a **picture pattern** derived from the sudoku pattern. All that needs to be done is to remove all the blank rows and columns from the pattern, which is easy to do on a computer. The size of these picture patterns depends on the extensiveness of the sudokus from which they are derived. They are most useful when they are small, and one must still perform all the mental gymnastic associated with rotations and reflections. The major problem is that the identity of boxes is destroyed, which is partly alleviated by my practice of shading alternate boxes, but that too is not entirely helpful when boxes of the same shade are merged due to the blank rows or columns between them having been deleted. When boxes so merge, I slightly alter their shades in the picture pattern in order to preserve distinction.

When two patterns have precisely the same picture pattern, there can be no doubt that they are identical. It takes time to make these comparisons, so I have only used them so far in conjunction with sudoku patterns with two subscripts, which I have spent the most time analyzing. Patterns with a limit of two subscripts are easier to compare, and they fall into groups more readily than patterns with a larger number of subscripts, where pattern variation is much more widespread.

A page from the Pattern File follows, showing the **picture pattern** beneath the pattern.

2 051 A4
L

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	1 ₃			1 ₁	1 ₂				
row2	1 ₁₂					1 ₃			
row3									X
row4							X		
row5		X							
row6				1 ₂₃	1 ₁				
row7			X						
row8								X	
row9					1 ₃	1 ₁₂			

2 051 A4
L

	col 1	col 4	col 5	col 6
row1	1 ₃	1 ₁	1 ₂	
row2	1 ₁₂			1 ₃
row6		1 ₂₃	1 ₁	
row9			1 ₃	1 ₁₂

(For more examples, go to the Pattern File.)

The solved problems in the two-subscript category have specified for each the transformations necessary to orient the pattern in the sudoku to the pattern of its box code. I had to perform these transformations for all of the patterns in order to arrive at the box codes, but it was mainly done in my head, and, except for more complicated ones, seldom written down, except in the case of the two-subscript group (of which I made a special study).

I divided the patterns up into six groups, according to the number of subscripts, on the basis that larger sudoku patterns tend to be more difficult, and more digits generally mean more complexity, and I wanted to present the sudoku patterns by difficulty of solution. Still, I didn't know quite how to go about it. I had been collecting these patterns for several years with the intent to use them for a study of patterns, but the occasion never seemed to arrive.

Conceivably, almost every subpattern might be used to solve a particular sudoku, or even a large number of sudokus, but I seldom tried to use the subpattern method until all other methods had failed, so it was always my ace in the hole, and I gained little expertise on how one might use them as the principal solving technique.

Still, the fact that they had always worked in clutch situations might have tipped me off as to their general solving efficacy. For the last year and a half I have tried them on almost every difficult puzzle, and have discovered in many instances that not just one subpattern, but often three or four, can be used to solve a particular sudoku. The one measure I follow faithfully, however, is to check first for what I call *n-wings* (my terminology for *xwings*). I have come to believe that the best pattern for subpattern solving is the remains of one which has been pared down by n-wing operations. Even when they don't lead to candidate reduction, patterns are the first thing I look at after the normal reduction which follows annotation.

The 5-subscript patterns & 6-subscript patterns have not yet been included in this study. They are, unsurprisingly, fewer in number, since rational sudoku solvers, as I like to think of myself, do not willingly make use of overlarge patterns, not primarily because they take time to analyze, which is certainly true, but because they have too many subpatterns, and each one must be laboriously tested with yet another temporary update. The only instance in which I settle for a large pattern is that rare one where the smaller ones don't free up enough digits to work

Since I had such a massive project on my hands, I started out by dividing the patterns into the six groups I have described, and I decided to deal with each one in its own section of the text. I did this partly because the box codes varied quite a bit from one group to the next. As a result, I dealt independently with each of the groups, creating them one at a time, even setting up a different set of alpha codes for each. The **alpha code** is a two-character alphanumeric code which relates the **box code** to the **pattern number** via the **Pattern Description File**, which, besides the alpha code, by which it is organized, contains the box code and the list of the pattern numbers which possess that same box code.

Two types of files follow this text:

1) The **Pattern File**, organized by **pattern number**, in which each pattern is shown on a sudoku form bearing the **pattern number** and **alpha code**. It is also accompanied by its **picture code**, which, for the smaller patterns, is a useful way to determine the precise structure, down to the squares within the boxes. An example of one of its entries has already been shown two pages back.

2) the **Pattern Description File**, organized by **alpha code**, showing the **alpha code**, the **box code** and all the **equivalent pattern numbers**, which relates it to the Pattern File. An example of the first few entries in it are:

Pattern Description Codes 2:

A1	3 - 2 2	S 023, 038, 047, 048, 056, 066, 068, 091, 092, 093, 094, 096, 105, 145.
A3	3 - 2 - 2	030, 102. (Straight three)
A4	3 - 2 - 2 2	S 110, 114. L 039, 051, 070, 072, 079, 095, 107, 110, 120, 123.
A6	3 - 2 - 2 2	X 104
A5	3 - 2 - 2 2 - 2	L 097
D	2 3 - 2 2	S 002, 003, 006, 010, 011, 020, 050, 078, 080, 089, 098, 099, 103, 106, 113, 115, 118, 122, 124, 127, 152, 154
		* * *

In the main text, every solved pattern is preceded by a header giving the following information:

Pattern 2.023 L	Box Orientation	Patterns with the same box code:
3 – 2	E – D	023, 038, 047, 048, 056, 066, 068, 091,
		092, 093, 094, 096, 103, 105, 126, 145.
2	H	
(box orientation for 023 – interchange stacks 1 & 2)		

The diagram on the extreme left is the box code, indicating, in this instance, which boxes have three pattern squares and which have two, and how they're arranged. If you compare it with the box orientation immediately to its right, you can see by the comparison how many pattern squares are in each of the pattern boxes E, D, and H.

There are six sets of files, one for each subscript range, from 1 to 6. Each set consists of a Pattern File and a Pattern Description File. It will be a future project to merge the six Pattern Description Files together, as well as to amalgamate the alpha codes for all of them into a single grand scheme. The alpha codes themselves need to be completely revamped for this scheme, in order to connote the level of the patterns, from simple to complex. The present alpha codes were adopted in a hurry, in order to get this project off the ground, and lack entirely in esthetics. The six Pattern Files will remain the same, however, as well as the six sections of this text, arranged, obviously, in order of the number of subscripts in the patterns themselves.

The initial study included an in-depth analysis of the 2-subscript patterns, which are the most extensive of the six sections. It surprised me considerably, when I analyzed the results, just how many of these patterns had nearly identical box codes, especially among the 2-subscript patterns (the largest category). Here is the summary:

1-subscript patterns	3-subscript patterns
9 box codes with one example each	24 box codes with one example each
3 box code with 2 examples each	9 box codes with 2 examples each
1 box code with 3 examples	2 box codes with 3 examples each
1 box code with 8 examples	2 box codes with 4 examples each
1 box code with 13 examples	1 box code with 6 examples
2-subscript patterns	1 box code with 11 examples
20 box codes with 1 example each	4-subscript patterns
9 box codes with 2 examples each	17 box codes with 1 example each
2 box codes with 3 examples each	5 box codes with 2 examples each
1 box code with 5 examples	3 box codes with 3 examples each
1 box code with 6 examples	
1 box code with 7 examples	
1 box code with 8 examples	
1 box code with 14 examples	
1 box code with 16 examples	
1 box code with 19 examples	
1 box code with 20 examples	
1 box code with 22 examples	

The in-depth study included comparison of the members of the first and third codes in the Pattern Description Codes, A1 and A2. This comparison was necessary to shed light on the degree to which box codes reflect the intricacy of the patterns.

The page below is a comparison of the picture codes for the A1 alpha code group. No effort was made to convert them into identity comparisons, via 9-perfect transformations, as the equalities between the picture codes are fairly evident.

If *all* the box codes reflected this kind of one-to-one comparison with the picture codes, my original dream would have been realized, because the box codes groups would be ones of equality, rather than groups of closely related patterns.

The following is a summary of the picture codes for the first alpha code, A1, for which all the members have exactly the same pattern, which simple rotations, axial reflections, and subscript rearrangements would suffice to show.

023	A1	col 3	col 4	col 5
row4		3 ₃	3 ₁	3 ₂
row5		3 ₁₂	3 ₃	
row9			3 ₂	3 ₁₃

038	A1	col 5	col 6	col 7
row3		8 ₁₃	8 ₂	
row5			8 ₁	8 ₂₃
row6		8 ₂	8 ₃	8 ₁

047	A1	col 5	col 6	col 9
row1		1 ₁	1 ₂	1 ₃
row3		1 ₃		1 ₁₂
row5		1 ₂	1 ₁₃	

048	A1	col 4	col 5	col 7
row1		2₁	2₂	2₃
row2			2₃	2₁₂
row7		2₂₃	2₁	

056	A1	col 1	col 2	col 5
row1		3 ₁	3 ₂	3 ₃
row2			3 ₃	3 ₁₂
row4		3 ₂₃	3 ₁	

066	A1	col 1	col 5	col 6
row1		4 ₂₃	4 ₁	
row2		4 ₁	4 ₂	4 ₃
row7			4 ₃	4 ₁₂

068	A1	col 1	col 3	col 5
row2		4₁	4₂	4₃
row3			4₃	4₁₂
row5		4₂₃	4₁	

091	A1	col 6	col 7	col 9
row2		2 ₁	2 ₂	2 ₃
row3		2 ₂₃		2 ₁
row4			2 ₁₃	2 ₂

092	A1	col 4	col 6	col 9
row5		6 ₂	6 ₁₃	
row7		6 ₁	6 ₂	6 ₃
row9		6 ₃		6 ₁₂

093	A1	col 1	col 5	col 6
row4			8₁	8₂₃
row8		8₃	8₂	8₁
row9		8₁₂	8₃	

094	A1	col 2	col 4	col 6
row5		5 ₁	5 ₂	5 ₃
row6		5 ₂₃	5 ₁	
row9			5 ₃	5 ₁₂

096	A1	col 5	col 8	col 9
row1		2 ₂₃		2 ₁
row2		2 ₁	2 ₂	2 ₃
row8			2 ₁₃	2 ₂

105	A1	col 5	col 8	col 9
row2		2₃	2₁	2₂
row3		2₁₂	2₃	
row8			2₂	2₁₃

145	A1	col 3	col 7	col 9
row1		1 ₂₃	1 ₁	
row3		1 ₁	1 ₂	1 ₃
row7			1 ₃	1 ₁₂

The second large box code group, for code A2, is first calculated for pattern 051, and is shown in its entirety:

This is the pattern snapshot:

A4					
051	L	col 1	col 4	col 5	col 6
row1		1 ₃	1 ₁	1 ₂	
row2		1 ₁₂			1 ₃
row6			1 ₂₃	1 ₁	
row9				1 ₃	1 ₁₂

Step 1: put cols in order 4651:

		A4			
051	L	col 4	col 6	col 5	col 1
	row1	1 ₁		1 ₂	1 ₃
	row2		1 ₃		1 ₁₂
	row6	1 ₂₃		1 ₁	
	row9		1 ₁₂	1 ₃	

Step 2. Interchange rows 6 & 9:

A4					
051	L	col 4	col 6	col 5	col 1
row1		1 ₁		1 ₂	1 ₃
row2			1 ₃		1 ₁₂
row9			1 ₁₂	1 ₃	
row6		1 ₂₃		1 ₁	

Comparison with pattern 039:

A4					
039	L	col 1	col 2	col 3	col 9
row1		7 ₁		7 ₂	7 ₃
row3			7 ₃		7 ₁₂
row5			7 ₁₂	7 ₃	
row9		7 ₂₃		7 ₁	

All of the subscripts exactly agree.

It must be pointed out that the operations leading to the comparison above are 9-imperfect. They cross stack and band boundaries, destroying the integrity of the boxes.. But, and this is the critical "but" – All of the rows and columns have been preserved, even though the boxes haven't. The sums expressed by the rows and columns are exactly the same on both sides, as well as the complete match on subscripts. The Law of Total Subscripts is upheld on every row and column. Therefore the solutions must be identical.

The remainder of the group 2 members run into no snags. The methods of conversion are provided, and they are all 9-perfect.

Group 1:

2 070 A4 L

	col 3	col 4	col 5	col 9
row4		4 ₂	4 ₁₃	
row7		4 ₁		4 ₂₃
row8	4 ₃		4 ₂	4 ₁
row9	4 ₁₂	4 ₃		

2 072 A4 L

	row7	row4	row6	row2
col 5		3 ₂	3 ₁₃	
col 4		3 ₁		3 ₂₃
col 6	3 ₃		3 ₂	3 ₁
col 2	3 ₁₂	3 ₃		

072: change col order from 2456 into 2645, swap rows 4&6, rotate 90 degrees clockwise, then change digits from 123 into 312.

Group 2:

051: interchange digits 1 & 2, put cols in order 4561, and swap rows 6 & 9.

095: no changes.

107: rotate 90 deg counterclockwise, change digits 123 into 231.

2 039 A4 L

	col 1	col 2	col 3	col 9
row1	7 ₁		7 ₂	7 ₃
row3		7 ₃		7 ₁₂
row5		7 ₁₂	7 ₃	
row9	7 ₂₃		7 ₁	

2 051 A4 L

	col 4	col 6	col 5	col 1
row1	1 ₁		1 ₂	1 ₃
row2		1 ₃		1 ₁₂
row9		1 ₁₂	1 ₃	
row6	1 ₂₃		1 ₁	

2 095 A4 L

	col 4	col 5	col 6	col 7
row2	7 ₁		7 ₂	7 ₃
row3		7 ₃		7 ₁₂
row6		7 ₁₂	7 ₃	
row9	7 ₂₃		7 ₁	

2 107 A4 L

	row4	row5	row6	row7
col 8	9 ₁		9 ₂	9 ₃
col 7		9 ₃		9 ₁₂
col 5		9 ₁₂	9 ₃	
col 2	9 ₂₃		9 ₁	

All subsequent conversions are 9-perfect, patter 095 agreeing, by accident, on pattern digit as well.

D1 3 – 3 006, 019, 021, 023, 028, 036
 | |
 3 – 2

subgroup 1 (24 possibilities): 006, 021, 023, 028 generated from model A (below)

abcd = 2134 for 006

3	006	col 4	col 6	col 7	col 8	3
row5		1 ₁₂	1 ₃	1 ₄		
row6		1 ₄		1 ₁₃	1 ₂	
row8		1 ₃	1 ₁₄	1 ₂		
row9			1 ₂		1 ₁₃₄	

abcd = 2314 for 021

021	col 1	col 3	col 7	col 8
row4	1 ₂	1 ₃₄	1 ₁	
row5		1 ₁	1 ₂₃	1 ₄
row7	1 ₁₃₄			1 ₂
row9		1 ₂	1 ₄	1 ₁₃

abcd = 4213 for 023

3	023	col 2	col 3	col 5	col 6	3
row1		4 ₁		4 ₂₄	4 ₃	
row3		4 ₂₃	4 ₄	4 ₁		
row7		4 ₄		4 ₃	4 ₁₂	
row8			4 ₁₂₃		4 ₄	

abcd = 2314 for 028

028	col 1	col 3	col 7	col 8
row4	1 ₂	1 ₃₄	1 ₁	
row5		1 ₁	1 ₂₃	1 ₄
row7	1 ₁₃₄			1 ₂
row9		1 ₂	1 ₄	1 ₁₃

MODEL A (abcd = perm(1234))

3	xxx	col ?	col ?	col ?	col ?
row?		9 _{ab}	9 _c	9 _d	
row?		9 _d		9 _{ac}	9 _b
row?		9 _c	9 _{ad}	9 _b	
row?			9 _b		9 _{acd}

subgroup 2 (24 possibilities): 019, 036. generated from model B (below)

abcd = 1234 for 019

3	019	col 5	col 6	col 7	col 9	3
row5			3 ₁₂		3 ₃₄	
row6		3 ₃	3 ₄	3 ₁	3 ₂	
row8		3 ₁		3 ₂₃₄		
row9		3 ₂₄	3 ₃		3 ₁	

abcd = 4213 for 036

036	col 4	col 6	col 8	col 9
row5	2 ₁₂	2 ₃	2 ₄	
row6	2 ₄			2 ₁₂₃
row7		2 ₂₄	2 ₁₃	
row9	2 ₃	2 ₁	2 ₂	2 ₄

MODEL B (abcd = perm(1234))

3	xxx	col ?	col ?	col ?	col ?
row?			9 _{ab}		9 _{cd}
row?		9 _c	9 _d	9 _b	9 _a
row?		9 _b		9 _{acd}	
row?		9 _{ad}	9 _c		9 _b

Note: to see agreement between picture code derived from a particular pattern and that generated by the model, some permutation of rows and columns will be necessary. It is standard practice to allow 9's to be used in the abstract to represent all possible digits.

The powers of Zap:

Zap is a power possessed by the squares of a sudoku in the process of being solved. It is used to create subpatterns, and its power is only available to certain squares called **zap squares**, which are under your command and guidance, in your role as **Zapmaster**. Subpatterns are collections of zap squares, and may only be created one at a time. Until a subpattern is complete, it exercises, through its members, the power of Zap. Once a subpattern has been completed, it becomes inactive, as far as the solver is concerned, and zap power is passed on to the next subpattern to be developed.

Zap squares are antisocial entities which cannot abide the presence of other members of the same subpattern. For a particular pattern digit, there must be exactly one member, one zap square in each box, and each zap square must be labeled with a subscript identifying it as a member of the particular subpattern which is under process of completion. When a subpattern has been completed, it ceases its aggression, at which time the power of zap is conferred upon the members of the next subpattern to be developed.

At the beginning of sudoku time, there exist already, for each subpattern, a number of already solved squares, which could be called **established zap freelancers**, which, while a subpattern is under development, exercise that same power of zap, but do not belong to that subpattern. They are the squares with single digits at their centers. Some of these freelancers were specified as **givens**, clues to the solution of the sudoku. Others were discovered by you, during the initial stages of solution prior to the process of annotation, and sometimes even a few during annotation. Each freelancer exercises zap power for one particular pattern digit, and it exercises that power over its entire domain, which is the neighborhood of the freelancer. (The neighborhood of any square is the collection of all other squares which are in the row, column, and box of that square.)

On the other hand, there are the blank squares with lists of candidates at their tops. We could call them **non-freelancers**, because, due to the candidates at their tops, they are associated with a number of **different** subpatterns, which are like different clubs to which they may belong. There are exactly nine of these clubs, one for each of the nine digits. Subpatterns are created from these non-freelancers, and subpatterns are oblivious to one another. They coexist, just as human organizations coexist, in that an individual square may belong to a number of them, independently.

Just after the beginning of sudoku time, the established zap freelancers exercised their zap power to confer upon all non-freelancers membership in these nine clubs. This initial period is called the **process of annotation**. It is the intention of all non-freelancers to gradually divest themselves of membership in all but one of these clubs, and, under the guidance of you, the Zapmaster, their multiple memberships are eventually whittled down to exactly one specific club each, at which point they themselves become established freelancers. At the end of sudoku time, when the sudoku has become completely solved, every one of the 81 squares has become an **established zap freelancer**, which is just another way of saying **solved square**.

The exercise of zap power is called ***zapping***. Zapping is always directed at the members of a particular box until a single unzapped square remains (called a ***zap square*** or ***zapper***), which becomes the next member of the growing subpattern. Zappers can only zap squares which are in the same row or column of the box whose squares are being zapped, the zap power passing invisibly through any squares in the way until that particular box is reached, at which point all squares of that box which are in the same row or column as the zapper become zapped, which renders them ineligible for membership in the subpattern being developed.

The most important powers that you, as Zapmaster, have, in the development of a subpattern, are threefold: the ***choice of the starting box*** of that subpattern, the ***choice of the starting square*** for that subpattern, and in the ***choice of the order of boxes*** which is to be followed during that development. Any choices you make for these three items will succeed, but some choices would result in much more labor for you than others, in your job as Zapmaster, directing the development of that subpattern.

The purpose of this Zap language is the facilitation of the process of subpattern evaluation by you. Without this language, the description of that process is laborious, lengthy and overwordy. The sheer number of words involved can become cumbersome. Lengthy description requires more concentration, as the salient points often become buried in the process of explanation, and the eye, as well as the mind, becomes easily fatigued by the discipline necessary.

The downside to this approach is the necessity of understanding the ***Zap*** language to the point of being able to think in terms of it. But once the language has been mastered, the understanding of the process becomes greatly simplified. If you have an aversion to abstraction, you are in trouble. If you prefer a volume of words to the simple terms of zapping, this is not a method you will easily embrace, but if you are willing to submit to the process of understanding it, you will find yourself carried along by it, and you will be able to calculate sudoku patterns with ease..

Once that understanding has been achieved, there is little more to learn about the calculation of subpatterns. Using zap language, the amount of description is greatly simplified, and you, as sudoku solver, will find that it focuses your solving on the specific information to be calculated – the determination of the squares of the set of subpatterns you have chosen to use in solving the sudoku. The payoff is the ease with which you will be able to solve some of the most difficult sudoku problems, in some instances, cutting two hours down to a half hour, and in most instances, being able to solve some of the most difficult problems without having to learn anything more in the way of technique.

The areas which will not be simplified are the initial ones of trapping, annotation and group separation.. The actual solving is where the power of Zap manifests itself, by making possible the determination of subpatterns, and it is the use of subpatterns which speeds up and simplifies that solving. This volume does not show you how to use subpatterns to solve sudokus; it merely shows you how to calculate those subpatterns in the first place. There are other texts on this website which thoroughly go into the use of subpatterns for solving.

There is one last point that should be made. The Zap language is meant only to assist you in learning how to solve patterns. It is not a language you will use personally (except in your mind while you are calculating a subpattern). You will never write down an instruction or action in it. The only items you will be using a pencil for are filling out the blank sudoku form with the digit pattern to be analyzed, the subpattern subscripts as you deduce them, the pending P's in the pending boxes, along with the p subscripts you append to the pending squares, and perhaps also the order of boxes, so you won't forget it, and, finally, the list of subpattern members that you calculate for each subpattern

* * *

In the calculation of a subpattern, one needs to prime the pump by choosing the starting box and the starting square of that subpattern. These are the choices that you, as Zapmaster, must make. There are other choices down the line, once you have begun the process of determining the squares of a subpattern. One of them is how to handle the situations in which several squares in a particular box are made available by the zapping process. We'll deal with these details in the comments which follow.

A subpattern is begun by choosing the starting box and the starting square within that box. The boxes of a pattern are all those in which the pattern digit appears as a candidate in two or more squares. (If the pattern digit is a candidate in only one square of a box, it must be promoted to the established value for that box.) Once a starting box is chosen for analyzing the subpatterns of a sudoku, it may never be changed. But it ceases to be important, or even meaningful, once the subpatterns have been calculated, since any box could have been chosen as the starting box. The same is true of the order of boxes. When you go to use the subpatterns to solve a sudoku, the subpattern members do not have to be looked at in any order, because they are equal in importance.

For the discussion which follows, we'll assume a situation in which you are determining the subpatterns for a particular digit, and in which you have chosen the pattern to analyze, and have arbitrarily chosen the starting box and the initial square within it to begin the first subpattern, which will be called ***subpattern-1***.

The initial square is able to ***zap*** all the squares in the sudoku which are in the same row or column of that initial square, but they must lie outside its box. You, as Zapmaster, have chosen the order of boxes, so the zapping power is directed only at the squares of the next box in the order of boxes. When a square zaps a square in another box which contains the pattern digit, it makes that other square ***ineligible*** for the subpattern being calculated. Let us suppose that all the squares but one in that other box are made ineligible by having been zapped by the zapping square. Let's consider an example. We'll restrict our attention to the middle three rows of a sudoku:

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row4						1 ₁			1
row5		1					1		
row6	1					1			

Let's suppose that the middle box, as well as the starting square **(46)** within it, has been chosen by you as the beginning of subpattern-1, with the box order **E → F → D**.. Then you perform the following action

square **(46)** zaps square **(49)**

Since square **(49)** has been zapped, it is no longer eligible for inclusion in subpattern-1. This leaves one square only as a possible member in box F, namely square **(57)**, which then becomes the second member of subpattern-1.

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row4						1 ₁			1
row5		1					1 ₁		
row6	1					1			

If, subsequently, square **(57)** zaps square **(52)**, the result is:

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row4						1 ₁			1
row5		1					1 ₁		
row6	1 ₁					1			

When we have completed subpattern-1, we must choose a beginning for subpattern-2. There isn't much choice in this case, as there's only one square left in starting box E

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row4						1 ₁			1
row5		1					1 ₁		
row6	1 ₁					1 ₂			

In this case, it would be much better if we could switch the box order and put box D next, because if E were next, box F would become a phony pending box, ending up by creating a contradiction up the line, necessitating a return to this point, erasing the digit 2 in every square along the way and selecting whichever of the two candidates caused all the trouble (by having created a false subpattern). At any rate, we travel back through time and change the box order to **E→D→F** before continuing subpattern-2.

Square (66) zaps square (61), adding square (52)

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row4						1 ₁			1
row5		1 ₂					1 ₁		
row6	1 ₁					1 ₂			

Our last step is: Square (52) zaps square (57) adding (49)

which then results in

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row4						1 ₁			1 ₂
row5		1 ₂					1 ₁		
row6	1 ₁					1 ₂			

In the next example, we have a four-box problem. Box G has three candidate squares, while the other three boxes, A, D and I, have two candidate squares each. We'll see why it is easiest to always make the box with the most candidate squares the starting box. We'll try two different box orders

2	006	D	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
					X						
row1											
									1		1
row2											
				X							
row3							X				
row4										X	
row5	1	1									
row6	1	1							1		
row7					X						
row8		1									1
row9											

We'll first try this problem using the box order **C→I→G→D**

		C
D		
G		I

We'll begin with box C, choosing square (27) as the starting square of the first subpattern, subpattern-1. We'll mark it with the subscript 1. We'll use it to find the second member of subpattern-1 in box I, by performing the action:

Square (27) zaps square (77), adding square (99) to subpattern-1

Remember that squares can only zap squares in other boxes, when those other squares are either in the same row, or the same column of the square that is doing the zapping.

2	006	D	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
					X						
									1 ₁		1
				X							
						X					
									X		
	1	1									
	1	1							1		
					X						
		1									1 ₁

The rest of this page is illustrated by the diagram on the next page

We'll go on to update box G with box I, with the action:

Square (99) zaps square (92) adding square (71) and pending square (72)

This time, two squares were left after the zapping. We arbitrarily chose square (71), which meant that square (72) had to be placed on hold, for later addition to the next subpattern. We could just as easily have added (72) and pending (71). The same results would be achieved, except that subscripts 1 & 2 would be swapped for all boxes following box G. The results of this last action will be shown on the next page.

We not only subscript the 1 in square (72) with a P. We also pencil in a large P in the box itself. We do this because we don't want to forget that box G is a pending box. Later, when we include square (72) in the next subpattern, we'll erase the pending P, and the small subscript P will be replaced by the digit 2, because it will be a member of the next subpattern, subpattern-2.

Note the pending P as well as the subscript p in box G.

2	006	D	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
					X						
row1											
									1 ₁		1
row2											
				X							
row3											
						X					
row4										X	
row5											
	1	1									
row6											
	1 ₁	1 _P						1			
row7											
					X						
row8											
		1	P								1 ₁
row9											

Now we shall update box D with the action

Square (71) zaps square (61) adding square (62) to subpattern-1.

This completes subpattern-1, since there is now a member of subpattern-1 in every pattern box. Notice that there are no members of subpattern-1 in boxes A, B, E, F, and H. That's because there are established 1's (in the form of large X's) in those boxes, which do not tolerate 1-candidates.

(You, as Zapmaster, always return to the starting box after finishing a subpattern, to ensure that every candidate square in the starting box, or any of the other boxes, has either been made a member of a subpattern, or disqualified as a candidate.)

Back at the starting box, there is a pending condition in box G, so you, as Zapmaster, must begin a **sister** subpattern to subpattern-1, one which begins in the same starting square in the starting box, and which shares squares all the way to the pending box, in the same sequence of boxes followed by subpattern-1, at which point this sister subpattern will part ways with subpattern-1 by taking possession of the pending square as its own member in the pending box.

The sudoku below is the picture you, as Zapmaster, are presented with when you return to the starting box C, with the box order **C→I→G→D**.

2	006	D	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
					X						
row1											
									1 ₁		1
row2											
				X							
row3											
						X					
row4											
									X		
row5											
	1	1 ₁									
row6											
	1 ₁	1 _P						1			
row7					X						
row8		1	P								1 ₁
row9											

The pending condition requires that you give equal opportunity to the pending square as a rightful inheritor of the sequence of squares, (27) and (99), as members of a new **sister** subpattern. Consequently, you begin subpattern-2 in the same starting square (27) as subpattern-1, and then you dutifully continue it in square (99). When you get to box G in the box order, you see the pending P and remember that subpattern-2 must be continued in the pending square (72). So you replace the subscript p with a 2 and erase the pending P. You then perform the next action

Square (72) zaps square (62) adding square (61) to subpattern-2

Notice that this action really goes on in your head, and is carried out with your pencil as you add subscripts and pencil in pending P's. Clearly, none of this get written down, except for the new subscripts and the penciling in and erasing of the pending P's.

Now when you return your attention to the starting box, C, you are aware that there is no pending situation at the moment, so your next item of business is to check for any unassigned squares in box C, and you note that square (29) has no subscripts, and therefore no membership yet in a subpattern. Your duty is to fill this void, and begin a new subpattern-3 in square (39) and update box I, next in the box order, with the action:

Square (29) zaps square (99) adding square (77) to subpattern-3

The result of this action is below:

2	006	D	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row1			X						
		row2							1 ₁₂		1 ₃
		row3				X					
		row4						X			
		row5								X	
		row6	1 ₂	1 ₁							
		row7	1 ₁	1 ₂					1 ₃		
		row8					X				
		row9		1							1 ₁₂

On the next action, we'll see some new notation. In this action, square (77) will zap **both** squares (71) and (72), leaving square (92) as the sole survivor.

Square (77) zaps square (71) & square (72) adding square (92)

2	006	D	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row7	1 ₁	1 ₂					1 ₃		
		row8					X				
		row9		1 ₃							1 ₁₂

The final action will be to update box D with box G:

Square (92) zaps square (62) adding square (61)

Back at the starting box C, all squares are members of subpatterns, and there are no squares in other boxes which are unclaimed. This completes the pattern analysis.

2	006	D	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row1			X						
		row2							1 ₁₂		1 ₃
		row3				X					
		row4						X			
		row5								X	
		row6	1 ₂₃	1 ₁							
		row7	1 ₁	1 ₂					1 ₃		
		row8					X				
		row9		1 ₃							1 ₁₂

This time you choose G as the starting box. Even though you know the solution, it won't help, because you've got to follow the rules and proceed step by step. You choose square (72), with the box order **G→D→I→C**. Then you upate box D with the action:

Square (72) zaps square (62) adding square (61)

2	006	D	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row1			X						
		row2							1		1
		row3				X					
		row4						X			
		row5								X	
		row6	1 ₁	1							
		row7	1	1 ₁					1		
		row8					X				
		row9		1							1

Notice that boxes D and I in the box order **G→D→I→C** are not adjacent to one another, and share no rows or columns. But box G can take care of box I. **It isn't obligatory that each box in the box order has to be responsible for the next box.** Previous boxes with members of the same subpattern are always ready to contribute their zapping powers..

So in this case, the action to take is:

Square (72) zaps square (77) adding square (99)

2	006	D	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
					X						
row1											
									1		1
row2											
					X						
row3											
							X				
row4										X	
row5											
row6											
row7											
row8											
row9											

The final action is:

Square (99) zaps square (29) adding square (27)

This completes subpattern-1. Next, you choose square (92) as the starting square of subpattern-2, and perform the action

Square (92) zaps square (99) adding square (77)

Notice that we no longer bother with the subpattern name after **adding**. That is because we can only work on one subpattern at a time, so there should never be a doubt about what the present subpattern is. **Adding** means adding to the current subpattern. It is important that we have a way of making it official that square (77) is now a member of the current subpattern, giving it the rights of zapping power. The keyword **adding** fills that need. It is also useful in that it makes the point that the subpattern itself is growing as we add pattern members, and therefore has more zapping power.

The final action in calculating subpattern-2 is

Square (77) zaps square (27) adding square (29)

2	006	D	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
					X						
									1		1 ₂
					X						
							X				
										X	
		1 ₁	1								
		1	1 ₁						1 ₂		
						X					
			1 ₂								1 ₁

This completes subpattern-2, and when a return is made to the starting box G, a final subpattern-3 is begun in the remaining square (71). Our next action is to update box D, the next box in the box order **G→D→I→C**

Square (92) zaps square (62) adding (61)

Then, the zappers turn their zap guns around and aim them in the direction of box I, the third box in the sequence of boxes, and perform the action

Square (71) zaps square (77) adding (99)

The final action

Square (99) zaps square (29) adding square (27)

completes the update. See the diagram on the next page.

[illegible]

Notice that the subscripts are different in the two solutions (the previous solution is at the top of page 10, three pages back). This difference was caused by the difference in choice of beginning squares for the three subpatterns, and amounts to nothing more than a simple transposition of digits,

$$\begin{array}{l} 1 \rightarrow 2 \\ 2 \rightarrow 3 \\ 3 \rightarrow 1 \end{array}$$

The importance of the two updates is that using the box with the greatest number of squares results in there being no pending situation. This will not always be the case. Pending situations are not always avoidable, but it is always best to avoid them when possible. The next example has a pending condition in either of two boxes, box D and box F. Whichever is chosen as the starting box, the other becomes a pending box.

2	016	ML	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row4			5					5	
		row5	5			5			5		
		row6	5			5			5		

If we make box D the starting box, then when a subpattern is begun in square (43),

Square (43) zaps square (48) adding square (57) and pending square (67)

On the other hand, if we make box F the starting box, then when a subpattern is begun in square (48)

Square (48) zaps square (43) adding square (51) and pending square (61)

Every time a zapping is made of a square in a box with three squares, two squares are left unzapped. One of them may be chosen as a member of the subpattern being developed, but the other must always be a pending square.

Some additional language:

3	009	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row7				1 ₁			1		1
	row8			X						
	row9				1	1		1 ₁		

Zapping can take out more than one square at a time. In the situation above, square (74) can zap both squares (77) and (79).

Square (74) zaps square (77) & square (79) adding square (97)

Notice the use of the underline. It's used in place of a pair of enclosing parentheses because parentheses are used to enclose the coordinates of a square. It keeps the zap language from looking too cluttered.

Another instance in which an underline is used is when two actions have a collective effect, as with: **square (82) zaps square (88) and square (94) zaps square (97):**

2	012	W6	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row7					2				2
		row8		2 ₁						2	
		row9			2	2 ₁			2		

Square (82) zaps square (88) & square (94) zaps square (97) adding square (79)

Notice the length of the last zap statement. See how cluttered it is, like not being able to see the trees because of the surrounding forest. It is not the intent of zap language to be so dense. Its purpose is to communicate quickly and understandably. We shall therefore make a further inroad on the readability of zap language, although its purpose is to attain greater clarity, as well as the ability to understand the action at a glance.

Therefore, except on the occasion of clarity, the word **square** shall no longer be used to specify a square. Instead, we shall rely solely on the pair of parentheses and the enclosed coordinate pair of row and column numbers.

The statement on the bottom of the previous page then becomes simplified:

(82) zaps (88) & (94) zaps (97) adding (79)

A second consideration is that when the entire line is in bold, it doesn't cause anything in particular to stand out. We choose therefore to reserve the bold typeface for information which changes, like the coordinates of squares, as well as showing active agents as opposed to passive ones. The statement above now looks like:

(82) zaps (88) & (94) zaps (97) adding (79)

Now the active agents, the squares **(82)** and **(94)**, as well as the result, **(79)**, can be clearly seen. The underline avoids clutter, the keywords **zap** and **adding**, since they are the two main underpinnings of the zap language, are expected, and therefore do not need to stand out. Since there is little else to the zap language, its sometimes apparent complexity is really little else than the multiple usage of statements like the one above.

There is one remaining wrinkle in the use of the zap language. It is used to reduce the repetitive and cumulative nature of zap actions, and is what is popularly called a **run-on sentence**. An example in English would be:

The teenager struck the child who yelled to the mother who called the policeman

There are three actions here, **struck, yelled, and called**, and the guiding principle of the sentence structure is that the passive object of one action becomes the active agent of the next action. Although run-on sentences are disliked by most, when the parts of the sentence are all related, as in the above example, the overall sense, and in particular the interconnectedness of the individual events, is better understood at a glance than from looking at the sequence of statements:

The teenager struck the child.
The child yelled to the mother.
The mother called the policeman.

It also uses the lines on the page more frugally, and, when used properly, creates less of a feeling of clutter. Short descriptions sometimes bring out the immediacy of cause and effect.

For these reasons and others, the zap language allows (and is frequently used in) run-on zap statements like the following:

(87) zaps (37) adding (19) zaps (14) adding (34)

This means the same as:

(87) zaps (37) adding (19)
(19) zaps (14) adding (34)

The adoption of the philosophy of zapping stemmed from a passion for direct and succinct connections, making it easier to know why something was being done, and what it led to. Our sprawling English language often seems to turn into a morass of unintended implication, compared to which formulaic language is a godsend. The run-on treatment hooks up together a string of seemingly disparate actions into a fathomable sequence of events. It makes it clear why anyone would go to the bother of zapping (37) above, when it is seen as a stepping stone to identify (34) as a bona fide extension of the subpattern being analyzed.

The zap language, albeit perhaps too formulaic, enables you to see at a glance when reading this text, to see whether, for example, all the members of a subpattern have been discovered. It is intended as a convenience for you in thinking about, using, and learning the underlying (simple) theory. Once you are solidly into using zap language, you need only realize its implications, so that it can assist you in deciphering the sudoku, and planning your next action.

The next item of importance is care and precision in following the box order. It might be of use to jot it down. Whenever you encounter a pending box with a false candidate, you are obliged to backtrack along the path that got you there, erasing the false candidate. You are obliged to be a **box accountant** when using this method, what the order is, when you can change it, how to know when you've finished analyzing a subpattern, whether to add a new subscript to all the squares leading from the starting box to the pending box, and what to do when you discover a square which somehow cannot be made a member of any subpattern.

Another way of showing the simultaneity and coordination of two actions is with the use of the keyword **while**. It is used when each of the actions zaps a different square or set of squares, but the result of both actions is that a single square is isolated, becoming the next member of the subpattern.

4	019	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row7	3 ₁				3			3	
	row8	3			3				3 ₁	
	row9	3				3 ₁				

(88) zaps (81) while **(95)** zaps (91) adding **(71)**

The alternative method would be:

(88) zaps (81) and **(95)** zaps (91) adding **(71)**

When a run-on zap statement runs out of room on a line, it can be simply continued on the next, always indenting the next line. Such continuations are seldom used.

(17) zaps (97) adding **(98)** zaps (58) adding **(69)** zaps (65) adding **(69)** zaps (66)
adding **(54)** zaps (14) adding **(25)** zaps (21) adding **(31)**

When you read a statement like this, you are also keeping an eye on the sudoku being updated, and you see each action separately. You first see how (98) is added as a result of (17) zapping (97). Then you see how (69) is added as a result of zapping (59), and so on. When you have become adept with the concept of zapping as well as with the use of the zap language, you begin to see

"(17) zaps (97) adding (98)"

as a single action, linking (17) to (98)

and your scanning of the entire run-on zap statement becomes a linking of consecutive pattern members, seven in a row, all in bold. You see only the bold squares, and demote the unbold squares to nothing but cannon fodder for the zapping process, seeing them only as obstructions to be dismissed, being little more than part of the geometry of the box

There is one further simplification, but it does not occur in a zap statement. It is the designation of a box, with will, most of the time, consist of nothing but the capital letters A, B, C, D, E, F, G, H, and I for the nine boxes. Instead of "**box A**" we will just use "**A**"

Now we get to the second most important part of a zap statement. When one or more squares in the same box are zapped, and more than one square remains unzapped, then a choice must be made as to which one is to be added to the subpattern, and which one(s)

is/are to be placed in a pending status, awaiting its/their assignment(s) to a future subpattern.

An explanatory situation is the following sudoku segment:

4 006	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row 7			5		5 ₁	5			5
row 8	5					5			5
row 9			5		5				

Remember that although zapping only operates within rows or columns, the purpose of zapping is to reduce the box whose rows and/or columns are being zapped, so the consequences of zapping are those squares in the box which escape being zapped, and it is from the ranks of those escapees, the **unzapped** squares, that you, the zapmaster, must make the selections for squares to be added and squares to be pended.

Let us first consider the action of (75) zapping (79):

(75) zaps (79) adding (89)

4 006	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row 7			5		5 ₁	5			5
row 8	5					5			5 ₁
row 9			5		5				

Here, there is no choice. Square (89) is forced. But imagine instead the action

(75) zaps (73) adding (??)

What square shall (??) be chosen to be? It's easy, when we introduce the next new piece of zap language, the **pending** keyword.

Let us return to the bottom three rows again, and this time point the zap guns in the opposite direction:

(75) zaps (73) adding (81) and pending (93)

4 006	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row 7	<i>P</i>		5		5 ₁	5			5
row 8	5 ₁					5			5
row 9			5 _P		5				

The reason that the *pending square* (93) is in *italics* as well as bold is to remind us that it is *not* going to be a member of the subpattern under analysis. It will become a member of the *next* subpattern, subpattern-2. The "p" will be replaced by a "2" when the time comes for subpattern-2. (One must always remember to pencil a P in the box, just for good measure. It must be erased when the pending square is given a real subscript).

In the next situation, still using the bottom three rows, the update is from the box with less pattern squares to the one with more, G to H.

(81) zaps (86) adding (75) and pending (76)&(95)

4 006	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row 7	<i>P</i>		5		5 ₁	5 _p			5
row 8	5 ₁					5			5
row 9			5 _P		5 _q				

In this case, both (76) and (95) are placed on hold. The choice is still open as to the order in which they are to be chosen, which is entirely up to you.

Pending situations.

The single most complicated feature of the calculation of subpatterns is the pending situation, so it is important that we spend some time discussing it, as well as the zap language associated with it.

When subpatterns are analyzed, it is a ***one-at-a-time*** process. A subpattern is always completely determined before the calculation of the next subpattern is undertaken. Pending situations are those in which more than one candidate within a particular box is available to a subpattern. Only one candidate may be chosen for the subpattern, and the rest must be placed on hold for the next subpattern(s). We accomplish this by giving the pending squares the false subscripts p, q, r, and so forth (you will probably never encounter a situation in which there are more than two pending squares, or in which more than two pending situations exist at the same time).

When, in the course of analyzing (calculating) a subpattern, two or more squares in the same box remain unzapped, only one of them can be chosen for the present subpattern, and the other one (or two) must be given pending subscripts (p, q, etc.), and a pending P must be penciled in the box as a reminder of the pending situation. Then the analysis of the subpattern must pass to the next box in the box order.

When the subpattern is complete, and you are back at the starting box, and a pending condition exists, you must begin a new subpattern in the same starting square as the preceding subpattern, adding the new subscript to all the squares containing the previous subscript, and when the pending box is arrived at, one of the pending squares in that box must become the next member of the new subpattern. If it is the only pending square in the pending box, then the pending P in the box must be erased, the pending square must be selected as the next member, and its pending subscript replaced by the subscript of the new, present subpattern. If there is yet another pending square in that same pending box, the pending P must not be erased, and that second pending square will become a member of yet another new subpattern, not to be started until the present subpattern is complete.

Note that the starting box never becomes a pending box, although it has many similarities to one.

Once the pending square has been assigned to a subpattern, control always continues on with the next box in the box order. If the pending box is the last one in the box order, then, the next box is the starting box, where there are either no more subpatterns to be started, or where the next subpattern will begin.

The order of boxes is the order in which boxes are evaluated in calculating a subpattern. The direction of the box order is considered to be ***downstream***. A box which is ***upstream*** from another is one which is earlier in the box order.

While a box is pending, it is possible for another box to become pending. This new pending box is always ***downstream*** from the first pending box, and is called a ***higher pending box***.

Higher pending boxes are *always* resolved before **lower pending boxes**. No new squares are allowed to be developed in any box **upstream** from the highest pending box. As boxes upstream from the highest pending box are encountered, no **new squares can be added**, the new subscript always being **slavishly** placed in the **same** square as the preceding, old subscript, **until** the highest pending box is no longer pending. At that point the **next highest** pending box becomes the highest.

It is vitally important to always label **new pending P's** with subscripts **higher** than any of the **present pending P's**, so that **higher** pending P's will always have a **higher** subscript than lower ones. When there is no pending P and a new pending P is being added, the numbering can, but need not, be started all over again.

Note that it is not logically possible, if you follow the rules, for a new pending condition to occur in a box which is upstream from an existing pending condition. **New** pending conditions *always* occur **downstream** from existing pending conditions. A pending condition **cannot be resolved** when there exists a pending condition **downstream** from it.

Thus if a pending box has three pending squares, it will take three additional subpatterns to be started before the pending condition in that box can be resolved.

In this fashion, it is guaranteed that all possible subpatterns will be discovered.

Blind Alleys and Killer Candidates

Situations occur when a subpattern cannot proceed any further because there is no square left unzapped in the next box in the box order. This can only occur when every square in that box has been zapped by the members of the subpattern being developed. These are cases in which the would-be subpattern has no continuation. They are called **blind alleys**, and must be **abandoned**. This is accomplished by **backtracking**, box by box, in the sequence of assignments made for that subpattern number, until the starting box is reached, removing the subscripts from every square along the way, including from the starting square itself, and no further subpatterns may be begun in that square in the starting box. If there are other squares in the starting box which have not yet been included in a subpattern, then the subpattern number, which has been painstakingly removed from all of its squares as a result of this blind alley, must be reassigned to a **new subpattern** beginning in one of those other squares, so that a gap in subpattern digits does not occur.

Blind alleys can occur as a result of pending situations, but they can also occur normally. They are the only way in which a square can end up not being assigned to a subpattern, but for that to be so, such a square will have been tried out as a possible member of every subpattern, and will have led to a blind alley in every instance. Such a square is labeled as a **killer candidate**, a terminology which will be explained later. It cannot be a real candidate, but is left in the pattern analysis with the **subscript k**.

Blind alleys do not occur frequently, but one must be prepared for their occasional manifestation.

Killer candidates are tested by every candidate during the subpattern analysis, but that testing is not always evident to the solver, as they simply are always among the zapped squares. The solver is often not aware of them until the analysis is complete, and they are the squares which have received no subscripts. It is at such a time that they are generally given the k subscript.

Example of the solution of a sudoku being expressed in zap language:

2	081	X1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1								X		
	row2			X							
	row3						X				
	row4	2				2				2	
	row5	2				2					
	row6	2				2				2	
	row7				X						
	row8		X								
	row9									X	

Since the top and bottom bands have no candidates, we'll leave them out till the end.

2	081	X1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row4	2				2				2	
	row5	2				2					
	row6	2				2				2	

Subpattern-1 is started in **(41)** with box order **D→F→E**

(41) zaps (49) adding **(69)**.

(41) zaps (45) while **(69)** zaps (65) adding **(55)**

Subpattern-1 = **(41),(69),(55)**

D F E

There are three actions above which give values to the subscripts in the middle three boxes. The first action is: Subpattern-1 is started in **(41)** with box order **D→F→E**. This causes the subscript "1" to be appended to the 2 in square (41):

2	081	X1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row4	2 ₁				2				2
		row5	2				2				
		row6	2				2				2

The second action is: **(41)** zaps (49) adding **(69)**.

This causes the subscript "1" to be appended to the 2 in square (69): It does this by limiting the adding statement to apply only to square (69), the only eligible pattern square left in box F (rightmost box) after the zapping action.

2	081	X1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row4	2 ₁				2				2
		row5	2				2				
		row6	2				2				2 ₁

The third action is: **(41)** zaps (45) while **(69)** zaps (65) adding **(55)**

It causes the subscript "1" to be appended to the 2 in square (55), the only pattern square remaining in box E (middle box) after the zapping action.

2	081	X1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row4	2 ₁				2				2
		row5	2				2 ₁				
		row6	2				2				2 ₁

The final zap statement is a summary of the three members of subpattern-1. Beneath each of the three members is the name of the box in which the member is found. Those boxes are D, F, and E. The three boxes are listed in the same order as in the box order statement. That order has no further meaning after the three members have been identified. It was simply used to discover the three members, and another order could have been used. The members themselves may be placed in any order, the important

piece of information being the box each is located in, which could easily be deduced from the coordinates of the square.

The zap language showing the calculation of subpattern-2 is the following:

Subpattern-2 is started in **(51)** with box order **D→F→E**

(51) zaps (55) adding **(45)** and pending **(65)**.

(45) zaps (49) adding **(69)**

Subpattern-2 = **(45),(69),(54)**

D F E

The first action is: Subpattern-2 is started in **(51)** with box order **D→F→E**

The result is below:

2	081	X1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row4	2 ₁				2				2
		row5	2 ₂				2 ₁				
		row6	2				2				2 ₁

The second action is: **(51)** zaps (55) adding **(45)** and pending **(65)**.

The result is below:

2	081	X1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row4	2 ₁			P	2 ₂				2
		row5	2 ₂				2 ₁				
		row6	2				2 _p				2 ₁

The third action is: **(45)** zaps (49) adding **(69)**

The result is below:

2	081	X1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row4	2 ₁			P	2 ₂				2
		row5	2 ₂				2 ₁				
		row6	2				2 _p				2 ₁₂

The zap language showing the calculation of subpattern-2 is the following:

Subpattern-3 is started in **(51)** (same as subpattern-2) with box order **D→F→E**

due to the pending action in box **E**, subpattern-3 must
begin in the same starting square **(51)** as subpattern-2
include the pending square **(55)**

(65) zaps (69) adding **(49)**

Subpattern-3 = **(51),(65),(49)**
D F E

Note the addition of a new keyword in the zap language, the **due to** statement. This is a reminder for you, to remember that the subpattern which follows the subpattern which created a pending box and pending square must start in the same starting square, and share every square of subpattern-2 until the pending box, E is reached, at which time the pending square must be the member in subpattern-3. In this example, there are no squares between the starting and pending boxes, so this second warning does not appear.

In the general situation, the **due to** statement has the form:

due to the pending action in box X, subpattern-N+1 must
begin in the same starting square **(ab)** as subpattern-N
share squares **(ab), (cd), . . .** with subpattern-N
include the pending square **(yz)**

where (ab), (cd), . . . is the list of squares between, (but not including) the starting and pending squares. Note that only the square designations above are in bold.

This statement is a reminder to you, as zapmaster, to add the shared squares to the subpattern which follows the pending action. In the example **which precedes the general statement above**, the pending box immediately follows the starting box, and there are no squares in between, so you don't need to be reminded.

Since two of the squares of subpattern-3 are forced (the starting and pending squares), so only one square needs to be calculated, which is accomplished by the sole action:

(65) zaps (69) adding **(49)**

The final pair of lines

Subpattern-3 = **(51),(65),(49)**
D F E

summarizes the findings. Note the list of boxes underneath the subpattern members, showing the boxes they are located in. This isn't necessary, since you could locate them from their coordinates. It simply makes it easier for you to understand the result, since

you can now compare them to the box order at the beginning. Sometimes, when there is insufficient room on the page, the line of box names (D F E) is incorporated with the list of subpattern members (*this is done rarely*):

Subpattern-3: **D(51), (F(65), E(49))**

After the update, we move the updated middle section back into the sudoku:

2	081	X1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X		
row2			X								
row3							X				
row4	2 ₁				2 ₂					2 ₃₄	
row5	2 ₂₃				2 ₁₄						
row6	2 ₄				2 ₃					2 ₁₂	
row7				X							
row8		X									
row9									X		

The one question which might still linger in your mind is why we updated the boxes in the order **D→F→E**, rather than **D→E→F**. That's because two squares must be used to zap the three squares of the middle box, in order to leave only one, and updating F first works because F has only two squares, so one square in box D can eliminate one square in box F, and then that one square in D and that one square in F can team up to eliminate two of the squares in E, leaving only one to become the result in E. Simple.

2	081	X1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row4											
row5											
row6											

Some final remarks on notation:

Pattern analysis begins with an arbitrarily chosen square, and an arbitrarily chosen order of boxes, then grows square by square, and as each new square is added, so is the total zapping power of the growing subpattern. Its zapping power grows by addition.

Consider the following paragraph, taken from the previous pattern analysis:

We choose **(83)** as the first member in **G**, which zaps (53) in **D**, making **(51)** the member in **D**. **(83)** also zaps (23), making **(32)** the member in **A**, which zaps (39) in **C**, making **(19)** the member in **C**, which zaps (16) in **B**, making **(26)** the member in **B**, completing subpattern-3.

This language can be more simply and directly expressed in the following manner:

(83) zaps (53) adding **(51)**.

(83) zaps (23) adding **(32)** zaps (39) adding **(19)** zaps (16) adding **(26)**

Subpattern-3 = **(83),(51),(32),(19),(26)**
 G D A C B

Here, the term "adding" is taken to mean that the square following the term is added to the subpattern being developed. The sequence of keywords "zaps" and "adding" explains the zapping of unwanted squares and subsequent adding of desired squares to the subpattern, which then are used to zap another unwanted square.

Note the list of subpattern boxes beneath the list of subpattern members, showing which boxes those members are in.

Another device is the use of an underline to show inclusion:

(88) zaps (82) & **(75)** zaps (72) adding (93)

(57) zaps **(51)** & **(53)** adding **(43)**

It is hoped that this new language will simplify and enhance the process of explanation.

General Remarks

The pattern examples used in this text all came from real sudokus. Except for bipatterns, none has been invented for the sake of example. The pattern digit has also not been altered, although there is no advantage to this, and the large X's showing the position of the established pattern digits have been retained, although, again, there is no advantage.

The one area which has not been properly represented is that of the simplest bipatterns, which have not been kept count of, and therefore not tallied with the other patterns to show their numbers. More sudokus were solved by bipatterns than by any other pattern, on a better than two-to-one basis.

It is intended to eventually include sections on the 5-subscript and 6-subscript patterns, and more material will be developed on box codes, picture codes, and their interrelationships, as well as a single box code system for all six pattern groups, and a more meaningful and useful alpha code.

In addition to all of this, I am still collecting successful patterns, adding at least one new pattern every day from the two or three sudokus that I solve, and intend to incorporate these as well into this study, which will therefore grow at a rate of at least 300 a year.

My search for an organizing principle in reducing the number of sudokus to be solved in this study turned out in the end to be the method of solving itself, with the introduction of the Zap language for its simplification in description of that solving process, and the internal similarity of solving examples. I hope the Zap language proves successful. It certainly reduced the sheer amount of verbiage previously necessary, and made this project a manageable one.

Chapter 1. Patterns with 1 subscript.

Simple bipatterns

A simple bipattern is defined as two candidate pairs in opposing boxes. Each pair must share a box. If the two pairs face each other vertically, it means that each pair consists of two candidates in the same row and same box, and that the corresponding members share columns. If they face each other horizontally, each pair consists of two candidates in the same column and box, and each pair of corresponding members share a row.

Below is a pattern composed of a bipattern. Let us solve it. The pattern exists in two boxes, A and D.

Subpattern-1 begins in square **(11)** with the order of boxes **A→D**.

(11) zaps (41) adding **(43)**

Subpattern-1 = **(11),(43)**
A D

Subpattern-2 begins in square **(13)** with the order of boxes **A→D**
(13) zaps (43) adding **(41)**

Subpattern-2 = **(13),(41)**
A D

Back at the starting box, there is no pending situation anywhere and no square in the starting box lacking a subpattern. The completed pattern analysis is below.

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	1 ₁		1 ₂						
row2					X				
row3							X		
row4	1 ₂		1 ₁						X
row5				X					
row6									
row7						X			
row8		X							
row9								X	

The next two pages show a few examples of simple bipatterns.

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				9 ₁		9 ₂			
row2		X							
row3									X
row4	X								
row5				9 ₂		9 ₁			
row6								X	
row7			X						
row8							X		
row9					X				

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									
row2			1 ₁					1 ₂	
row3			1 ₂					1 ₁	
row4							X		
row5				X					
row6	X								
row7									X
row8									
row9									

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						X			
row2			X						
row3								X	
row4	X						X		
row5				X					
row6									
row7									X
row8		2 ₁			2 ₂				
row9		2 ₂			2 ₁				

For horizontal pairs,
there are 27 columnar arrangements of two pairs
and 9 row arrangements for a single pair,
making $27 \times 9 = 243$ vertically facing pairs.

By a similar argument,
there are 243 horizontally facing pairs,
making altogether $243 + 243 = 486$ possible simple bipatterns.

Despite their simplicity, simple bipatterns solve more sudokus than any other kind of pattern. There are many instances in which the venerated sudoku masters would cringe at the ease with which bipatterns solve their otherwise complicated sudokus.

Pattern Code	Box Orientation	Patterns with the same box code
2 – 2 – 2	G – H – I	033

G	H	I

Subpattern-1 begins in (73) with the box order **G→H→I**

(73) zaps (74) adding (94) zaps (98) adding (88)
(94) zaps (98) adding (88)

Subpattern-1 = (73),(94),(88)
 G H I

Subpattern-2 begins in (83) with box order **G→I→H**

(83) zaps (88) adding (98) zaps ((94) adding (74)

Subpattern-2 = (83),(98),(74)
 G I H

Back at the starting box, nothing is pending, and no squares remain unclaimed. We are done.

1	017	A1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
									X		
			X								
						X					
							X				
			X								
											X
					5 ₁	5 ₂					
					5 ₂					5 ₁	
						5 ₁				5 ₂	

Example 1.033

Although this pattern is related to the $2 - 2 - 2$ group (preceding page), it must be derived from it by a 90 degree rotation, so we shall examine it separately.

A		
D		
G		

Subpattern-1 begins in **(11)** with box order **A→G→D**.

(11) zaps (81) adding **(82)** zaps (62) adding **(63)**

Subpattern-1 = **(11),(82),(63)**
A G D

Subpattern-2 begins in **(13)** with box order **A→D→G**

(13) zaps (63) adding **(62)** zaps (82) adding **(81)**

Subpattern-2 = **(13),(62),(81)**
A D G

1	033	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		3 ₁		3 ₂						
row2				X						
row3								X		
row4					X					
row5										X
row6		3 ₂	3 ₁							
row7						X				
row8		3 ₂	3 ₁							
row9								X		

Pattern Code	Box Orientation	Patterns with the same box code
2 – 2	I – F	032
2	G	

		F
G		I

Box order: **F→I→G**

Subpattern-1 is begun in **(48)** zaps (78) adding **(89)** zaps (89) adding **(71)**

Subpattern-1 = **(48),(89),(71)**
F I G

Subpattern-2 in begun in **(49)** zaps (99) adding **(78))** zaps (71) adding **(81)**

Subpattern-2 = **(49),(78),(81)**
F I G

Back at the starting box, nothing is pending and no squares remain un-claimed. We are done.

1	006	A2	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X								
row2					X						
row3							X				
row4									3 ₁	3 ₂	
row5		X									
row6						X					
row7	3 ₁								3 ₂		
row8	3 ₂									3 ₁	
row9				X							

Pattern Code	Box Orientation	Patterns with the same box code
2 – 2 2 – 2	B – A G – H	035

A	B	C
D	E	F
G	H	I

Box order: A→B→H→G

Subpattern-1 starts in **(23)** zaps (36) adding **(34)** zaps (94) adding **(76)** zaps (72) adding **(92)**

Subpattern-1 = **(23),(34),(76),(92)**
A B H G

Subpattern-2 starts in **(33)** zaps (34) adding **(26)** zaps (76) adding **(94)** zaps (92) adding **(72)**

Subpattern-2 = **(33),(26),(94),(72)**
A B H G

Back at the starting box, there is no pending condition and no unclaimed squares. We are done.

1	020	A4	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1											X
row2			3 ₁				3 ₂				
row3			3 ₂	3 ₁							
row4	X										
row5					X						
row6							X				
row7		3 ₂					3 ₁				
row8									X		
row9		3 ₁		3 ₂							

Pattern Code	Box Orientation	Patterns with the same box code
2 - 2 - 2	G - H - I	none
2 - 2	E - D	

D	E	
G	H	I

Box order: **E→D→G→H→I**

Subpattern-1 begins in **(44)** zaps (43) adding **(51)** zaps (91) adding **(73)** zaps (77) adding **(87)** zaps (85) adding **(95)**

Subpattern-1 = **(44),(51),(73),(87),(95)**
E D G H I

Subpattern-2 begins in **(54)** zaps (51) adding **(43)** zaps (73) adding **(91)** zaps (95) adding **(85)** zaps (97) adding **(77)**

Subpattern-2 = **(54),(43),(91),(85),(77)**
E D G H I

Back at the starting box E, no pattern square remains unclaimed, and there is no pending situation. We are done.

1	034	A5	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1										X	
row2		X									
row3						X					
row4			7 ₂	7 ₁							
row5	7 ₁			7 ₂							
row6										X	
row7			7 ₁					7 ₂			
row8					7 ₂			7 ₁			
row9	7 ₂				7 ₁						

Pattern Code	Box Orientation	Patterns with the same box code									
$\begin{array}{c} 2 \\ \\ 2-2 \\ \\ 2 \end{array}$	$\begin{array}{c} F \\ \\ B-C \\ \\ H \end{array}$	none									
<table><tr><td></td><td>B</td><td>C</td></tr><tr><td></td><td></td><td>F</td></tr><tr><td></td><td>H</td><td></td></tr></table>		B	C			F		H			
	B	C									
		F									
	H										

Box H connects only to box B, and box F only connects to box C. Therefore one should be the starting box and the other the ending box. We'll choose H for the starting box, making the **box order** **H→B→C→F**.

Subpattern-1 begins in **(85)** zaps (35) adding **(26)** zaps (27) adding **(38)** **(38)** zaps (68) adding **(67)**

Subpattern-1 = **(85),(26),(38),(67)**
H B C F.

Subpattern-2 begins in **(86)** zaps (26) adding **(35)** zaps (38) adding **(27)** **(27)** zaps (67) adding **(68)**

Subpattern-2 = **(86),(35),(27),(68)**
H B C F.

Back at the starting box, nothing is pending and no square unclaimed. We are done.

1	024	A6	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X								
row2							4 ₁	4 ₂			
row3					4 ₂				4 ₁		
row4				X							
row5			X								
row6								4 ₁	4 ₂		
row7	X										
row8					4 ₁	4 ₂					
row9										X	

Pattern Code	Box Orientation	Patterns with the same box code
$\begin{array}{c} 2-2 \\ \\ 2-2 \\ \\ 2 \end{array}$	$\begin{array}{c} A-B \\ \\ I-G \\ \\ F \end{array}$	none

A	B	
		F
G		I

Box order: A→B→G→H→F

Subpattern-1 begins in (13) zaps (14) adding (24)

(13) zaps (93) adding (71) zaps (79) adding (98) zaps (68) adding (69)

Subpattern-1 = (13),(24),(71),(98),(69)

A B G H F

Subpattern-2 begins in (21) zaps (24) adding (14)

(21) zaps (71) adding (93) zaps (98) adding (79)

(79) zaps (69) adding (68)

Subpattern-2 = (21),(14),(71),(98),(69)

A B G H F

At the starting box A, nothing is pending & no squares unclaimed. We are done.

1	009	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			6 ₁	6 ₂						
row2	6 ₂			6 ₁						
row3							X			
row4						X				
row5		X								
row6								6 ₂	6 ₁	
row7	6 ₁								6 ₂	
row8					X					
row9			6 ₂					6 ₁		

Pattern Code	Box Orientation	Patterns with the same box code
2 – 2 2 – 2	A – B D – E	005, 013, 015, 019, 021, 022, 031, 039.

A	B	
D	E	

Box order A→B→E→D

Subpattern-1 begins in **(22)** zaps (26) adding **(35)** zaps (55) adding **(66)** zaps (62) adding **(53)**

Subpattern-1 = **(22),(35),(66),(53)**
A B E D

Subpattern-2 begins in **(33)** zaps (35) adding **(26)** zaps (66) adding **(55)** zaps (53) adding **(62)**

Subpattern-2 = **(33),(26),(55),(53)**
A B E D

At the starting box A, nothing is pending & no squares unclaimed. Done.

1 002 B1 col 1 col 2 col 3 col 4 col 5 col 6 col 7 col 8 col 9

row1								X
row2		1 ₁			1 ₂			
row3			1 ₂		1 ₁			
row4							X	
row5			1 ₁		1 ₂			
row6		1 ₂			1 ₁			
row7						X		
row8				X				
row9	X							

Pattern Code	Box Orientation	Patterns with the same box code
<pre> 2-----2 2-2 2-2 </pre>	<pre> A-----C D-E H-I </pre>	003, 007, 010, 011, 012, 014, 016, 025, 026, 028, 031, 039.

A		C
D	E	
	H	I

Box order A→C→I→H→E→D

Subpattern-1 begins in **(12)** zaps (18) adding **(27)** zaps (87) adding **(98)** zaps (95) adding **(86)** zaps (56) adding **(45)** zaps (42) adding **(51)**

Subpattern-1 = **(12),(27),(98),(86),(45),(51)**
A C I H E D

			col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
1	001	B9									
		row1		2 ₁						2	
		row2	2						2 ₁		
		row3				X					
		row4		2			2 ₁				
		row5	2 ₁					2			
		row6									X
		row7			X						
		row8						2 ₁	2		
		row9					2			2 ₁	

Pattern 1.001 continued.

A		C
D	E	
	H	I

Box order A→C→I→H→E→D

Subpattern-2 begins in (21) zaps (27) adding (18) zaps (98) adding (87) (87) zaps (86) adding (95) zaps (45) adding (56) zaps (51) adding (42)

Subpattern-2 = (21),(18),(87),(95),(56),(42)

Back at the starting box A, nothing is pending and no squares remain unclaimed. The pattern analysis is complete.

1	001	B9	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row1		2 ₁						2 ₂	
		row2	2 ₂						2 ₁		
		row3				X					
		row4		2 ₂			2 ₁				
		row5	2 ₁					2 ₂			
		row6									X
		row7			X						
		row8						2 ₁	2 ₂		
		row9					2 ₂			2 ₁	

Pictorial demonstration of Pattern 1 001.

We'll first show it for subpattern-1:

	1	2	3	4	5	6	7	8	9
1		2						2	
2	2						2		
3				x					
4		2			2				
5	2					2			
6									x
7			x						
8						2	2		
9					2			2	

Arbitrary choice of first member of subpattern-1 in box A..

	1	2	3	4	5	6	7	8	9
1		2						2	
2	2						2		
3				x					
4		2			2				
5	2					2			
6									x
7			x						
8						2	2		
9					2			2	

After zapping by first member, showing zapped area in dark. Forced choice of second member of subpattern-1 in box C.

	1	2	3	4	5	6	7	8	9
1		2						2	
2	2						2		
3				x					
4		2			2				
5	2					2			
6									x
7			x						
8						2	2		
9					2			2	

After zapping by second member of subpattern-1 in box C, showing zapped area in dark. Forced choice of third member of subpattern-1 in box I

	1	2	3	4	5	6	7	8	9
1		2						2	
2	2						2		
3				x					
4		2			2				
5	2					2			
6									x
7			x						
8						2	2		
9					2			2	

After zapping by third member of subpattern-1 in box I, showing zapped area in dark. Forced choice of fourth member of subpattern-1 in box H.

continued on next page

Pictorial demonstration of example 1 001, continued.

End of pictorial view of zapping by subpattern-1.

	1	2	3	4	5	6	7	8	9
1		2						2	
2	2						2		
3				X					
4		2			2				
5	2					2			
6									X
7			X						
8						2	2		
9					2			2	

After zapping by fourth member, showing zapped area in dark. Forced choice of 5th member of subpattern-1 in box E.

	1	2	3	4	5	6	7	8	9
1		2						2	
2	2						2		
3				X					
4		2			2				
5	2					2			
6									X
7			X						
8						2	2		
9					2			2	

After zapping by fifth member, showing zapped area in dark. Forced choice of 6th and final member of subpattern-1 in box D.

Pictorial view of zapping by subpattern-2:

	1	2	3	4	5	6	7	8	9
1		2						2	
2	2						2		
3				X					
4		2			2				
5	2					2			
6									X
7			X						
8						2	2		
9					2			2	

First member of subpattern-2 is the only remaining choice in box A,

	1	2	3	4	5	6	7	8	9
1		2						2	
2	2						2		
3				X					
4		2			2				
5	2					2			
6									X
7			X						
8						2	2		
9					2			2	

After zapping of surrounding sudoku by first member, showing zapped area in dark. Forced choice of second member in box C. (Note that this action also reveals last member of subpattern-2 in box D.)

continued on next page

Pictorial demonstration of example 1 001, continued.

Continuation of pictorial view of zapping by subpattern-2.

	1	2	3	4	5	6	7	8	9
1		2						2	
2	2						2		
3				X					
4		2			2				
5	2					2			
6									X
7			X						
8						2	2		
9					2			2	

After zapping by second member of subpattern-2, the third choice in box I reveals forced choice of subpattern-2.

	1	2	3	4	5	6	7	8	9
1		2						2	
2	2						2		
3				X					
4		2			2				
5	2					2			
6									X
7			X						
8						2	2		
9					2			2	

After zapping by third member, fourth member is revealed, again a forced choice.

	1	2	3	4	5	6	7	8	9
1		2						2	
2	2						2		
3				X					
4		2			2				
5	2					2			
6									X
7			X						
8						2	2		
9					2			2	

After zapping by fourth member of subpattern-2, the fifth choice in box D is forced.

	1	2	3	4	5	6	7	8	9
1		2						2	
2	2						2		
3				X					
4		2			2				
5	2					2			
6									X
7			X						
8						2	2		
9					2			2	

Finally, after zapping by fifth member, sixth member in box C is forced. The subpattern is finished, but if we zapped what remained by the last member, the only squares not zapped would be the X's, revealing the positions of the established 2's.

Pattern Code	Box Orientation	Patterns with the same box code
2 - 2 - 2 2 - 2	D - F - E A - C	023, 030

A		C
D	E	F

The box order below is chosen so as to simplify the determination of subpattern-1. If we chose a counterclockwise order starting at box A, we would have to go from box F to D and then to E, instead of going directly from F to E to D.

Subpattern-1 begins in **(22)** with box order **A→D→E→F→C**

(22) zaps (52) adding **(61)** zaps (66) adding **(46)**

(46) zaps (49) adding **(57)** zaps (27) adding **(39)**

Subpattern-1 = **(22),(61),(46),(57),(39)**

A D E F C

1	008	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					X					
row2		1 ₁					1			
row3	1									1 ₁
row4						1 ₁				1
row5		1					1 ₁			
row6	1 ₁					1				
row7			X							
row8				X						
row9								X		

Example 1.008, continued.

A		C
D	E	F

Back at the starting box, there is no pending condition, so we begin subpattern-2 in (31), the only remaining square in box A. Looking ahead, we see a problem in progressing from box E to box F, so we change the box order and choose a counterclockwise route, going from **A to C to F to E to D**.

Subpattern-2 begins in **(31)** with box order **A→C→F→E→D**

(31) zaps (39) adding **(27)** zaps (57) adding **(49)** zaps (46) adding **(66)**
(66) zaps (61) adding **(52)**

Subpattern-2 = **(31),(27),(49),(66),(52)**
A C F E D

Back at the starting box A, nothing is pending and no squares are un-claimed, so the pattern analysis is complete.

1	008	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					X					
row2		1 ₁					1 ₂			
row3	1 ₂								1 ₁	
row4						1 ₁			1 ₂	
row5		1 ₂					1 ₁			
row6	1 ₁					1 ₂				
row7			X							
row8				X						
row9								X		

Pattern Code	Box Orientation	Patterns with the same box code
2 2-2-2 2-2	B G-I-H D-F	none
(box orientation for 038 – interchange columns 2 & 3, then interchange rows 2 & 3)		

	B	
D		F
G	H	I

Subpattern-1 begins in (35) with box order **B→H→G→I→F→D**

(35) zaps (95) adding (86) zaps (83) adding (72) zaps (78) adding (97)
(97) zaps (57) adding (48) zaps (42) adding (53)

Subpattern-1 = (35),(86),(72),(97),(48),(53)
B H G I F D

1	038	B3	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	X										
row2											X
row3					3 ₁	3					
row4		3							3 ₁		
row5			3 ₁					3			
row6				X							
row7		3 ₁							3		
row8			3			3 ₁					
row9					3		3 ₁				

Pattern 1,038 continued.

	B	
D		F
G	H	I

Subpattern-2 begins in **(36)** with box order **B→H→I→G→D→F**.

(36) zaps (86) adding **(95)** zaps (97) adding **(78)** zaps (72) adding **(83)**
(83) zaps (53) adding **(42)** zaps (48) adding **(57)**

Subpattern-2 = **(36),(95),(78),(57),(42),(57)**
B H I G D F

Back at the starting box B, there are no unclaimed squares nor pending situations. We are done.

1	038	B3	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
			row1	X							
			row2								X
			row3					3 ₁	3 ₂		
			row4		3 ₂					3 ₁	
			row5			3 ₁				3 ₂	
			row6				X				
			row7		3 ₁					3 ₂	
			row8			3 ₂			3 ₁		
			row9					3 ₂		3 ₁	

Pattern Code	Box Orientation	Patterns with the same box code
3 – 2	B – C	none
2 – 2	E – F	

	B	C
	E	F

Box order: **B(→C)→E→F**

Subpattern-1 begins in **(14)** zaps (17) adding **(37)**
(14) zaps (44) adding **(55)** zaps (59) adding **(49)**

Subpattern-1 = **(14),(37),(55),(49)**
B C E F

Subpattern-2 begins in **(15)** zaps (17) adding **(37)**
(15) zaps (55) adding **(44)** zaps (49) adding **(59)**

Subpattern-2 = **(15),(37),(44),(59)**
B C E F

1 037 C0 col 1 col 2 col 3 col 4 col 5 col 6 col 7 col 8 col 9

row1				7 ₁	7 ₂		7		
row2		X							
row3				7			7 ₁₂		
row4				7 ₂					7 ₁
row5					7 ₁				7 ₂
row6			X						
row7						X			
row8	X								
row9								X	

Pattern 1.037, continued.

	B	C
	E	F

Box order: **B(→C)→E→F**

Subpattern-3 begins in **(34)** zaps (37) adding **(17)**
(34) zaps (44) adding **(55)** zaps (59) adding **(49)**

Subpattern-3 = **(34),(17),(55),(49)**
B C E F

Back at the starting box, there are no unclaimed squares and nothing pending, so the pattern analysis is complete.

1	037	C0	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row1				7 ₁	7 ₂		7 ₃		
		row2		X							
		row3				7 ₃			7 ₁₂		
		row4				7 ₂					7 ₁₃
		row5					7 ₁₃				7 ₂
		row6			X						
		row7						X			
		row8	X								
		row9								X	

Pattern Code	Box Orientation	Patterns with the same box code
$ \begin{array}{c} 2 \\ \\ 3-3-2 \\ \quad \\ 2-2 \end{array} $	$ \begin{array}{c} G2 \\ \\ C3-B3-A2 \\ \quad \\ E2-F2 \end{array} $	none
(box orientation for 027: swap rows 1 & 3, then columns 1 & 3)		

A	B	C
	E	F
G		

Subpattern-1 begins in (14) with box order **B→E→F→C→A→G**

(14) zaps (64) adding (55) zaps (58) adding (67) zaps (37) & (17) adding (28)

(28) zaps (21) adding (33) zaps (73) adding (71)

Subpattern-1 = (14),(55),(67),(28),(33),(71)

B E F C A G

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
1 027									
row1				2 ₁			2		
row2	2				2			2 ₁	
row3			2 ₁	2			2		
row4		X							
row5					2 ₁			2	
row6				2			2 ₁		
row7	2 ₁		2						
row8						X			
row9									X

Example 1.027, continued.

A	B	C
D	E	F
G	H	I

Subpattern-2 begins in (25) with box order $B \rightarrow A \rightarrow G \rightarrow C \rightarrow F \rightarrow E$.

(25) zaps (21) adding (33) zaps (73) adding (71)

(25) zaps (55) adding (64) zaps (67) adding (58)

(58) zaps (28) while (33) zaps (37) adding (17)

Subpattern-2 = (25),(33),(71),(64),(58),(17)

B A G C F E

Subpattern-3 begins in (34) with box order $B \rightarrow E \rightarrow F \rightarrow C \rightarrow A \rightarrow G$

(34) zaps (64) adding (55) zaps (58) adding (67) zaps (37) & (17) adding (28)

(34) zaps (33) adding (21)

But now, there are two members of subpattern-3 in the same row, namely squares (28) and (21). Every action was forced, except for the choice of (34). This means that (34) cannot be the start of any subpattern, and we must remove all the 3 subscripts from the other squares in the aborted subpattern-3. The result of all these actions is that there is no pending situation, and no *claimable* unclaimed squares remaining in the starting box B. Therefore we are done! On the next page, we'll consider the meaning of all this.

1	027	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				2 ₁			2 ₂			
row2	2 ₃				2 ₂			2 ₁₃		
row3			2 ₁₂	2 ₃			2			
row4		X								
row5					2 ₁₃			2 ₂		
row6				2 ₂			2 ₁₃			
row7	2 ₁₂		2							
row8						X				
row9										X

Pattern 1.027, continued.

We first attach the killer subscript to the 2's not included in either of the subpatterns. And what meaning can we give to the two 2's with both subscripts 1 and 2? Clearly, there are not three subpatterns, so the 2's in squares (33) and (71) must be established 2's, and should be replaced by large X's. See the treatment of killers in the introduction .

1 027

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				2 ₁			2 ₂		
row2	2 _K				2 ₂			2 ₁	
row3			2 ₁₂	2 _K			2 _K		
row4		X							
row5					2 ₁			2 ₂	
row6				2 ₂			2 ₁		
row7	2 ₁₂		2 _K						
row8						X			
row9									X

1 027

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				2 ₁			2 ₂		
row2	2 _K				2 ₂			2 ₁	
row3			X	2 _K			2 _K		
row4		X							
row5					2 ₁			2 ₂	
row6				2 ₂			2 ₁		
row7	X		2 _K						
row8						X			
row9									X

Pattern Code	Box Orientation	Patterns with same box code
<pre> 3-----3 2-2 2-2 </pre>	<pre> B-----C E-D G---I </pre>	none
(box orientation for 004: swap columns 1 & 2)		

	B	C
D	E	
G		I

Box order B→E→D→G→I→C

Note the importance of a good box order for a particular beginning square. If we had begun in square (15) of box B and progressed to box C, we would have encountered a false pending situation.

Subpattern-1 begins in **(15)** zaps (65) adding **(54)** zaps (55) adding **(62)** zaps (72) adding **(83)** zaps (87) & (89) adding **(77)** zaps (27) & (17) adding **(29)**

Subpattern-1 = **(15),(54),(62),(83),(77),(29)**

B E D G I C

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
1 004									
row1					3 ₁		3		
row2				3			3		3 ₁
row3	X								
row4								X	
row5			3	3 ₁					
row6		3 ₁			3				
row7		3					3 ₁		
row8			3 ₁				3		3
row9						X			

Pattern 1.004, continued.

	B	C
D	E	
G		I

Subpattern-2 begins in **(24)** with box order **B→C→I→G→D→E**

(24) zaps (27) & (29) adding **(17)** zaps (77) & (87) adding **(89)**

(89) zaps (83) adding **(72)** zaps (62) adding **(53)** zaps (54) adding **(65)**

Subpattern-2 = **(24),(17),(89),(72),(53),(65)**

B C I G D E

Back at the starting box B, nothing is pending, and no square is unclaimed in the starting box. The pattern analysis is complete, but what about the two unclaimed squares (27) and (87)? They must be killers. See the next page for further information.

1 004

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					3 ₁		3 ₂		
row2				3 ₂			3		3 ₁
row3	X								
row4								X	
row5			3 ₂	3 ₁					
row6		3 ₁			3 ₂				
row7		3 ₂					3 ₁		
row8			3 ₁				3		3 ₂
row9						X			

Pattern 1.004, continued.

	B	C
D	E	
G		I

This is the sudoku after completion of the two subpatterns: What about the two unsubscripted 3's in squares (27) and (87)? They are killers, candidates which do not have viable continuations to become subpatterns. One way to test them is by seeing what would happen if they were promoted to established 3's. See the introduction for an example of such testing.

1	004	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					3 ₁		3 ₂			
row2				3 ₂			3 _K		3 ₁	
row3	X									
row4								X		
row5			3 ₂	3 ₁						
row6		3 ₁			3 ₂					
row7		3 ₂					3 ₁			
row8			3 ₁				3 _K		3 ₂	
row9						X				

Pattern Code	Box Orientation	Patterns with the same box code
$ \begin{array}{c} 3 \text{-----} 2 \\ \qquad \quad \\ 2 - 3 \quad \\ \qquad \quad \\ 3 - 2 \end{array} $	$ \begin{array}{c} A3 \text{-----} B2 \\ \qquad \quad \\ D2 - F3 \\ \qquad \quad \\ I3 - H2 \end{array} $	none (box orientation for 014: swap columns 2 & 3)

A	B	
D		F
	H	I

A→D→F→I→H→B

Subpattern-1 starts in **(21)** zaps (51) adding **(42)** zaps (47) & (48) adding **(57)** **(57)** zaps (87) & (97) adding **(98)** zaps (95) adding **(86)** zaps (26) adding **(35)**

Subpattern-1 = **(21),(42),(57),(98),(86),(35)**

A D F I H B

1	014	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1										X
row2	5 ₁					5				
row3	5	5			5 ₁					
row4		5 ₁					5	5		
row5	5						5 ₁			
row6				X						
row7			X							
row8						5 ₁	5			
row9					5		5	5 ₁		

Pattern 1.014, continued.

A	B	
D		F
	H	I

A→D→F→I→H→B

Subpattern-2 begins in **(31)** zaps **(51)** adding **(42)** zaps **(47)** & **(48)** adding **(57)**
(57) zaps **(87)** & **(97)** adding **(98)** zaps **(95)** adding **(86)** zaps **(26)** adding **(35)**
 Subpattern-2 = **(31),(42),(57),(98),(86),(35)**

But there are two members of the same subpattern-2 in row 3, **(31)** & **(35)**, based on the choice of square (31) as the beginning of subpattern-2. Moreover, every choice in the development of subpattern-2 is forced, based only on the choice of (31). Therefore the choice of (31) as the beginning of a subpattern leads to a contradiction. Therefore square (31) cannot be a member of a subpattern, so it must be a killer. We backtrack through all the squares of subpattern-2, removing the subscript 2 from all of them, until we get back to square (31), where, after we remove the subscript 2, we place the subscript K, for killer. On the next page, we'll begin a new subpattern-2 in a different square of box A.

1	014	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1										X
row2	5 ₁					5				
row3	5 ₂	5			5 ₁₂					
row4		5 ₁₂					5	5		
row5	5						5 ₁₂			
row6				X						
row7			X							
row8						5 ₁₂	5			
row9					5		5	5 ₁₂		

Pattern 1.014, continued.

A	B	
D		F
	H	I

A→D→F→I→H→B

This time we choose square (32) as the beginning square of subpattern-2. This choice is forced, as there is no other.

(32) zaps (42) adding (51) zaps (57) adding (47) and pending (48)

(47) zaps (87) & (97) adding (98) zaps (95) adding (86) zaps (96) adding (35)

But then there are two squares in subpattern-2 – (32) and (35), and the choice back in the pending box F which led to this was square (57). We must backtrack to this point in the development of subpattern-2 and make the choice in the pending square instead. We'll accomplish this on the next page.

1	014	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1										X
row2	5 ₁					5				
row3	5 _K	5 ₂			5 ₁₂					
row4		5 ₁					5 ₂	5 _p		
row5	5 ₂						5 ₁			
row6				X						P
row7			X							
row8						5 ₁₂	5			
row9					5		5	5 ₁₂		

Pattern 1.014, continued.

A	B	
D		F
	H	I

A→D→F→I→H→B

After backtracking subpattern-2 back to the pending box F, we remove the pending P and choose the pending square (48) as the extension of subpattern-2.

(48) zaps ((98) adding (97) and pending (87)
(97) zaps (95) adding (86) zaps (26) adding (35)

But now there are two members of subpattern-2 in the same row 3 – namely (32) and (35). The source of this contradiction goes back to the choice of pending square (87), so we must backtrack to the pending box I, cancel the choice of (97) for subpattern-2, and choose the pending square instead. We'll accomplish this on the next page.

1	014	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1										X
row2	5 ₁					5				
row3	5 _K	5 ₂			5 ₁₂					
row4		5 ₁					5	5 ₂		
row5	5 ₂							5 ₁		
row6				X						
row7			X							P
row8						5 ₁₂	5 _p			
row9					5		5 ₂	5 ₁		

Pattern 1.014, continued.

A	B	
D		F
	H	I

A→D→F→I→H→B

Backtracking back to the pending box B, we remove the pending P and assign subpattern-2 to the pending square (87) instead.

(87) zaps (86) adding (95) zaps (35) adding (26)

Back at the starting box A, there are no unclaimed squares and no pending condition. Therefore we are done. There are still two unclaimed squares, (47) and (97), which must both be killers, and we must subscript them as such.

1	014	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1									X
	row2	5 ₁					5 ₂			
	row3	5 _K	5 ₂			5 ₁				
	row4		5 ₁					5 _K	5 ₂	
	row5	5 ₂						5 ₁		
	row6				X					
	row7			X						
	row8						5 ₁	5 ₂		
	row9					5 ₂		5 _K	5 ₁	

Pattern Code	Box Orientation	Patterns with the same box code
<pre> 3-----3 2-2 3 2 </pre>	<pre> C3-----B2 F3-D2 G2-H3 </pre>	none
(box orientation for 018: interchange columns 2 & 3, then columns 1 & 2)		

	B	C
D		F
G	H	

B→C→F→D→G→H for subpattern-1

B→H→G→D→F→C for subpattern-2

Using B as the starting box, and these two box orders, we can avoid all pending boxes.

Subpattern-1 begins in **(24)** with box order **B→C→F→D→G→H**

(24) zaps **(27)** & **(29)** adding **(17)** zaps **(57)** & **(67)** adding **(59)** zaps **(53)** adding **(61)**
(61) zaps **(71)** adding **(93)** zaps **(94)** & **(95)** adding **(75)**

Subpattern-1 = **(24),(17),(59),(61),(93),(75)**

B C F D G H

1 018 col 1 col 2 col 3 col 4 col 5 col 6 col 7 col 8 col 9

row1				8		8 ₁		
row2			8 ₁			8		8
row3	X							
row4					X			
row5		8				8		8 ₁
row6	8 ₁					8		
row7	8			8 ₁				
row8							X	
row9		8 ₁	8	8				

Pattern 1.018, continued.

	B	C
D		F
G	H	

Subpattern-2 begins in **(15)** with box order **B→H→G→D→F→C**

(15) zaps (75) & (95) adding **(94)** zaps (93) adding **(71)** zaps (61) adding **(53)**
(53) zaps (57) & (59) adding **(67)** zaps (27) & (17) adding **(29)**

Subpattern-2 = **(15),(94),(71),(53),(67),(29)**
B H G D F C

Back at the starting box B, there are no unclaimed squares in the starting box, and no pending conditions anywhere, so we are done. The unclaimed squares (27), (57), and (95) must all be killers, and we shall assign them all the subscript K.

1	018	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1					8 ₂		8 ₁		
	row2				8 ₁			8 _K		8 ₂
	row3		X							
	row4						X			
	row5			8 ₂				8 _K		8 ₁
	row6	8 ₁						8 ₂		
	row7	8 ₂				8 ₁				
	row8								X	
	row9			8 ₁	8 ₂	8 _K				

Chapter 2. Patterns with 2 subscripts.

Pattern 2.023 L	Box Orientation	Patterns with the same box code
3 – 2	E – D	023, 038, 047, 048, 056, 066, 068, 091,
		092, 093, 094, 096, 103, 105, 126, 145.
2	H	
(box orientation for 023 – interchange stacks 1 & 2)		

D	E	
	H	

Order of boxes: E→D→H

Subpattern-1 begins in (44) zaps (43) adding (53)
(44) zaps (94) adding (95)

Subpattern-1: (44),(53),(95)
E D H

2	023	A1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row1	X								
		row2								X	
		row3						X			
		row4			3	3 ₁	3				
		row5			3 ₁	3					
		row6									X
		row7							X		
		row8		X							
		row9				3	3 ₁				

Pattern 2.023, continued.

D	E	
	H	

Order of boxes: E→D→H

Subpattern-2 begins in (45) zaps (43) adding (53)
(45) zaps (95) adding (94)

Subpattern-2: (45),(53),(94)
E D H

2	023	A1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row1	X								
		row2								X	
		row3						X			
		row4			3	3 ₁	3 ₂				
		row5			3 ₁₂	3					
		row6									X
		row7							X		
		row8		X							
		row9				3 ₂	3 ₁				

Pattern 2.023, continued.

D	E	
	H	

Order of boxes: E→D→H

Subpattern-3 begins in (54) zaps (53) adding (43)
(54) zaps (94) adding (95)

Subpattern-3: (54),(43),(95)
E D H

Back at the starting box, nothing is pending and no squares are unclaimed. Done.

2	023	A1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row1	X								
		row2								X	
		row3						X			
		row4			3 ₃	3 ₁	3 ₂				
		row5			3 ₁₂	3 ₃					
		row6									X
		row7							X		
		row8		X							
		row9				3 ₂	3 ₁₃				

Pattern 2.030	Box Orientation	Patterns with the same box code
3 – 2 – 2	A – D – G	102

A		
D		
G		

Box order:A→D→G

Subpattern-1 begins in (31) zaps (41) adding (42)
(31) zaps (81) adding (83)

Subpattern-1: (31),(42),(83)
A D G

Subpattern-2 begins in (32) zaps (42) adding (41) zaps (81) adding (83)

Subpattern-2: (32),(41),(83)
A D G

2	030	A3	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					X						
row2								X			
row3	3 ₁	3 ₂	3								
row4	3 ₂	3 ₁									
row5									X		
row6					X						
row7						X					
row8	3		3 ₁₂								
row9											

Pattern 2.030, continued.

A		
D		
G		

Box order:A→D→G

Subpattern-3 begins in (33) zaps (83) adding (81) zaps (41) adding (42)

Subpattern-3: (33),(81),(42)
A G D

Back at the starting box A, nothing is pending and no squares are unclaimed. The analysis is complete.

2	030	A3	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
						X					
row1											
									X		
row2											
row3											
row4											
row5										X	
row6											
row7											
row8											
row9											

Pattern 2.110	Box Orientation	Patterns with the same box code
3 – 2 – 2	H – I – G	113, 114.
2	E	
(box orientation for 110: switch bands 1 & 3, then stacks 1 & 2, then stacks 2 & 3)		

	E	
G	H	I

Box order: H→E→G→I

Subpattern-1 begins in (84) zaps (64) adding (65)
(84) zaps (82) adding (92) zaps (98) adding (78)

Subpattern-1: (84),(65),(92),(78)
H E G I

2	110	A4	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
									X		
			X								
							X				
											X
					X						
						4	4 ₁				
							4			4 ₁	
				4		4 ₁	4				
				4 ₁						4	

Pattern 2.110, continued.

	E	
G	H	I

Subpattern-2 begins in (75) with box order **H→E→I→G**

(75) zaps (65) adding (64)
(75) zaps (78) adding (98) zaps (92) adding (62)

Subpattern-2 = (75),(64),(98),(62)
 H E I G

2	110	A4	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row1							X		
		row2	X								
		row3						X			
		row4									X
		row5			X						
		row6				4 ₂	4 ₁				
		row7					4 ₂			4 ₂	
		row8		4 ₂		4 ₁	4				
		row9		4 ₁						4 ₂	

Pattern 2.110, continued.

	E	
G	H	I

Subpattern-3 is begun in **(85)** with box order **H→E→G→I**

(85) zaps (65) adding **(64)**
(85) zaps (82) adding **(92)** zaps (98) adding **(78)**

Subpattern-3 = **(85),(64),(92),(78)**
 H E G I

Back at the starting box H, nothing is pending, no squares are unclaimed, so the analysis is complete.

2	110	A4s	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
									X		
			X								
								X			
											X
					X						
						4 ₂₃	4 ₁				
							4 ₂			4 ₁₃	
				4 ₂		4 ₁	4 ₃				
				4 ₁₃						4 ₂	

Pattern 2.039 L	Box Orientation	Patterns with the same box code
3 – 2 – 2	A – D – G	051, 070, 072, 079, 095, 107, 110, 120, 123.
2	C	
(box orientation for 039: rotate sudoku 90 degrees counterclockwise, then swap bands 2 & 3, then swap bands 1 & 2)		

A		C
D		
G		

Subpattern-1 will begin in **(11)** with box order **A→C→G→D**

(11) zaps (19) adding **(39)**

(11) zaps (91) adding **(93)** zaps (53) adding **(52)**

Subpattern-1 = **(11),(39),(93),(52)**

A C G D

2

039

A4

L

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1	7 ₁		7						7
row2					X				
row3		7							7 ₁
row4							X		
row5		7 ₁	7						
row6				X					
row7						X			
row8								X	
row9	7		7 ₁						

Pattern 2.039, continued.

A		C
D		
G		

Subpattern-2 will begin in (13) with box order A→C→D→G

(13) zaps (19) adding (39)

(13) zaps (53) adding (52)

(13) zaps (93) adding (91)

Subpattern-2 = (13),(39),(52),(91)

A C D G

2	039	A4	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		L									
		row1	7 ₁		7 ₂						7
		row2					X				
		row3		7							7 ₁₂
		row4							X		
		row5		7 ₁₂	7						
		row6				X					
		row7						X			
		row8								X	
		row9	7 ₂		7 ₁						

Pattern 2.039, continued.

A		C
D		
G		

Subpattern-3 will begin in (32) with box order A→C→D→G

(32) zaps (39) adding (19)
(32) zaps (52) adding (53) zaps (93) adding (91)

Subpattern-3 = (32),(19),((53),(91)

Back at the starting box A, nothing is pending, no squares remain unclaimed, so the pattern analysis is complete.

2039

A4
L

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1	7 ₁		7 ₂						7 ₃
row2					X				
row3		7 ₃							7 ₁₂
row4							X		
row5		7 ₁₂	7 ₃						
row6				X					
row7						X			
row8							X		
row9	7 ₂₃		7 ₁						

Pattern 2.104
3-2-2
|
2

Box Orientation
D-A-G
|
C

Patterns with the same box code
none

(box orientation for 039: rotate sudoku 90 degrees clockwise, then swap stacks 1 & 2, then swap stacks 2 & 3, then swap bands 2 & 3)

A		C
D		
G		

Box order: D→G→A→C

Subpattern-1 begins in (52) zaps (82) adding (81)
(52) zaps (22) adding (13) zaps (19) adding (29)

Subpattern-1 = (52),(81),(13),(29)

2104A6X

col 1col 2col 3col 4col 5col 6col 7col 8col 9

row1			9 ₁						9
row2		9							9 ₁
row3						X			
row4				X					
row5	9	9 ₁	9						
row6								X	
row7					X				
row8	9 ₁	9							
row9							X		

Pattern 2.104, continued.

A		C
D		
G		

Subpattern-2 starts in (51) with box order **D→G→A→C**

(51) zaps (81) adding (82) zaps (22) adding (13)
(13) zaps (19) adding (29)

Subpattern-2 = (51),(82),(13),(29)
D G A C

Subpattern-3 starts in (53) with box order **D→A→G→C**

(53) zaps (13) adding (22) zaps (82) adding (81)
(22) zaps (29) adding (19)

Subpattern-3 = (53),(22),(81),(19)
D A G C

Back at the starting box, nothing is pending, no boxes unclaimed, Done.

2104A6X

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			9 ₁₂						9 ₃
row2		9 ₃							9 ₁₂
row3						X			
row4				X					
row5	9 ₂	9 ₁	9 ₃						
row6								X	
row7					X				
row8	9 ₁₃	9 ₂							
row9							X		

Pattern 2.097 L	Box Orientation	Patterns with the same box code
3 - 2 - 2	F - E - D	none
2 - 2	H - I	
(box orientation for 097: swap bands 1 & 2, then stacks 1 & 3)		

D	E	F
	H	I

We'll omit boxes A, B & C from the calculations, since they have no candidates, and restrict our calculations to boxes D, E and F, then use derivative squares to complete boxes H and I.

row1								X
row2				X				
row3		X						

2	097	A5	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		L			2	2			2		
						2				2	
				2					2		

row7						2 _C	2 _A		
row8	X								
row9						2 _D		2 _B	

Pattern 2.097, continued.

D	E	F
---	---	---

Subpattern-1 begins in (67) with box order **F→D→E**

(67) zaps (63) adding (43) zaps (44) adding (54)

Subpattern-1 = (67),(43),(54)
F D E

Subpattern-2 begins in (58) with box order **F→E→D**

(58) zaps (54) adding (44) zaps (45) adding (54)

Subpattern-2 = (58),(44),(54)
F E D

Subpattern-3 begins in (47) with box order **F→E→D**

(47) zaps (44) adding (54)

(47) zaps (43) adding (63)

Subpattern-3 = (47),(54),(63)
F E D

Back at the starting box F, nothing is pending, no square unclaimed. Done.

2

097

A5

L

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row4

row5

row6

		2 ₁	2 ₂			2 ₃		
			2 ₁₃				2 ₂	
		2 ₂₃				2 ₁		

A and 3 and 1 = 123, so **A = 2** C and A add up to 123, so **C = 13**
A and B = 123, so **B = 13** C and D add up to 123, so **D = 2**

row7						2 _C	2 _A		
row8	X								
row9						2 _D		2 _B	

Pattern 2.097, continued.

D	E	F
	H	I

Putting the three bands back together, we have the final solution:

2

097

A5
L

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2					X				
row3		X							
row4			2 ₁	2 ₂			2 ₃		
row5				2 ₁₃				2 ₂	
row6			2 ₂₃				2 ₁		
row7						2 ₁₃	2 ₂		
row8	X								
row9						2 ₂		2 ₁₃	

Pattern 2.002	Box Orientation	Patterns with the same box code
$ \begin{array}{c} 2 \\ \\ 3-2 \\ \\ 2 \end{array} $	$ \begin{array}{c} F \\ \\ B-C \\ \\ H \end{array} $	003, 006, 010, 011, 050, 078, 080, 089, 098, 099, 103, 106, 115, 118, 122, 124, 152, 154.
(box orientation for 002: swap stacks 1 & 2, then 2 & 3, then swap bands 1 & 2.)		

	B	C
		F
	H	

Box order: B→H→C→F

Subpattern-1 begins in (24) zaps (94) adding (95)
(24) zaps (27) adding (38) zaps (68) adding (67)

Subpattern-1 = (24),(95),(38),(67)
B H C F

Subpattern-2 begins in (34) zaps (94) adding (95)
(34) zaps (38) adding (27) zaps (67) adding (68)

Subpattern-2 = (34),(95),(27),(68)
B H C F

2	002	D	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
					X						
						1 ₁			1 ₂		
					1 ₂	1				1 ₁	
									1 ₁	1 ₂	
						1	1 ₁₂				

Pattern 2.002, continued.

	B	C
		F
	H	

Box order: B→H→C→F

Subpattern-3 begins in (35) zaps (95) adding (94)
(35) zaps (38) adding (27) zaps (67) adding (68)

Subpattern-3 = (35),(94),(27),(68)
 B H C F

Back at the starting box B, nothing is pending and no boxes are unclaimed. The pattern is complete.

2	002	D	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
					X						
row1											
						1 ₁			1 ₂₃		
row2											
						1 ₂	1 ₃			1 ₁	
row3											
row4											
row5											
row6									1 ₁	1 ₂₃	
row7											
row8											
row9						1 ₃	1 ₁₂				

Pattern 2.004	Box Orientation	Patterns with the same box code 026, 073, 111, 119, 146.
2 3-2 2-2	C E-F G-H	

		C
	E	F
G	H	

Box order: E→F→C→H→G

Subpattern-1 begins in (45) zaps (47) adding (58) zaps (18) adding (17)
(45) zaps (85) adding (76) zaps (71) adding (61)

Subpattern-1 = (45),(58),(17),(76),(61)
E F C H G

Subpattern-2 begins in (55) zaps (58) adding (47) zaps (17) adding (18)
(55) zaps (85) adding (76) zaps (71) adding (81)

Subpattern-2 = (55),(47),(18),(76),(81)
E F C H G

2	004	E	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									9 ₁	9 ₂	
row2				X							
row3			X								
row4					9 ₁			9 ₂			
row5					9 ₂	9			9 ₁		
row6		X									
row7	9						9 ₁₂				
row8	9 ₁₂				9						
row9											X

Pattern 2.004, continued.

		C
	E	F
G	H	

Box order: E→F→C→H→G

Subpattern-3 begins in (56) zaps (58) adding (47) zaps (17) adding (18)
(56) zaps (76) adding (85) zaps (81) adding (71)

Subpattern-3 = (56),(47),(18),(85),(71)
 E F C H G

Back at the starting box E, nothing is pending and no squares are unclaimed. The pattern analysis is complete.

2 004 E		col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1								9 ₁	9 ₂₃	
row2				X						
row3			X							
row4					9 ₁		9 ₂₃			
row5					9 ₂	9 ₃		9 ₁		
row6		X								
row7	9 ₃					9 ₁₂				
row8	9 ₁₂				9 ₃					
row9									X	

Pattern 2.008	Box Orientation	Patterns with the same box code
$ \begin{array}{c} 2-2 \\ \\ 3-2 \\ \\ 2 \end{array} $	$ \begin{array}{c} I-C \\ \\ B-H \\ \\ A \end{array} $	044, 071, 117, 151.

A	B	C
	H	I

Box order: B→A→H→I→C

Subpattern-1 begins in **(15)** zaps (11) adding **(21)**

(15) zaps (95) adding **(86)** zaps (88) adding **(99)** zaps (39) adding **(38)**

Subpattern-1 = **(15),(21),(86),(99),(38)**

B A H I C

Subpattern-2 begins in **(16)** zaps (11) adding **(21)**

(16) zaps (86) adding **(95)** zaps (99) adding **(88)** zaps 938) adding **(39)**

Subpattern-2 = **(16),(21),(95),(88),(39)**

B A H I C

2	008	F	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	5				5 ₁	5 ₂					
row2	5 ₁₂					5					
row3									5 ₁	5 ₂	
row4											
row5		X							X		
row6				X							
row7			X								
row8						5 ₁			5 ₂		
row9					5 ₂					5 ₁	

Pattern 2.008

A	B	C
	H	I

Box order: B→A→H→I→C

Subpattern-3 begins in (26) zaps (21) adding (11)
(26) zaps (86) adding (95) zaps (99) adding (88) zaps (38) adding (39)

Subpattern-3 = (26),(11),(95),(88),(39)
 B A H I C

Back at the starting box, nothing is pending and no squares
are unclaimed. The pattern analysis is complete.

2

008

F

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	5 ₃				5 ₁	5 ₂			
row2	5 ₁₂					5 ₃			
row3								5 ₁	5 ₂₃
row4									
row5		X					X		
row6				X					
row7			X						
row8						5 ₁		5 ₂₃	
row9					5 ₂₃				5 ₁

Pattern 2.007	Box Orientation	Patterns with the same box code
3 - 2 - 2 L	G - I - H	015, 017, 019, 021, 027, 029, 031, 046, 049,
		059, 062, 063, 067, 074, 075, 077, 082, 083,
2 - 2	D - F	088, 108, 150.

D		F
G	H	I

Box order: G→H→I→F→D

Subpattern-1 begins in (72) zaps (76) adding (96)

(72) zaps (78) adding (87) zaps (47) adding (58) zaps (52) adding (41)

Subpattern-1 = (72),(96),(87),(58),(41)

G H I F D

Subpattern-2 begins in (92) zaps (96) adding (76) zaps (78) adding (87)

(87) zaps (47) adding (58) zaps (52) adding (41)

Subpattern-2 = (92),(76),(87),(58),(41)

G H I F D

2	007	G2	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		L			X						
		row1			X						
		row2									X
		row3				X					
		row4	6 ₁₂						6		
		row5		6						6 ₁₂	
		row6					X				
		row7		6 ₁				6 ₂		6	
		row8	6						6 ₁₂		
		row9		6 ₂				6 ₁			

Pattern 2.007, continued.

D		F
G	H	I

Box order changed to: **G→I→H→F→D**

Subpattern-3 begins in **(81)** zaps (87) adding **(78)** zaps (76) adding **(96)**
(78) zaps (58) adding **(47)** zaps (41) adding **(52)**

Subpattern-3 = **(81),(78),(96),(47),(52)**
G I H F D

Back at the starting box, nothing is pending, and no boxes are unclaimed.
The pattern analysis is complete.

2	007	G2	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		L									
		row1			X						
		row2									X
		row3				X					
		row4	6 ₁₂						6 ₃		
		row5		6 ₃						6 ₁₂	
		row6					X				
		row7		6 ₁				6 ₂		6 ₃	
		row8	6 ₃						6 ₁₂		
		row9		6 ₂				6 ₁₃			

Pattern 2.036	Box Orientation	Patterns with the same box code
3 - 2 - 2	G - H - I	none
2 - 2	D - E	
2	A	(box orientation for 036: swap bands 1 & 3)

A		
D	E	
G	H	I

Box order: G→D→A→E→H→I

Subpattern-1 is begun in (71) zaps (61) adding (52) zaps (12) adding (13)
(52) zaps (54) adding (65) zaps (85) adding (94)
(71) zaps (79) adding (89)

Subpattern-1 = (71),(52),(13),(65),(94),(89)
G D A E H I

Subpattern-2 is begun in (81) zaps (61) adding (52) zaps (12) adding (13)
(52) zaps (54) adding (65) zaps (85) adding (94)
(81) zaps (89) adding (79)

Subpattern-2 = (81),(52),(13),(65)(94),(79)
G D A E H I

G4		col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
2	036	L								
row1		9	9 ₁₂							
row2						X				
row3							X			
row4								X		
row5		9 ₁₂		9						
row6	9				9 ₁₂					
row7	9 ₁								9 ₂	
row8	9 ₂				9				9 ₁	
row9			9	9 ₁₂						

Example 2.036, continued.

A		
D	E	
G	H	I

New box order:G→A→D→E→H→I.

Subpattern-3 begins in (93) zaps (13) adding (12) zaps (52) adding (61) (61) zaps (65) adding (54) zaps (94) adding (85) zaps (89) adding (79)

Subpattern-3 = (93),(12),(61),(54),(85),(79)

Back at the starting box G, nothing is pending and no boxes are unclaimed, so we are done.

2

036

G4

L

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		9 ₃	9 ₁₂						
row2						X			
row3							X		
row4								X	
row5		9 ₁₂		9 ₃					
row6	9 ₃				9 ₁₂				
row7	9 ₁								9 ₂₃
row8	9 ₂				9 ₃				9 ₁
row9			9 ₃	9 ₁₂					

Pattern 2.045	Box Orientation	Patterns with the same box code
3---2 2 - 2 - 2 2	C---I B - H - E A	none (Box orientation for 045 – rotate 90 degrees counterclockwise, then swap stacks 2 & 3)

A	B	C
	E	
	H	I

Subpattern-1 begins in **(18)** with box order **C→A→B→E→G→H**

(18) zaps (12) adding **(32)** zaps (35) adding **(24)** zaps (44) adding **(46)**
(46) zaps (86) adding **(75)** zaps (78) adding **(89)**

Subpattern-1 = **(18),(32),(24),(46),(75),(89)**
C A B E G H

Subpattern-2 begins in **(29)** with box order **C→B→A→G→E→H**

(29) zaps (24) adding **(35)** zaps (32) adding **(12)**
(35) zaps (75) adding **(86)** zaps (46) adding **(44)**
(86) zaps (89) adding **(78)**

Subpattern-2 = **(29),(35),(12),(86),(44),(78)**
C B A G E H

2

045

G5

L

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		1 ₂						1 ₁	
row2				1 ₁					1 ₂
row3		1 ₁			1 ₂			1	
row4				1 ₂		1 ₁			
row5			X						
row6							X		
row7					1 ₁			1 ₂	
row8						1 ₂			1 ₁
row9	X								

Example 2.045, continued.

A	B	C
	E	
	H	I

Subpattern-3 begins in **(38)** with box order **C→B→A→E→H→I**
(38) zaps (35) adding **(24)**
(38) zaps (32) adding **(12)**
(24) zaps (44) adding **(46)** zaps (86) adding **(75)** zaps (78) adding **(89)**

Subpattern-3 = **(38),(24),(12),(46),(75),(89)**
C B A E H I

Back at the starting box C, nothing is pending, and no squares are unclaimed, so we are done.

G5

2 045 L

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		1 ₂₃						1 ₁	
row2				1 ₁₃					1 ₂
row3		1 ₁			1 ₂			1 ₃	
row4				1 ₂		1 ₁₃			
row5			X						
row6							X		
row7					1 ₁₃			1 ₂	
row8						1 ₂			1 ₁₃
row9	X								

Pattern 2.156	Box Orientation	Patterns with the same box code
3 - 2 - 2	B - A	none
2 - 2	E - D - F	
2	H	(Box orientation for 156 - swap stacks 1 & 3)

A	B	
D	E	F
	H	

Subpattern-1 begins in (15) with box order **B→A→D→F→E→H**
(15) zaps (12) adding (23) zaps (53) adding (42) zaps (48) adding (68)
(68) zaps (65) adding (56) zaps (86) adding (84)

Subpattern-1 = (15),(23),(42),(68),(56),(84)
B A D F E H

G7		col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
2	156	L								
row1			1			1 ₁				
row2				1 ₁	1		1			
row3								X		
row4			1 ₁						1	
row5				1			1 ₁			
row6					1				1 ₁	
row7										X
row8					1 ₁		1			
row9			X							

Example 2.156. continued.

A	B	
D	E	F
	H	

Subpattern-2 begins in (24) with box order **B→A→D→E→F→H**

(24) zaps (23) adding (12) zaps (42) adding (53) zaps (56) adding (65)
(65) zaps (68) adding (48)
(24) zaps (84) adding (86)

Subpattern-2 = (24),(12),(53),(65),(48),(86)
 B A D E F H

Subpattern-3 begins in (26) with box order **B→A→D→E→F→H**

(26) zaps (23) adding (12) zaps (42) adding (53) zaps (56) adding (65)
(65) zaps (68) adding (48)
(26) zaps (86) adding (84)

Subpattern-3 = (26),(12),(53),(65),(48),(84)
 B A D E F H

Back at the starting box B, nothing is pending, and no squares are unclaimed, so the pattern analysis is complete.

2

156

G7

L

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1

row2

row3

row4

row5

row6

row7

row8

row9

	1 ₂₃			1 ₁				
		1 ₁	1 ₂		1 ₃			
						X		
	1 ₁						1 ₂₃	
		1 ₂₃			1 ₁			
				1 ₂₃			1 ₁	
								X
			1 ₁₃		1 ₂			
X								

Pattern 2.143	Box Orientation	Patterns with the same box code
2-2 3-2-2 2 2	C-A D-E-F H G	none

A		C
D	E	F
G	H	

Subpattern-1 begins in (52) with box order **D(→G)→F→E(→H)→C→A**

(52) zaps (82) adding (83)
(52) zaps (57) adding (49)
 (49) zaps (44) adding (66) zaps (76) adding (74)
 (49) zaps (39) adding (27) zaps (21) adding (31)

Subpattern-1 = (52),(83),(49),(66),(74),(27),(31)
 D G F E H C A

2	143	G6	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						X					
row2	5							5 ₁			
row3	5 ₁									5	
row4				5						5 ₁	
row5		5 ₁	5					5			
row6		5					5 ₁				
row7				5 ₁		5					
row8		5	5 ₁								
row9									X		

Example 2.143, continued.

A		C
D	E	F
G	H	

Subpattern-3 begins in (62) with new box order D(→G)→E(→H)→F→C→A

(62) zaps (83) adding (82)
(62) zaps (66) adding (44) zaps (74) adding (76)
(62) zaps (49) adding (57) zaps (27) adding (39) zaps (31) adding (21)

Subpattern-3 = (62),(82),(44),(76),(57),(39),(21)
D G E H F C A

Back at the starting box, nothing is pending, and no squares are unclaimed, The pattern analysis is complete.

2	143	G6	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
							X				
			5 ₃						5 ₁₂		
			5 ₁₂								5 ₃
						5 ₃					5 ₁₂
				5 ₁	5 ₂				5 ₃		
				5 ₃				5 ₁₂			
						5 ₂		5 ₃			
				5 ₂	5 ₃						
										X	

Pattern 2.053	Box Orientation	Patterns with the same box code
3 – 3	H – B	109
		(Box orientation for 053: rotate 90 degrees clockwise,
2 – 2	I – C	then swap bands 1 & 2, then swap bands 2 & 3)

	B	C
	H	I

Subpattern-1 begins in **(25)** with box order **B→C→I→H**

(25) zaps **(28)** adding **(39)** zaps **(99)** adding **(78)** zaps **(74)** & **(75)** adding **(94)**

Subpattern-1 = **(25),(39),(78),(94)**

B C I H

Subpattern-2 begins in **(34)** with box order **B→C→I→H**

(34) zaps **(39)** adding **(28)** zaps **(78)** adding **(99)**

(34) zaps **(34)** & **(35)** adding **(75)**

Subpattern-2 = **(34),(28),(99),(75)**

B C I H

2	053	L2	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
				X							
							3 ₁			3 ₂	
						3 ₂	3				3 ₁
				X							
								X			
									X		
						3	3 ₂			3 ₁	
				X							
						3 ₁					3 ₂

Pattern 2.053, continued.

	B	C
	H	I

Subpattern-3 begins in **(35)** with box order **B→C→I→H**

(35) zaps (39) adding **(28)** zaps (78) adding **(99)**

(35) zaps (75) while **(99)** zaps (94) adding **(74)**

Subpattern-3 = **(35),(28),(99),(74)**

B C I H

Back at the starting box B, there is nothing pending and no boxes left unclaimed. The analysis is complete.

2 053 L2		col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		X								
row2					3 ₁			3 ₂₃		
row3				3 ₂	3 ₃				3 ₁	
row4			X							
row5						X				
row6							X			
row7				3 ₃	3 ₂			3 ₁		
row8	X									
row9				3 ₁					3 ₂₃	

Pattern 2.138	Box Orientation	Patterns with the same box code
3 – 3 – 2	E – F – D	none
		(Box orientation for 138: swap bands 1 & 2,
2	B	then swap stacks 1 & 2, then stacks 2 & 3)

	B	
D	E	F

Subpattern-1 begins in (46) with box order E→D→F→B

(46) zaps (43) adding (63)
(46) zaps (48) while (63) zaps (68) adding (58)
(46) zaps (16) adding (15)

Subpattern-1 = (46),(63),(58),(15)
E D F B

Subpattern-2 begins in (66) with box order E→D→F→B

(66) zaps (63) adding (43)
(66) zaps (68) while (43) zaps (48) adding (58)
(66) zaps (16) adding (15)

Subpattern-2 = (66),(43),(58),(15)
E D F B

2	138	L3	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row1					7 ₁₂	7			
		row2	X								
		row3							X		
		row4			7 ₂			7 ₁		7	
		row5					7			7 ₁₂	
		row6			7 ₁			7 ₂		7	
		row7		X							
		row8				X					
		row9									X

Pattern 2.138, continued.

	B	
D	E	F

Subpattern-3 begins in (55) with box order **E→D→F→B**

(55) zaps (**nothing**) adding (43) and pending (63)

(55) zaps (58) while (43) zaps (48) adding (68)

(55) zaps (15) adding (16)

Subpattern-3 = (55),(43),(68),(16)

E D F B

Due to the pending situation in **D**, subpattern-4 must
begin in the same starting square (55) as subpattern-3
include the pending square (63)

The box order is chosen to be **E→D→F→B**

(55) zaps (58) while (63) zaps (68) adding (48)

(55) zaps (15) adding (16)

Subpattern-4 = (55),(63),(48),(16)

Back at the starting box E, there is no longer a pending situation, and no boxes remain unclaimed, so the pattern analysis is complete.

2	138	L3	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							7 ₁₂	7 ₃₄			
row2	X										
row3									X		
row4			7 ₂₃				7 ₁		7 ₄		
row5	P					7 ₃₄			7 ₁₂		
row6			7 ₁₃			7 ₂		7 ₃			
row7		X									
row8				X							
row9										X	

Pattern 2.001	Box Orientation	Patterns with the same box code
3 – 3 – 2	B – H – E	005, 016, 022, 024, 034, 035, 040, 042, 043,
		054, 055, 060, 069, 084, 086, 139, 144, 147,
2 – 2	C – I	153.
(Box orientation for 001: rotate 90 degrees clockwise, then swap bands 1 & 2, then swap bands 2 & 3, then swap stacks 2 & 3, then swap stacks 1 & 2)		

	B	C
	E	
	H	I

Subpattern-1 starts in **(24)** with box order **B→C→I→H→E**

(24) zaps (27) adding **(38)** zaps (78) adding **(87)** zaps (84) & (86) adding **(75)**
(24) zaps (54) adding **(56)**

Subpattern-1 = **(24),(38),(87),(75),(56)**
B C I H E

Subpattern-2 starts in **(26)** with box order **B→C→I→H→E**

(26) zaps (27) adding **(38)** zaps (78) adding **(87)** zaps (84) & (86) adding **(75)**
(26) zaps (56) adding **(54)**

Subpattern-2 = **(26),(38),(87),(75),(54)**
B C I H E

2	001	ML	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row1	X								
		row2				6 ₁		6 ₂	6		
		row3					6			6 ₁₂	
		row4		X							
		row5				6 ₂		6 ₁			
		row6									X
		row7					6 ₁₂			6	
		row8				6		6	6 ₁₂		
		row9			X						

Pattern 2.085	Box Orientation	Patterns with the same box code
3 – 3	I – H	087
3 – 2	F – E	
(Box orientation for 085: swap bands 1 & 3, then swap stacks 1 & 3)		

	E	F
	H	I

Subpattern-1 begins in (78) with box order I→F→E→H

(78) zaps (68) & (48) adding (49) zaps (44) adding (66)
(78) zaps (74) & (76) adding (94)

Subpattern-1 = (78),(49),(66),(94)
I H E F

Subpattern-2 begins in (98) with box order I→F→E→H

(98) zaps (68) & (48) adding (49) zaps (44) adding (66)
(66) zaps (76) while (98) zaps (94) adding (74)

Subpattern-2 = (98),(49),(66),(74)
I F E H

2	085	N	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row1	X								
		row2					X				
		row3							X		
		row4				8				8	8 ₁₂
		row5		X							
		row6						8 ₁₂		8	
		row7				8 ₂		8		8 ₁	
		row8			X						
		row9				8 ₁				8 ₂	8

Pattern 2.085, continued.

	E	F
	H	I

Subpattern-3 begins in **(99)** with box order **I→F→E→H**

(99) zaps (49) adding **(68)** and pending **(48)**

(68) zaps (66) adding **(44)** zaps (74) & (94) adding **(76)**

Subpattern-3 = **(99),(68),(44),(76)**

I F E H

Due to the pending condition in **F**, subpattern-4 must
begin in the same starting square **(99)** as subpattern-3
include the pending square **(48)**

Box order will be **I→F→E→H**

(48) zaps (44) adding **(66)**

(66) zaps (76) while **(99)** zaps (94) adding **(74)**

Subpattern-4 = **(99),(48),(66),(74)**

2	085	N	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		X									
row2					X						
row3								X			
row4				8₃						8₄	8₁₂
row5		X									P
row6							8₁₂₄			8₃	
row7				8₂₄			8₃			8₁	
row8			X								
row9				8₁						8₂	8₃₄

Pattern 2.136	Box Orientation	Patterns with the same box code
3 – 3	A – C	none
3 – 2 – 2	G – I – H	

A		C
G	H	I

Subpattern-1 begins in **(98)** with box order **I→H→G→A→C**

(98) zaps (96) adding **(86)** zaps (81) adding **(73)** zaps (13) & (33) adding **(11)**
(98) zaps (18) & (38) adding **(37)**

Subpattern-1 = **(98),(86),(73),(11),(37)**
I H G A C

Subpattern-2 begins in **(97)** with box order **I→H→G→A→C**

(97) zaps (96) adding **(86)** zaps (81) adding **(73)** zaps (13) & (33) adding **(11)**
(11) zaps (18) while **(97)** zaps (37) adding **(38)**

Subpattern-2 = **(97),(86),(73),(11),(38)**
I H G A C

2	136	O	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	1 ₁₂		1						1		
row2				X							
row3	P		1					1 ₁	1 ₂		
row4		X									
row5					X						
row6										X	
row7			1 ₁₂					1			
row8	1						1 ₁₂				
row9							1	1 ₂	1 ₁		

Pattern 2.136, continued

A		C
G	H	I

Subpattern-3 begins in (77) with box order **I→G→H→A→C**

(77) zaps (73) adding (81) zaps (86) adding (96)

(81) zaps (11) adding (13) and pending (33)

(13) zaps (18) while (77) zaps (37) adding (38)

Subpattern-3 = (77),(81),(96),(13),(38)

I G H A C

Due to the pending condition in **A**, subpattern-4 must

begin in the same starting square (77) as subpattern-3

share squares (96), (81) with subpattern-3

include the pending square (33)

(33) zaps (37) & (38) adding (18)

Subpattern-4 = (77),(96),(81),(33),(18)

I G H A C

Back at the starting box I, there is no longer a pending situation, and no squares remain unclaimed, so the analysis is complete.

2	136	O	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			1 ₁₂		1 ₃					1 ₄	
row2						X					
row3			P		1 ₄				1 ₁	1 ₂₃	
row4				X							
row5							X				
row6											X
row7					1 ₁₂				1 ₃₄		
row8			1 ₃₄					1 ₁₂			
row9								1 ₃₄	1 ₂	1 ₁	

Pattern 2.013	Box Orientation	Patterns with the same box code
4 – 2	F – D	028, 052, 101, 130, 132.
2	C	
(Box orientation for 013: Swap stacks 1 & 2, then swap bands 1 & 2)		

		C
D		F

Box order: F→D→C

Subpattern-1 begins in **(47)** zaps (41) adding **(61)**
(47) zaps (37) adding **(39)**

Subpattern-1 = **(47),(61),(39)**
F D C

Subpattern-2 begins in **(49)** zaps (41) adding **(61)**
(49) zaps (39) adding **(37)**

Subpattern-2 = **(49),(61),(37)**
F D C

2	013	P	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				X							
row2					X						
row3									3 ₂		3 ₁
row4	3								3 ₁		3 ₂
row5					X						
row6	3 ₁₂								3		3
row7							X				
row8				X							
row9										X	

Pattern 2.013, continued.

		C
D		F

Box order: F→D→C

Subpattern-3 begins in (67) zaps (61) adding (41)
(67) zaps (37) adding (39)

Subpattern-3 = (67),(41),(39)
F D C

Subpattern-4 begins in (69) zaps (61) adding (41)
(69) zaps (39) adding (37)

Subpattern-4 = (69),(41),(37)
F D C

At the starting box, nothing is pending and no squares are unclaimed.
The pattern analysis is complete..

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
2 013 P									
row1		X							
row2				X					
row3							3 ₂₄		3 ₁₃
row4	3 ₃₄						3 ₁		3 ₂
row5					X				
row6	3 ₁₂						3 ₃		3 ₄
row7						X			
row8			X						
row9								X	

Pattern 2.018	Box Orientation	Patterns with the same box code 041, 057, 064, 112, 125, 137, 141.
2 4 – 2 2	G F – I D	(Box orientation for 013: rotate 90 degrees counterclockwise, then swap stacks 1 & 2, then stacks 2 & 3, then swap bands 2 & 3)

D		F
G		I

Box order: F→D→I→G

Subpattern-1 begins in **(47)** zaps (41) adding **(61)**
(47) zaps (97) adding **(79)** zaps (72) adding **(92)**

Subpattern-1 = **(47),(61),(79),(92)**
F D I G

Subpattern-2 begins in **(49)** zaps (41) adding **(61)**
(49) zaps (79) adding **(97)** zaps (92) adding **(72)**

Subpattern-2 = **(49),(61),(97),(72)**
F D I G

2	018	Q	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1								X			
row2										X	
row3			X								
row4	6								6 ₁		6 ₂
row5					X						
row6	6 ₁₂								6		6
row7		6 ₂									6 ₁
row8				X							
row9		6 ₁							6 ₂		

Example 2.018, continued.

D		F
G		I

Box order: F→D→I→G

Subpattern-3 begins in (67) zaps (61) adding (41)
(67) zaps (97) adding (79) zaps (72) adding (92)

Subpattern-3 = (67),(41),(79),(92)
F D I G

Subpattern-4 begins in (69) zaps (61) adding (41)
(69) zaps (79) adding (97) zaps (92) adding (72)

Subpattern-4 = (69),(41),(97),(72)
F D I G

Back at the starting box, F, there is no pending condition, and no squares remain unclaimed, so the analysis is complete.

2 018 Q		col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						X				
row2								X		
row3			X							
row4	6 ₃₄							6 ₁		6 ₂
row5					X					
row6	6 ₁₂							6 ₃		6 ₄
row7		6 ₂₄								6 ₁₃
row8				X						
row9		6 ₁₃						6 ₂₄		

Pattern 2.058	Box Orientation	Patterns with the same box code
4 – 2 – 2	D – A – G	none
2	E	(Box orientation for 013: rotate 90 degrees clockwise, then swap stacks 1 & 2, then stacks 2 & 3)

A	B	C
D	E	F
G	H	I

Subpattern-1 begins in **(41)** with box order **D→A→G→E**

(41) zaps (31) adding **(32)** zaps (92) adding **(93)**
(41) zaps (45) adding **(65)**

Subpattern-1 = **(41),(32),(93),(65)**
D A G E

Subpattern-2 begins in **(43)** with box order **D→G→A→E**

(43) zaps (93) adding **(92)** zaps (32) adding **(31)**
(43) zaps (45) adding **(65)**

Subpattern-2 = **(43),(92),(31),(65)**
D G A E

2	058	R	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1											X
row2				X							
row3	2 ₂	2 ₁									
row4	2 ₁		2 ₂		2						
row5											
row6	2 ₃		2 ₄		2 ₁₂						
row7									X		
row8						X					
row9		2 ₂	2 ₁								

Example 2.058, continued.

A	B	C
D	E	F
G	H	I

Subpattern-3 begins in **(61)** with box order **D→A→G→E**

(61) zaps (31) adding **(32)** zaps (92) adding **(93)**

(61) zaps (65) adding **(45)**

Subpattern-3 = **(61),(32),(93),(45)**

D A G E

Subpattern-4 begins in **(63)** with box order **D→G→A→E**

(63) zaps (93) adding **(92)** zaps (32) adding **(31)**

(63) zaps (65) adding **(45)**

Subpattern-4 = **(63),(92),(31),(45)**

D G A E

Back at the starting box, nothing is pending and no squares unclaimed, so the analysis is complete.

2	058	R	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row1									X
		row2				X					
		row3	2 ₂₄	2 ₁₃							
		row4	2 ₁		2 ₂		2 ₃₄				
		row5									
		row6	2 ₃		2 ₄		2 ₁₂				
		row7								X	
		row8						X			
		row9		2 ₂₄	2 ₁₃						

Pattern 2.134	Box Orientation	Patterns with the same box code
$\begin{array}{c} 2-2 \\ \\ 4-2 \\ \\ 2 \end{array}$	$\begin{array}{c} I-C \\ \\ E-H \\ \\ D \end{array}$	none
		(Box orientation for 134: rotate 90 degrees counterclockwise, then swap stacks 1 & 2, then swap stacks 2 & 3)

		C
D	E	
	H	I

Box order: E→D→H→I→C

Subpattern-1 begins in (44) zaps (41) adding (51)
(44) zaps (94) adding (86) zaps (89) adding (98) zaps (28) adding (29)

Subpattern-1 = (44),(51),(86),(98),(29)
E D H I C

Subpattern-2 begins in (46) zaps (41) adding (51)
(46) zaps (86) adding (94) zaps (98) adding (89) zaps (29) adding (28)

Subpattern-2 = (46),(51),(94),(89),(28)
E D H I C

2	134	S	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
							X				
row1											
										5 ₂	5 ₁
row2											
		X									
row3											
	5			5 ₁		5 ₂					
row4											
	5 ₁₂			5		5					
row5											
									X		
row6											
			X								
row7											
						5 ₁				5 ₂	
row8											
				5 ₂						5 ₁	
row9											

Example 2.134, continued.

		C
D	E	
	H	I

Box order: E→D→H→I→C

Subpattern-3 begins in (54) zaps (51) adding (41)
(54) zaps (94) adding (86) zaps (89) adding (98) zaps (28) adding (29)

Subpattern-3 = (54),(41),(86),(98),(29)
 E D H I C

Subpattern-4 begins in (56) zaps (51) adding (41)
(56) zaps (86) adding (94) zaps (98) adding (89) zaps (29) adding (28)

Subpattern-4 = (56),(41),(94),(89),(28)

Back at the starting box, nothing is pending and no squares unclaimed,
so the analysis is complete.

2	134	S	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
							X				
row1											
										5 ₂₄	5 ₁₃
row2											
		X									
row3											
	5 ₃₄			5 ₁		5 ₂					
row4											
	5 ₁₂			5 ₃		5 ₄					
row5											
									X		
row6											
			X								
row7											
						5 ₁₃				5 ₂₄	
row8											
				5 ₂₄						5 ₁₃	
row9											

Pattern 2.148	Box Orientation	Patterns with the same box code
4 – 2 – 2	A – D – G	149
		(Box orientation for 148:
2	C	rotate 90 degrees counterclockwise,
		then swap stacks 2 & 3, then swap stacks 1 & 2)

A		C
D		
G		

Subpattern-1 begins in (21) with box order A→G→D→C

(21) zaps (71) adding (72) zaps (42) adding (43)
(21) zaps (29) adding (39)

Subpattern-1 = (21),(72),(43),(39)
A G D C

Subpattern-2 begins in (23) with box order A→D→G→C

(23) zaps (43) adding (42) zaps (72) adding (71)
(23) zaps (29) adding (39)

Subpattern-2 = (23),(42),(71),(39)
A D G C

2	148	T	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
						X					
			9 ₁		9 ₂						9
				9	9						9 ₁₂
				9 ₂	9 ₁						
										X	
								X			
			9 ₂	9 ₁							
							X				
									X		

Example 2.148, continued.

A		C
D		
G		

Subpattern-3 begins in (32) with box order A→D→G→C

- (32) zaps (42) adding (43)
- (32) zaps (72) adding (71)
- (32) zaps (39) adding (29)

Subpattern-3 = (32),(43),(71),(29)
 A D G C

Subpattern-4 begins in (33) with box order A→D→G→C

- (33) zaps (43) adding (42) zaps (72) adding (71)
- (33) zaps (39) adding (29)

Subpattern-4 = (33),(42),(71),(29)
 A D G C

Back at the starting box, nothing is pending and no square unclaimed.
The pattern analysis is complete.

2	148	T	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row1				X					
		row2	9 ₁		9 ₂						9 ₃₄
		row3		9 ₃	9 ₄						9 ₁₂
		row4		9 ₂₄	9 ₁₃						
		row5								X	
		row6						X			
		row7	9 ₂₃₄	9 ₁							
		row8					X				
		row9							X		

Pattern 2.065	Box Orientation	Patterns with the same box code
4 - 2 - 2	B - H - E	none
3 - 2	A - G	
(Box orientation for 065: rotate 90 degrees counterclockwise, then swap bands 1 & 2, then swap bands 2 & 3, then swap stacks 2 & 3)		

A	B	
	E	
G	H	

Subpattern-1 begins in **(14)** with box order **B→E→H→G→A**

(14) zaps (54) adding **(55)**

(14) zaps (94) adding **(76)** zaps (72) adding **(91)**

(91) zaps (31) while **(14)** zaps (12) adding **(32)**

Subpattern-1 = **(14),(55),(76),(91),(32)**

B E H G A

2 U	065	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1		2		2 ₁		2			
	row2								X	
	row3	2	2 ₁		2	2				
	row4			X						
	row5				2	2 ₁				
	row6							X		
	row7		2 ₂				2 ₁			
	row8									X
	row9	2 ₁			2					

Example 2.065, continued.

A	B	
	E	
G	H	

Subpattern-2 begins in **(16)** with box order **B→H→E→G→A**

(16) zaps (76) adding **(94)** zaps (91) adding **(72)** zaps (12) & (32) adding **(31)**
(31) zaps (34) & (35) while **(76)** zaps (16) adding **(14)**

Subpattern-2 = **(16),(94),(72),(31),(14)**

Subpattern-3 begins in **(34)** with box order **B→H→G→eE→A**

(34) zaps (94) adding **(76)** zaps (72) adding **(91)**

(34) zaps (54) adding **(55)**

(34) zaps (31) & (32) adding **(12)**

Subpattern-3 = **(34),(76),(91),(55),(12)**
B H G E A

2 U	065	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1		2 ₃		2 ₁		2 ₂			
	row2								X	
	row3	2 ₂	2 ₁		2 ₃	2				
	row4			X						
	row5				2 ₄	2 ₁₂₃				
	row6							X		
	row7		2 ₂				2 ₁₃			
	row8									X
	row9	2 ₁₃			2 ₂					

Example 2.065, continued.

A	B	
	E	
G	H	

Subpattern-4 begins in (35) with box order **B→E→H→G→A**
(35) zaps (55) adding (54) zaps (94) adding (76) zaps (72) adding (91)
(35) zaps (31) & (32) adding (12)
Subpattern-4 = (35),(54),(76),(91),(12)

Back at the starting box B, there are no boxes pending and no squares unclaimed.
The analysis is complete.

2	065	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
U	row1		2 ₃₄		2 ₁		2 ₂			
	row2								X	
	row3	2 ₂	2 ₁		2 ₃	2 ₄				
	row4			X						
	row5				2 ₄	2 ₁₂₃				
	row6							X		
	row7		2 ₂				2 ₁₃₄			
	row8									X
	row9	2 ₁₃₄			2 ₂					

Pattern 2.025	Box Orientation	Patterns with the same box code
4 - 3 - 2	A - B - C	none
2 - 2	D - E	

A	B	C
D	E	

Box order: A→C→D→E→B

Subpattern-1 begins in (22) zaps (27) adding (37)
(22) zaps (52) adding (43) zaps (46) adding (55)
(55) zaps (15) while (22) zaps (27) adding (16)
Subpattern-1 = (22),(37),(43),(55),(16)

A C D E B

Subpattern-2 begins in (23) zaps (27) adding (37)
(23) zaps (43) adding (52) zaps (55) adding (46) zaps (16) & (36) adding (15)
Subpattern-2 = (23),(37),(52),(46),(15)

A C D E B

2	025	U2	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							8 ₂	8 ₁₃			
row2			8 ₁	8 ₂					8 ₃		
row3			8 ₃	8				8 _K	8 ₁₂		
row4				8 ₁₃				8 ₂			
row5			8 ₂				8 ₁₃				
row6										X	
row7	X										
row8					X						
row9											X

Example 2.025, continued.

A	B	C
D	E	

Box order: A→C→D→E→B

Subpattern-3 begins in (32) zaps (37) adding (27)

(32) zaps (52 adding (43) zaps (46) adding (55)

(55) zaps (15) while (32) zaps (36) adding (27)

Subpattern-3 = (32),(27),(43),(55),(27)

A C D E B

Subpattern-4 begins in (33) zaps (37) adding (27)

(33) zaps (43) adding (52) zaps (55) adding (46) zaps (36) & (16) adding (15)

Subpattern-4 = (33),(27),(52),(46),(15)

A C D E B

Back at the starting box, there is no pending situation, and no square unclaimed in the starting box A, but there is an unclaimed square in box B, namely (36), which is not a member of any subpattern. Therefore it is a killer candidate, and should be subscripted with a K. The analysis is complete.

2	025	U2	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
							8 ₂₄	8 ₁₃			
				8 ₁	8 ₂				8 ₃₄		
				8 ₃	8 ₄			8 _K	8 ₁₂		
					8 ₁₃			8 ₂₄			
				8 ₂₄			8 ₁₃				
										X	
				X							
						X					
											X

Pattern 2.100	Box Orientation	Patterns with the same box code
3 – 3 – 2	I→H→G	102

G	H	I

	1	2	3	4	5	6	7	8	9
1						X			
2								X	
3	X								
4		X							
5							X		
6					X				
7			3						3
8				3					3
9			3	3					3

Since all the drama is in the bottom six boxes, we'll dispense with the top six boxes during the analysis.

2	100	W1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row7			3						3 ₁
		row8				3					3
		row9			3	3					3

Box order: I→H→G
Subpattern-1 begins in (79) zaps (73) adding (93) zaps (94) adding (84)
Subpattern-1 = (79),(93),(64)
I H G

2	100	W1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row7			3						3 ₁
		row8				3 ₁					3
		row9			3 ₁	3					3

Pattern 2.100, continued.

Box order: **I→H→G**

Subpattern-2 begins in **(89)** zaps (84) adding **(94)** zaps (93) adding **(73)**

Subpattern-2 = **(89),(94),(73)**

I H G

2	100	W1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row7			3 ₂						3 ₁
		row8				3 ₁					3 ₂
		row9			3 ₁	3 ₂					3

Box order: **I→H→G**

Subpattern-3 begins in **(99)** zaps (94) adding **(84)**
(99) zaps (73) adding **(93)**

Subpattern-3 = **(99),(84),(93)**

I H G

2	100	W1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row7			3 ₂						3 ₁
		row8				3 ₁₃					3 ₂
		row9			3 ₁	3 ₂					3 ₃

This middle section is reconnected with the rest of the sudoku on the next page.

2 100 W1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						X			
row2								X	
row3	X								
row4		X							
row5							X		
row6					X				
row7			3 ₂₃						3 ₁
row8				3 ₁₃					3 ₂
row9			3 ₁	3 ₂					3 ₃

Pattern 2.121	Box Orientation	Patterns with the same box code
3 – 2 – 2	B – E – H	061, 116
2	F	
(Box orientation for 121: rotate 90 degrees clockwise, then swap stacks 1 & 3)		

	B	
	E	F
	H	

Subpattern-1 begins in (24) with box order **B→E→F→H**

(24) zaps (64) adding (46) zaps (47) adding (67)
(24) zaps (24) while (46) zaps (26) adding (25)

Subpattern-1 = (24),(46),(67),(25)
 B E F H

Subpattern-2 begins in (25) with box order **B→H→E→F**

(25) zaps (95) adding (94) zaps (64) adding (46) zaps (47) adding (67)

Subpattern-2 = (25),(94),(46),(67)
 B H E F

2	121	W2	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1											
row2				9 ₁	9 ₂	9					
row3											
row4							9 ₁₂	9			
row5											
row6				9				9 ₁₂			
row7											
row8											
row9				9 ₂	9 ₁						

Pattern 2.129	Box Orientation	Patterns with the same box code
3 - 2 - 2	G - A - D	none
2	B	
2	C	
(Box orientation for 129: rotate 90 degrees clockwise, then swap stacks 2 & 3)		

A	B	C
D		
G		

Subpattern-1 begins in (81) with box order G→D→A→C→B

(81) zaps (51) adding (53) zaps (23) adding (32) zaps (39) adding (19)
(19) zaps (16) adding (26)

Subpattern-1 = (81),(53),(32),(19),(26)
 G D A C B

Subpattern-2 begins in (82) with box order G→A→B→C→D

(82) zaps (32) adding (23) zaps (26) adding (16) zaps (19) adding (39)
(23) zaps (51) adding (51)

Subpattern-2 = (82),(23),(16),(39),(51)
 G A B C D

2	129	W3	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							8 ₂				8 ₁
row2			8 ₂				8 ₁				
row3		8 ₁									8 ₂
row4					X						
row5	8 ₂		8 ₁								
row6								X			
row7				X							
row8	8 ₁	8 ₂	8								
row9									X		

Example 2.129, continued.

A	B	C
D		
G		

Subpattern-1 begins in **(83)** with box order **G→D→A→C→B**

(83) zaps (53) adding **(51)**

(83) zaps (23) adding **(32)** zaps (39) adding **(19)** zaps (16) adding **(26)**

Subpattern-3 = **(83),(51),(32),(19),(26)**

Back in the starting box G, no boxes are pending and no squares are unclaimed. The analysis is complete.

2	129	W3	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row1						8 ₂			8 ₁₃
		row2			8 ₂			8 ₁₃			
		row3		8 ₁₃							8 ₂
		row4					X				
		row5	8 ₂₃		8 ₁						
		row6							X		
		row7				X					
		row8	8 ₁	8 ₂	8 ₃						
		row9								X	

Pattern 2.090, continued.

Subpattern-2 begins in (39) with box order $C \rightarrow B \rightarrow A \rightarrow H \rightarrow G$

(39) zaps (35) adding (16)

(39) zaps (31), adding (21)

(16) zaps (96) adding (75) zaps (73) adding (93)

Subpattern-2 = (39),(16),(21),(75),(93)

C B A H G

Subpattern-3 starts in (29) with box order to $C \rightarrow A \rightarrow B \rightarrow H \rightarrow G$

(29) zaps (21) adding (31) zaps (35) adding (16)

(16) zaps (96) adding (75) zaps (73) adding (93)

Subpattern-3 = (29),(31),(16),(75),(93)

C A B H G

Back at the starting box, nothing is pending, and no boxes remain unclaimed. The pattern analysis is complete.

2	090	W5	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row1						2 ₂			2 ₁
		row2	2 ₁₂								2
		row3	2				2 ₁				2 ₂
		row4		X							
		row5								X	
		row6				X					
		row7			2 ₁		2 ₂₃				
		row8							X		
		row9			2 ₂₃			2 ₁			

Pattern 2.012	Box Orientation	Patterns with the same box code
3 - 2 - 2 2 - 2 2 ----- 2	I - H - G C - B F-----D	032, 033 (same structure except for one 2-box replaced by 3-box or 4-box) (Box orientation for 012: rotate 180 degrees clockwise, then swap bands 2 & 3)

	B	C
D		F
G	H	I

	•	←
→		↑
↑	←	←

Subpattern-1 is started in (79) with box order **I→H→G→D→F→C→B**

(79) zaps (75) adding (94) zaps (93) adding (82) zaps (62) adding (53)
 (53) zaps (57) adding (68).

Then (79) zaps (39) adding (27) zaps (24) adding (35).

Subpattern-1 = (79),(94),(82),(53),(68),(27),(35)

I H G D F C B

2	012	W6	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X								
row2				2				2 ₁			
row3					2 ₁					2	
row4						X					
row5			2 ₁					2			
row6		2							2 ₁		
row7					2					2 ₁	
row8		2 ₁							2		
row9			2	2 ₁				2			

Pattern 2.012 continued.

	B	C
D		F
G	H	I

	↓	←
→		↑
↑	•	←

Subpattern-2 is started in **(88)** with box order **I→G→D→F→C→B→H**

(88) zaps (82) adding **(93)** zaps (53) adding **(62)** zaps (68) adding **(57)** zaps (27)
(57) zaps (27) adding **(39)** zaps (35) adding **(24)**. zaps (94) adding **(75)**.

Subpattern-2 = **(88),(93),(62),(57),(39),(24),(75)**
I G D F C B H

2	012	W6	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row1			X						
		row2				2 ₂			2 ₁		
		row3					2 ₁				2 ₂
		row4						X			
		row5			2 ₁				2 ₂		
		row6		2 ₂						2 ₁	
		row7					2 ₂₃				2 ₁
		row8		2 ₁						2 ₂	
		row9			2 ₂	2 ₁			2 ₃		

Pattern 2.012 continued.

	B	C
D		F
G	H	I

	↓	←
→		↑
↑	•	←

Subpattern-3 is started in (97) with box order **I→H→G→D→F→C→B**

(97) zaps (94) adding (75).

(97) zaps (93) adding (82) zaps (62) adding (53) zaps (57) adding (68).

(97) zaps (27) adding (39) zaps (35) adding (24).

Subpattern-3 = (97),(75),(82),(53),(68),(39),(24)

I H G D F C B

2	012	W6	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X								
row2				2 ₂₃				2 ₁			
row3					2 ₁					2 ₂₃	
row4						X					
row5			2 ₁₃					2 ₂			
row6		2 ₂							2 ₁₃		
row7					2 ₂₃					2 ₁	
row8		2 ₁₃							2 ₂		
row9			2 ₂	2 ₁				2 ₃			

Back at the starting box I, there are no outstanding pending boxes and no unclaimed squares, either in the starting box or elsewhere, so the analysis is complete.

Pattern 2.032	Box Orientation	Patterns with the same box code
3 - 2 - 3	I - H - G	none (several have same structure but
		with one higher-order box)
3 - 2	C - B	(Box orientation for 032:
		rotate 180 degrees clockwise,
2 ----- 2	F-----D	then swap bands 2 & 3)

	B	C
D		F
G	H	I

	•	←
→		↑
↑	←	←

Subpattern-1 is started in (79) with box order **I→H→G→D→F→C→B**

(79) zaps (75) adding (94)

(79) zaps.(72) while (94) zaps (93) adding (82) zaps (62) adding (53)

(53) zaps (57) adding (68)

(79) zaps (39) while (68) zaps (38) adding (27) zaps (24) adding (35)

Subpattern-1 = (79),(94),(82),(53),(68),(27),(35)

I H G D F C B

2 032 W7 col 1 col 2 col 3 col 4 col 5 col 6 col 7 col 8 col 9

row1	X								
row2				5			5 ₁		
row3					5 ₁			5	5
row4						X			
row5			5 ₁				5		
row6		5						5 ₁	
row7		5			5				5 ₁
row8		5 ₁						5	
row9			5	5 ₁			5		

Pattern 2.032, continued.

	B	C
D		F
G	H	I

	↓	←
•		↑
↑	←	↑

Subpattern-2 is started in **(88)** with box order **I→F→C→B→H→G→D**

(88) zaps (68) adding **(57)**.
(88) zaps.(38) & **(57)** zaps (27) adding **(39)** zaps (35) adding **(24)** zaps (94) adding **(75)**
(88) zaps (82) & **(75)** zaps (72) adding **(93)** zaps (53) adding **(62)**

Subpattern-2 = **(88),(57),(39),(24),(75),(93),(62)**
I F C B H G D

2	032	W6	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row1	X								
		row2				5 ₂			5 ₁		
		row3					5 ₁			5	5 ₂
		row4						X			
		row5			5 ₁				5 ₂		
		row6		5 ₂						5 ₁	
		row7		5			5 ₂				5 ₁
		row8		5 ₁						5 ₂	
		row9			5 ₂	5 ₁			5		

Pattern 2.032, continued.

	B	C
D		F
G	H	I

	•	←
→		↑
↑	←	←

Subpattern-3 is started in (97) with box order **I→H→G→D→F→C→B**

(97) zaps (94) adding (75)
(97) zaps.(93) while (75) zaps (72) adding (82) zaps (62) adding (53)
(53) zaps (57) adding (68)
(97) zaps (27) while (68) zaps (38) adding (39) zaps (35) adding (24)

Subpattern-3 = (97),(75),(82),(53),(68),(39),(24)
I H G D F C B

Back at the starting box I, nothing is pending. Squares (38) and (72) are unclaimed, so they are not members of any subpattern, and must be given killer K subscripts.

2	032	W6	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	X										
row2				5 ₂₃				5 ₁			
row3					5 ₁				5 _K	5 ₂₃	
row4							X				
row5			5 ₁₃					5 ₂			
row6		5 ₂							5 ₁₃		
row7		5 _K			5 ₂₃					5 ₁	
row8		5 ₁₃							5 ₂		
row9			5 ₂	5 ₁				5 ₃			

Pattern 2.033	Box Orientation	Patterns with the same box code
4 - 2 - 2	A - C - B	*016, *032.
3 - 2	D - F	
2 ----- 2	G-----H	

A	B	C
D		F
G	H	

→	→	↓
↓		←
→	•	

Subpattern-1 is started in (12) with box order A→B→C→F→D→G→H

(12) zaps (15) adding (24) zaps (17) adding (38) zaps (48) adding (57)
(57) zaps (51) & (53) adding (43)
(12) zaps.(92) adding (81) zaps (84) adding (95)

Subpattern-1 = (12),(24),(38),(57),(43),(18),(95)
A B C F D G H

2	033	W6	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				1 ₁			1				
row2			1		1	1 ₁			1		
row3					1					1 ₁	
row4					1 ₁					1	
row5			1		1				1 ₁		
row6								X			
row7											X
row8			1 ₁			1					
row9				1			1 ₁				

Pattern 2.033, continued.

	B	C
D		F
G	H	I

	↓	←
•		↑
↑	←	↑

Subpattern-2 is started in (21) with box order **A→B→C→F→D→G→H**

(21) zaps (24) adding (15)
(21) zaps (27) adding (38) zaps (48) adding (57) zaps (51) & (53) adding (43)
(21) zaps (81) adding (92) zaps (95) adding (84)

Subpattern-2 = (21),(15),(38),(57),(43),(91),(84)
 A B C F D G H

2	033	W6	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		1 ₁			1 ₂						
row2	1 ₂		1	1 ₁			1				
row3			1						1 ₁₂		
row4			1 ₁₂						1		
row5	1		1					1 ₁₂			
row6						X					
row7										X	
row8	1 ₁			1 ₂							
row9		1 ₂			1 ₁						

Pattern 2.033, continued.

	B	C
D		F
G	H	I

	•	←
→		↑
↑	←	←

Subpattern-3 is started in (23) with box order $A \rightarrow B \rightarrow C \rightarrow F \rightarrow D \rightarrow G \rightarrow H$

(23) zaps (24) adding (15)

(23) zaps.(27) adding (38) zaps (48) adding (57) zaps (51) & (53).

(23) zaps (43)

But then (51), (53) & (53) are all zapped, leaving nothing in box D. Therefore our choice of (23) as the beginning square for subpattern-3 leads to an impossibility, so we must abandon (23) and try the other available square (33) as the beginning square for subpattern-3. We must first backtrack to box A, erasing all the subscript 3's.

Subpattern-3 is next started in (33) with box order $A \rightarrow C \rightarrow B \rightarrow F \rightarrow D \rightarrow G \rightarrow H$

(33) zaps (38) adding (27) zaps (24) making (15)

(27) zaps.(57) adding (48).

(33) zaps (43) & (53) adding (51) zaps (81) adding (92) zaps (95) adding (84)

Subpattern-3 = (33),(27),(15),(48),(51),(92),(84)

A C B F D G H

Back at the starting box I, nothing is pending. Squares (38) and (72) are unclaimed, so they are not members of any subpattern, and must be given killer K subscripts.

2	033	W6	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			1 ₁				1 ₂₃				
row2		1 ₂		1 _K	1 ₁				1 ₃		
row3				1 ₃						1 ₁₂	
row4				1 ₁₂						1 ₃	
row5		1 ₃		1 _K					1 ₁₂		
row6								X			
row7											X
row8		1 ₁				1 ₂₃					
row9			1 ₂₃				1 ₁				

Notes on patterns 2.012, 2.032, and 2.033:

These three patterns are quite unusual. All three are slightly different from one another, yet all three have exactly the same set of subscripts. All of this is caused by the K subscripts. If it weren't for the killer candidates, the patterns would be identical. Patterns 2.012 and 1.032 are even in the same set of boxes.

Pattern 2.081	Box Orientation	Patterns with the same box code
3 – 3 – 2	D – E – F	142

Since the top and bottom bands have no candidates, we'll leave them out.

D	E	F	→	•	←

Subpattern-1 is started in (41) with box order D→F→E

(41) zaps (49) adding (69).
(41) zaps (45) while (69) zaps (65) adding (55)

Subpattern-1 = (41),(69),(55)
 D F E

Subpattern-2 is started in (51) with box order D→F→E

(51) zaps (55) adding (45) and pending (65)
(45) zaps (49) adding (69)

Subpattern-2 = (45),(69),(54)
 D F E

2	081	X1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
			2 ₁				2 ₂				2
			2 ₂				2 ₁				
			2				2 _p	P			2 ₁₂

Pattern 2.081, continued.

Subpattern-3 is started in **(51)** (same as subpattern-2) with box order **D→F→E**

(65) no longer pending zaps (69) adding **(49)**

Subpattern-3 = **(51),(65),(49)**
D F E

2	081	X1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row4	2 ₁				2 ₂				2 ₃
		row5	2 ₂₃				2 ₁	P			
		row6	2				2 ₃				2 ₁₂

Back at the starting box A, there is nothing pending, but there is still an unassigned square, (61), looking for a subpattern, so

Subpattern-4 is started in **(61)** with box order **D→F→E**

(61) zaps (69) adding **(49)**
(61) zaps (65) while **(49)** zaps (45) adding **(55)**

Subpattern-4 = **(61),(49),(55)**

Back at the starting box D, nothing is pending, and no squares anywhere without subpatterns. The analysis is complete.

2	081	X1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row4	2 ₁				2 ₂				2 ₃₄
		row5	2 ₂₃				2 ₁₄				
		row6	2 ₄				2 ₃				2 ₁₂

Pattern 2.099	Box Orientation	Patterns with the same box code
3 – 3 – 2	A – D – G	none
2	I	

A		
D		
G		I

↓		
↓		
→		•

Subpattern-1 is started in (21) with box order A→G→I→D

(21) zaps (81) adding (73) zaps (78) adding (88)
(21) zaps (51) while (73) zaps (53) adding (52)

Subpattern-1 = (21),(73),(88),(52)
 A G I D

Subpattern-2 is started in (22) with box order A→D→I→G

(22) zaps (52) adding (51) and pending (53)
(51) zaps (81) adding (73) zaps (78) adding (88)

Subpattern-2 = (22),(51),(73),(88)

2	009	L1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row1							X		
		row2	8 ₁	8 ₂							
		row3				X					
		row4									X
		row5	8 ₂	8 ₁							
		row6					X				
		row7			8 ₁₂					8	
		row8	8							8 ₁₂	
		row9						X			

Pattern 2.099, continued.

A								
D								
G		I						

↓								
↓								
→			•					

Due to pending situation,

Subpattern-3 must have the same starting square (22)

and same **box order** A→G→I→D as subpattern-2,

and must claim pending square (53) in pending box D (and erase pending P).

(53) zaps (73) adding (81) zaps (88) adding (89)

Subpattern-3 = (22),(53),(81),(89)

Subpattern-4 is started in (23).

D is no longer pending, so box order may be changed to A→G→I→D

(23) zaps (73) adding (81) zaps (88) adding (78)

(23) zaps (53) while (81) zaps (61) adding (52)

Subpattern-4 = (23),(81),(78),(52)

A G I D

Back at starting box A, nothing pending, no boxes unclaimed, analysis complete.

2 009 L1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							X		
row2	8 ₁	8 ₂₃	8 ₄						
row3				X					
row4			P						X
row5	8 ₂	8 ₁₄	8 ₃						
row6					X				
row7			8 ₁₂					8 ₃₄	
row8	8 ₃₄							8 ₁₂	
row9						X			

Pattern 2.131	Box Orientation	Patterns with the same box code
3 – 3 – 2	A – C – B	none
2	D	

A	B	C
D		

Subpattern-1 is started in (12) with box order A→B→C→D

(12) zaps (16) adding (26)
(12) zaps (17) & (26) zaps (27) adding (37).
(12) zaps (42) adding (43).

Subpattern-1 = (12),(26),(37),(43)
A B C D

Subpattern-2 is started in (22) with box order A→B→C→D

(22) zaps (26) adding (16)
(22) zaps (27) & (16) zaps (17) adding (37)
(22) zaps (42) adding (43)

Subpattern-2 = (22),(16),(37),(43)
A B C D

2	131	X3	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				1 ₁				1 ₂₃	1 ₄		
row2				1 ₂				1 ₁₄	1 ₃		
row3					1 ₃₄				1 ₁₂		
row4				1 ₃₄	1 ₁₂						
row5						X					
row6											X
row7							X				
row8										X	
row9											

Pattern 2.131 continued.

A	B	C
D		

Subpattern-3 is started in (33) with box order $A \rightarrow C \rightarrow B \rightarrow D$

(33) zaps (37) adding (27) & pending (17)

(27) zaps (26) adding (16).

(33) zaps (42) adding (42).

Subpattern-3 = (33),(27),(16),(42)

A C B D

Due to *pending*,

subpattern-4 also started in (33) with same box order $A \rightarrow C \rightarrow B \rightarrow D$

subpattern-4 continued in pending square (17)

(17) zaps (16) adding (26)

(33) zaps (43) adding (42)

Subpattern-4 = (33),(17),(26),(42)

At the starting box A, no pending situation, no unclaimed boxes, we are done.

2 131 X3

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		1 ₁				1 ₂₃	1 ₄		P
row2		1 ₂				1 ₁₄	1 ₃		
row3			1 ₃₄				1 ₁₂		
row4		1 ₃₄	1 ₁₂						
row5				X					
row6									X
row7					X				
row8								X	
row9	X								

Pattern 2.140	Box Orientation	Patterns with the same box code
3 – 3 – 2	C – A – B	none
2	F	(Box orientation for 140:
		swap stacks 1 & 3, then
2	I	swap stacks 2 & 3)

A	B	C
		F
		I

Subpattern-1 is started in (11) with box order A→C→B→I→F

- (11) zaps (17) adding (28) & pending (38)
- (28) zaps (25) adding (35)
- (28) zaps (88) adding (89) zaps (49) adding (47)

Subpattern-1 = (11),(28),(35),(89),(47)
A C B I F

2	140	X4	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	2 ₁							2			
row2	2				2				2 ₁		
row3	2				2 ₁				2		
row4								2 ₁		2	
row5							X				
row6			X								
row7		X									
row8									2	2 ₁	
row9				X							

2.140, continued.

due to pending condition,

subpattern-2 started in same beginning square **(11)** as subpattern-1

subpattern-2 must have same box order **A→C→B→I→F**

subpattern-2 must claim pending square **(38)**\

(38) zaps (35) adding **(25)**

(38) zaps (88) adding **(89)** zaps (49) adding **(47)**

subpattern-2 = **(11),(38),(25),(89),(47)**

A C B I F

Subpattern-3 started in **(21)** with box order **A→B→C→F→I**

(21) zaps (25) adding **(35)**

(21) zaps (28) while (35) zaps (38) adding **(17)** zaps (47) adding **(49)**

(49) zaps (89) adding **(88)**

Subpattern-3 = **(21),(35),(17),(49),(88)**

A B C F I

2	140	X4	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			2 ₁₂						2 ₃		P
row2			2 ₃				2 ₂			2 ₁	
row3			2				2 ₁₃			2 ₂	
row4									2 ₁₂		2 ₃
row5								X			
row6				X							
row7			X								
row8										2 ₃	2 ₁₂
row9					X						

2.140, continued.

Subpattern-4 started in (31) with box order A→B→C→F→I

(31) zaps (35) adding (25)
(31) zaps (38) while (25) zaps (28) adding (17) zaps (47) adding (49)
(49) zaps (89) adding (88)

Subpattern-4 = (31),(25),(17),(49),(88)

Back at the starting box A, nothing is pending, and no squares are unclaimed, so the analysis is complete.

2	140	X4	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
			row1	2 ₁₂					2 ₃₄		
			row2	2 ₃			2 ₂₄			2 ₁	
			row3	2 ₄			2 ₁₃			2 ₂	
			row4						2 ₁₂		2 ₃₄
			row5					X			
			row6			X					
			row7		X						
			row8							2 ₃₄	2 ₁₂
			row9				X				

Pattern 2.128	Box Orientation	Patterns with the same box code
3 – 3 – 3	B – E – H	none
(Box orientation for 131: rotate 90 degrees clockwise, then swap bands 1 & 2)		

	B	
	E	
	H	

Subpattern-1 started in (14) with box order: **B→E→H**

(14) zaps (64) adding (65) and (66) *pending*

(14) zaps (94) & (65) zaps (95) adding (96)

Subpattern-1 = (14),(65),(96)

B E H

Due to pending situation, subpattern-2 must
 start in same square (14) as subpattern-1
 keep same box order **B→E→H**
 include pending square (66)
 (14) zaps (64) while (66) zaps (96) adding (95)

Subpattern-2 = (14),(66),(95)

B E H

2	128	Y1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
						5 ₁₂	5	5			
				X							
											X
			X					P			
										X	
						5	5 ₁	5 ₂			
									X		
					X						
						5	5 ₂	5 ₁			

Pattern 2.128, continued.

Subpattern-3 started in **(15)** with box order: **B→E→H**

(15) zaps (65) adding **(64)** and (66) *pending*
(15) zaps (95) while **(64)** zaps (94) adding **(96)**

Subpattern-3 = **(15),(64),(96)**
B E H

Due to pending situation, subpattern-4 must
start in same square **(15)** as subpattern-3
keep same box order **B→E→H**
include pending square **(66)**
(15) zaps (95) while **(66)** zaps (96) adding **(94)**

Subpattern-4 = **(15),(66),(94)**
B E H

2	128	Y1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row1				5 ₁₂	5 ₃₄	5			
		row2		X							
		row3									X
		row4	X					P			
		row5								X	
		row6				5 ₃	5 ₁	5 ₂₄			
		row7							X		
		row8			X						
		row9				5 ₄	5 ₂	5 ₁₃			

Pattern 2.128, continued.

Subpattern-5 starts in **(16)** with box order: **B→E→H**

(16) zaps (66) adding **(64)** and *pending* (65)

(16) zaps (96) & **(64)** zaps (94) adding (95)

Subpattern-5 = **(16),(64),(95)**

B E H

Due to pending situation, subpattern-6 must
start in same square **(16)** as subpattern-5

keep same box order **B→E→H**

include pending square (65)

(16) zaps (96) & **(65)** zaps (95) adding (94)

Subpattern-6 = **(16),(65),(94)**

B E H

2	128	Y1	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row1				5 ₁₂	5 ₃₄	5 ₅₆			
		row2		X							
		row3									X
		row4	X					P			
		row5								X	
		row6				5 ₃₅	5 ₁₆	5 ₂₄			
		row7							X		
		row8			X						
		row9				5 ₄₆	5 ₂₅	5 ₁₃			

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Chapter 3. Patterns with 3 subscripts

Pattern 3.008	Box Orientation	Patterns with the same box code
$\begin{array}{c} 2 \\ \\ 3-2 \\ \\ 2 \end{array}$	$\begin{array}{c} B \\ \\ I-C \\ \\ G \end{array}$	none

	B	C
G		I

Box order: I→G→C→B

Subpattern-1 is begun in **(87)** zaps (81) adding **(91)**
(87) zaps (37) adding **(19)** zaps (14) adding **(34)**

Subpattern-1 = **(87),(91),(19),(43)**
I G C B

3	008	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A2	row1				9					9 ₁
	row2		X							
	row3				9 ₁			9		
	row4					X				
	row5								X	
	row6			X						
	row7						X			
	row8	9						9 ₁		9
	row9	9 ₁								9

Pattern 3.008, continued.

	B	C
G		I

Box order: I→G→C→B

Subpattern-2 begins in (89) zapping (81) adding (91)
(89) zaps (19) adding (37) zaps (34) adding (14)
Subpattern-2 = (89),(91),(37),(14)
I G C B

Subpattern-3 begins in (99) zaps (91) adding (81)
(99) zaps (19) adding (37) zaps (34) adding (14)
Subpattern-3 = (99),(81),(37),(14)
I G C B

At the starting box, nothing pending, nothing unclaimed, analysis complete

3	008	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A2	row1				9 ₂₃					9 ₁
	row2		X							
	row3				9 ₁			9 ₂₃		
	row4					X				
	row5								X	
	row6			X						
	row7						X			
	row8	9 ₃						9 ₁		9 ₂
	row9	9 ₁₂								9 ₃

Pattern 3.031	Box Orientation	Patterns with the same box code
3 – 3 – 2	D – E – F	none
2	G	

D	E	F
G		

Subpattern-1 starts in (51) with box order **D→F→E→G**

(51) zaps (59) adding (69).
(51) zaps (56) & (69) zaps (66) adding (46)
(51) zaps (81) adding (82)

Subpattern-1 = (51),(69),(46),(82)
 D F E G

3 A8	031	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1							X		
	row2				X					
	row3			X						
	row4	1					1 ₁			
	row5	1 ₁	1				1			1
	row6						1			1 ₁
	row7					X				
	row8	1	1 ₁							
	row9								X	

Pattern 3.031, continued.

D	E	F
G		

Subpattern-2 starts in (52) with box order **D→F→E→G**

(52) zaps (59) adding (69)
(52) zaps (56) & (69) zaps (66) adding (46) &
(52) zaps (82) adding (81)

Subpattern-2 = (52),(69),(46),(81)
 D F E G

3 A8	031	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1							X		
	row2				X					
	row3			X						
	row4	1					1 ₁₂			
	row5	1 ₁	1 ₂				1			1
	row6						1			1 ₁₂
	row7					X				
	row8	1 ₂	1 ₁							
	row9								X	

Pattern 3.031, continued.

D	E	F
G		

Subpattern-3 starts in (41) with box order **D→F→E→G**

(41) zaps (46) adding (56) and pending (66)

(56) zaps (59) adding (69)

(41) zaps (81) adding (82)

Subpattern-3 = (41),(56),(69),(82)

3	031	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A8	row1							X		
	row2				X					
	row3			X						
	row4	1 ₃					1 ₁₂			
	row5	1 ₁	1 ₂				1 ₃			1
	row6				P		1			1 ₁₂₃
	row7					X				
	row8	1 ₂	1 ₁₃							
	row9								X	

Pattern 3.031, continued.

D	E	F
G		

Due to pending situation

subpattern-4 starts in same beginning square **(41)** as subpattern-2

subpattern-4 must follow same squares between starting and pending squares

subpattern-4 must include pending square **(66)**

(66) zaps (69) adding **(59)**

(41) zaps (81) adding **(82)**

Subpattern-4 = **(41),(66),(59),(82)**

D F E G

Back at the starting box **D**, nothing is left pending and no squares remain unclaimed, so the pattern analysis is complete.

3	031	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A8	row1							X		
	row2				X					
	row3			X						
	row4	1 ₃₄					1 ₁₂			
	row5	1 ₁	1 ₂				1 ₃			1 ₄
	row6				1		1 ₄			1 ₁₂₃
	row7					X				
	row8	1 ₂	1 ₁₃₄							
	row9							X		

Pattern 3.011	Box Orientation	Patterns with the same box code
2 3-3-2 2	C G-D-A E	020

A		C
D	E	
G		

Subpattern-1 is started in (91) with box order: **G→D→E→A→C**

(91) zaps (41) & (51) adding (43) zaps (44) adding (54)

(91) zaps (11) adding (32) zaps (39) adding (19)

Subpattern-1 = (91),(43),(54),(32),(19)

G D E A C

3	011	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A4	row1	8								8 ₁
	row2					X				
	row3		8 ₁							8
	row4	8		8 ₁	8					
	row5	8			8 ₁					
	row6								X	
	row7					X				
	row8							X		
	row9	8 ₁	8	8						

Pattern 3.011 continued.

A		C
D	E	
G		

Subpattern-2 is started in (92) with box order **G→A→C→D→E**

(92) zaps (32) adding (11) zaps (19) adding (39)
(11) zaps (41) & (51) adding (43) zaps (44) adding (54)

Subpattern-2 = (92),(11),(39),(43),(54)
 G A C D E

3 A4	011	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1	8 ₂								8 ₁
	row2						X			
	row3		8 ₁							8 ₂
	row4	8		8 ₁₂	8					
	row5	8			8 ₁₂					
	row6								X	
	row7					X				
	row8							X		
	row9	8 ₁	8 ₂	8						

Pattern 3.011 continued.

A		C
D	E	
G		

Subpattern-3 is started in (93) with box order **G→D→E→A→C**

(93) zaps (43) adding (41) and pending (51)
(41) zaps (44) adding (54)
(41) zaps (11) adding (32) zaps (39) adding (19)

Subpattern-3 = (93),(41),(54),(32),(19)
 G D E A C

3		011	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A4		row1	8 ₂								8 ₁₃
		row2						X			
		row3		8 ₁₃							8 ₂
		row4	8 ₃		8 ₁₂	8					
		row5	8			8 ₁₂₃					
		row6		P						X	
		row7					X				
		row8							X		
		row9	8 ₁	8 ₂	8 ₃						

Pattern 3.011 continued.

A		C
D	E	
G		

Due to pending situation, subpattern-4 must
be started in same square **(93)** as subpattern-3
follow same squares between starting & pending
include pending square **(51)**

(51) zaps (54) adding **(44)**
(51) zaps (11) adding **(32)** zaps (39) adding **(19)**

Subpattern-4 = **(93),(51),(44),(32),(19)**
 G D E A C

Back at the starting box G, no pending situation exists, and no squares are unclaimed, so
the analysis is complete.

3 A4	011	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1	8 ₂								8 ₁₃₄
	row2						X			
	row3		8 ₁₃₄							8 ₂
	row4	8 ₃		8 ₁₂	8 ₄					
	row5	8 ₄			8 ₁₂₃					
	row6		P						X	
	row7					X				
	row8							X		
	row9	8 ₁	8 ₂	8 ₃₄						

Pattern 3.033 Box Orientation Patterns with the same box code

$\begin{array}{c} 2 \\ \\ 3-3-2 \\ \\ 2 \end{array}$	$\begin{array}{c} E \\ \\ C-F-I \\ \\ A \end{array}$	none
--	--	-------------

A		C
	E	F
		I

Subpattern-1 is started in (27) with box order C→A→I→F→E

(27) zaps (22) adding (32)

(27) zaps (97) adding (98)

(27) zaps (67) and (98) zaps (48) adding (69) zaps (65) adding (45)

Subpattern-1 = (27),(32),(98),(69),(45)

		C A I F E								
3 033		col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
G3	row1				X					
	row2		8					8 ₁		8
	row3		8 ₁						8	
	row4					8 ₁			8	
	row5			X						
	row6					8		8		8 ₁
	row7	X								
	row8						X			
	row9							8	8 ₁	

Pattern 3.033, continued.

A		C
	E	F
		I

Subpattern-2 is started in (38) with box order C→A→I→F→E

(38) zaps (32) adding (22)
(38) zaps (98) adding (97)
(38) zaps (48) and (97) zaps (67) adding (69) zaps (65) adding (45)

Subpattern-2 = (38),(22),(97),(69),(45)
 C A I F E

3 G3	033	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1				X					
	row2		8 ₂					8 ₁		8
	row3		8 ₁						8 ₂	
	row4					8 ₁₂			8	
	row5			X						
	row6					8		8		8 ₁₂
	row7	X								
	row8						X			
	row9							8 ₂	8 ₁	

Pattern 3.033, continued.

A		C
	E	F
		I

Subpattern-3 is started in (29) with box order C→A→F→E→I

- (29) zaps (22) adding (32)
- (29) zaps (69) adding (48) and pending (67)
- (48) zaps (45) adding (65)
- (48) zaps (98) adding (97)

Subpattern-3 = (29),(32),(48),(65),(97)
 C A F E I

3 G3	033	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1				X					
	row2		8 ₂					8 ₁		8 ₃
	row3		8 ₁₃						8 ₂	
	row4					8 ₁₂			8 ₃	
	row5			X				P		
	row6					8 ₃		8		8 ₁₂
	row7	X								
	row8						X			
	row9							8 ₂₃	8 ₁	

Pattern 3.033, continued.

A		C
	E	F
		I

Due to the pending situation

subpattern-4 must start in the same square **(29)** as subpattern-3

subpattern-4 must use same squares between starting and ending as subpattern-3

subpattern-4 must include the pending square **(67)**

(29) zaps (22) adding **(32)**

(67) zaps (65) adding **(45)**

(67) zaps (97) adding **(98)**

Subpattern-4 = **(29),(32),(67),(45),(98)**

C A F E I

Back at the starting box C, there is no longer a pending condition, and no squares in any of the boxes are unclaimed. The analysis is complete.

3 G3	033	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1				X					
	row2		8 ₂					8 ₁		8 ₃₄
	row3		8 ₁₃₄						8 ₂	
	row4					8 ₁₂₄			8 ₃	
	row5			X				P		
	row6					8 ₃		8 ₄		8 ₁₂
	row7	X								
	row8						X			
	row9							8 ₂₃	8 ₁₄	

Pattern 3.024	Box Orientation	Patterns with the same box code
3 - 2 - 2	G - I - H	none
2 - 3	D - F	
2	C	

A	B	C
D	E	F
G	H	I

Subpattern-1 starts in **(68)** with box order **F→C→I→H→D→G**

(68) zaps (18) adding **(19)**
(68) zaps (88) adding **(77)** zaps (75) adding **(95)**
(68) zaps (62) adding **(51)** zaps (71) & (91) adding **(82)**

Subpattern-1 = **(68),(19),(77),(95),(51),(82)**
F C I H D G

3	024	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B2	row1								1	1 ₁
	row2			X						
	row3						X			
	row4				X					
	row5	1 ₁						1		
	row6		1						1 ₁	1
	row7	1				1		1 ₁		
	row8		1 ₁						1	
	row9	1				1 ₁				

Pattern 3.024, continued

A	B	C
D	E	F
G	H	I

Subpattern-2 starts in **(69)** with box order **F→C→I→H→D→G**

(69) zaps (19) adding **(18)** zaps (88) adding **(77)** zaps (75) adding **(95)**
(69) zaps (62) adding **(51)** zaps (71) & (91) adding **(82)**

Subpattern-2 = **(69),(18),(77),(95),(51),(82)**

F C I H D G

3	024	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B2	row1								1 ₂	1 ₁
	row2			X						
	row3						X			
	row4				X					
	row5	1 ₁₂						1		
	row6		1 ₁						1 ₁	1 ₂
	row7	1				1		1 ₁₂		
	row8		1 ₁₂						1	
	row9	1				1 ₁₂				

Pattern 3.024, continued

		C
D		F
G	H	I

Subpattern-3 starts in **(57)** with box order **F→I→C→D→G→H**

(57) zaps **(77)** adding **(88)** zapping **(18)** adding **(19)**

(57) zaps **(51)** adding **(62)** zapping **(82)** adding **(71)** and pending **(91)**

(71) zaps **(75)** adding **(95)**

Subpattern-3 = **(57),(88),(19),(62),(71),(95)**

F I C D G H

3	024	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B2	row1								1 ₂	1 ₁₃
	row2			X						
	row3						X			
	row4				X					
	row5	1 ₁₂						1 ₃		
	row6		1 ₃						1 ₁	1 ₂
	row7	1 ₃				1		1 ₁₂		
	row8		1 ₁₂						1 ₃	
	row9	1		P		1 ₁₂₃				

Pattern 3.024, continued

		C
D		F
G	H	I

Due to pending condition, subpattern-4 must
start in the same square (57) as subpattern-3
and share the same squares, (88), (19) and (66) with subpattern-3

(91) zaps (95) adding (75)

Subpattern-4 = (57),(88),(19),(66),(91),(75)
F I C D G H

3	024	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B2	row1								1 ₂	1 ₁₃₄
	row2			X						
	row3						X			
	row4				X					
	row5	1 ₁₂						1 ₃₄		
	row6		1 ₃₄						1 ₁	1 ₂
	row7	1 ₃				1 ₄		1 ₁₂		
	row8		1 ₁₂						1 ₃₄	
	row9	1 ₄		P		1 ₁₂₃				

Pattern 3.029	Box Orientation	Patterns with the same box code
3 – 3 – 2	C – A – B	031, 043, 044.
2	I	

A	B	C
		I

→	→	↓
		•

Box order throughout: A→B→C→I

Subpattern-1 starts in (13)

(13) zaps (15) adding (25)
(13) zaps (19) and (25) zaps (28) adding (38) zaps (78) adding (79)

Subpattern-1 = (13),(25),(38),(79)
A B C I

3	029	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B3	row1			2 ₁		2				2
	row2			2		2 ₁			2	
	row3			2					2 ₁	
	row4							X		
	row5				X					
	row6		X							
	row7								2	2 ₁
	row8	X					X			
	row9									

Pattern 3.029, continued.

A	B	C
D	E	F
G	H	I

→	→	↓
		•

Box order throughout: A→B→C→I

Subpattern-2 starts in (23) zaps (25) adding (15)
(23) zaps (28) and (15) zaps (19) adding (38) zaps (78) adding (79)

Subpattern-2 = (23),(15),(38),(79)
A B C I

3	029	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B3	row1			2 ₁		2 ₂				2
	row2			2 ₂		2 ₁			2	
	row3			2					2 ₁₂	
	row4							X		
	row5				X					
	row6		X							
	row7								2	2 ₁₂
	row8	X					X			
	row9									

Pattern 3.029, continued.

A	B	C
		I

→	→	↓
		•

Box order throughout: A→B→C→I

Subpattern-3 starts in (33) zaps row 3 of box B adding (25) and pending (15)
(33) zaps (38) and (25) zaps (28) adding (19) zaps (79) adding (78)

Subpattern-3 = (33),(25),(19),(78)
A B C I

3 B3	029	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1			2 ₁		2 ₂				2 ₃
	row2			2 ₂		2 ₁₃			2	
	row3			2 ₃			P		2 ₁₂	
	row4							X		
	row5				X					
	row6		X							
	row7								2 ₃	2 ₁₂
	row8	X					X			
	row9									

Pattern 3.029, continued.

Box order throughout: **A→B→C→I**

Due to pending situation in **B**, subpattern-4 must
begin in same starting square **(33)** as subpattern=3
include pending square **(15)** (and erase pending P)

(33) zaps (38) and **(15)** zaps (19) adding **(28)** zaps (78) adding **(79)**

Subpattern-4 = **(33),(15),(28),(79)**
A B C I

Back at starting box, nothing pending, no unclaimed squares, analysis complete.

3
B3

029

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			2 ₁		2 ₂₄				2 ₃
row2			2 ₂		2 ₁₃			2 ₄	
row3			2 ₃₄			P		2 ₁₂	
row4							X		
row5				X					
row6		X							
row7								2 ₃	2 ₁₂₄
row8	X					X			
row9									

Pattern 3.009	Box Orientation	Patterns with the same box code
<pre> 2 3-3 2 </pre>	<pre> F H-I B </pre>	010, 015, 018, 035, 037, 039, 041, 047, 050, 051

	B	
		F
	H	I

Box order: H→I→F→B

Subpattern-1 starts in **(74)** zaps (77) & (79) adding **(97)** zaps(47) adding **(49)**
(74) zaps (14) adding **(15)**

Subpattern-1 = **(74),(97),(49),(15)**
H I F B

3	009	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B4	row1				1	1 ₁				
	row2	X								
	row3								X	
	row4							1		1 ₁
	row5						X			
	row6		X							
	row7				1 ₁			1		1
	row8			X						
	row9				1	1		1 ₁		

Pattern 3.009, continued.

	B	
		F
	H	I

Box order: H→I→F→B

Subpattern-2 is started in **(94)** zaps (97) adding **(77)** & pending **(79)**
(77) zaps (47) adding **(49)**
(94) zaps (14) adding **(15)**

Subpattern-2 = **(94),(77),(49),(15)**
H I F B

3 B4	009	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1				1	1 ₁₂				
	row2	X								
	row3								X	
	row4							1		1 ₁₂
	row5						X			
	row6		X							
	row7				1 ₁			1 ₂		1
	row8			X						
	row9				1 ₂	1		1 ₁		P

Pattern 3.009, continued.

	B	
		F
	H	I

Box order: H→I→F→B

Due to pending condition, subpattern-3 must
begin in same square **(94)** as subpattern-2
include pending square **(77)**

(77) zaps (47) adding **(49)**

(94) zaps (14) adding **(15)**

Subpattern-3 = **(94),(77),(49),(15)**
H I F B

3 B4	009	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1				1	1 ₁₂₃				
	row2	X								
	row3								X	
	row4							1 ₃		1 ₁₂
	row5						X			
	row6		X							
	row7				1 ₁			1 ₂		1 ₃
	row8			X						
	row9				1 ₂₃	1		1 ₁		≠

Pattern 3.009, continued.

	B	
		F
	H	I

Box order: H→I→F→B throughout.

Subpattern-4 starts in **(95)** zaps (97) adding **(77)** and pending **(79)**
(77) zaps (47) adding **(49)**
(95) zaps (15) adding **(14)**

Subpattern-4 = **(95),(77),(49),(14)**
H I F B

3		009	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B4	row1				1 ₄	1 ₁₂₃					
	row2	X									
	row3									X	
	row4								1 ₃		1 ₁₂₄
	row5							X			
	row6		X								
	row7				1 ₁				1 ₂₄		1 ₃
	row8			X							
	row9				1 ₂₃	1 ₄			1 ₁		P

Pattern 3.009, continued.

	B	
		F
	H	I

Box order: H→I→F→B throughout.

Due to pending condition, subpattern-5 must
start in same beginning square **(95)** as subpattern-4
include pending square **(79)**

(79) zaps (49) adding **(47)**

(95) zaps (15) adding **(14)**

Subpattern-5 = **(95),(79),(47),(14)**

H I F B

Back at the starting box H, nothing remains pending, and no squares are unclaimed, so the analysis is complete.

3	009	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B4	row1				1 ₄₅	1 ₁₂₃				
	row2	X								
	row3								X	
	row4							1 ₃₅		1 ₁₂₄
	row5						X			
	row6		X							
	row7				1 ₁			1 ₂₄		1 ₃₅
	row8			X						
	row9				1 ₂₃	1 ₄₅		1 ₁		≠

Pattern 3.045	Box Orientation	Patterns with the same box code
3 - 2 - 2	E - H - B	046
2 - 3	I - F	

A	B	C
D	E	F
G	H	I

Box order: E→F→I→H→B

Subpattern-1 is started in (45) zaps (48) adding (58) and pending (59)
(58) zaps (78) adding (79)
(45) zaps (85) adding (86)
(45) zaps (35) adding (34)

Subpattern-1 = (45),(58),(79),(86),(34)
E F I H B

3	045	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B5	row1							X		
	row2		X							
	row3				4 ₁	4				
	row4					4 ₁			4	
	row5				4		4		4 ₁	4
	row6			X				P		
	row7								4	4 ₁
	row8					4	4 ₁			
	row9	X								

Pattern 3.045, continued.

A	B	C
D	E	F
G	H	I

Box order: E→F→I→H→B

Due to pending situation, subpattern-2 must
begin in same square (45) as subpattern-1
include pending square (59)

(59) zaps (79) adding (78)
(45) zaps (85) adding (86)
(45) zaps (35) adding (34)

Subpattern-2 = (45),(59),(78),(86),(34)
 E F I H B

3 B5	045	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1							X		
	row2		X							
	row3				4 ₁₂	4				
	row4					4 ₁₂			4	
	row5				4		4		4 ₁	4 ₂
	row6			X				≠		
	row7								4 ₂	4 ₁
	row8					4	4 ₁₂			
	row9	X								

Pattern 3.045, continued.

A	B	C
D	E	F
G	H	I

Box order: E→F→I→H→B

Subpattern-3 is started in (56) zaps (58) & (59) adding (48) zaps (78) adding (79) (56) zaps (86) adding (85) zaps (35) adding (34)

Subpattern-3 = (56),(48),(79),(85),(34)

E F I H B

3	045	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B5	row1							X		
	row2		X							
	row3				4 ₁₂₃	4				
	row4					4 ₁₂			4 ₃	
	row5				4		4 ₃		4 ₁	4 ₂
	row6			X						
	row7								4 ₂	4 ₁₃
	row8					4 ₃	4 ₁₂			
	row9	X								

Pattern 3.045, continued.

A	B	C
D	E	F
G	H	I

Subpattern-4 is started in **(54)** with box order **E→F→I→B→H**

(54) zaps (58) & (59) adding **(48)** zaps (78) adding **(79)**

(54) zaps (34) adding **(35)** zaps (85) adding **(86)**

Subpattern-4 = **(54),(48),(79),(35),(86)**

E F I B H

Back at the starting box E, nothing remains pending, and no squares are unclaimed, so pattern analysis is complete.

3	045	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B5	row1							X		
	row2		X							
	row3				4 ₁₂₃	4 ₄				
	row4					4 ₁₂			4 ₃₄	
	row5				4 ₄		4 ₃		4 ₁	4 ₂
	row6			X						
	row7								4 ₂	4 ₁₃₄
	row8					4 ₃	4 ₁₂₄			
	row9	X								

Pattern 3.042	Box Orientation	Patterns with the same box code
2 3-3-2 2	D I-C-F A	none

A		C
D		F
		I

Subpattern-1 begins in **(88)** with box order **I→F→C→A→D**

(88) zaps (58) adding **(59)** zaps (39) & (19) adding **(37)** zaps (33) adding **(11)** zaps (61) adding **(63)**

Subpattern-1 = **(88),(59),(37),(11),(63)**
I F C A D

3
G6

042	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	7 ₁								7
row2						X			
row3			7				7 ₁		7
row4				X					
row5								7	7 ₁
row6	7		7 ₁						
row7					X				
row8							7	7 ₁	7
row9		X							

Pattern 3.042, continued.

A		C
D		F
		I

Subpattern-2 begins in (89) with box order I→F→C→A→D

(89) zaps (59) adding (58)

(89) zaps (39) & (19) adding (37) zaps (33) adding (11) zaps (61) adding (63)

Subpattern-2 = (89),(58),(37),(11),(63)

I F C A D

3
G6

042	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	7 ₁₂								7
row2						X			
row3			7				7 ₁₂		7
row4				X					
row5								7 ₂	7 ₁
row6	7		7 ₁₂						
row7					X				
row8							7	7 ₁	7 ₂
row9		X							

Pattern 3.042, continued.

A		C
D		F
		I

Subpattern-3 begins in (87) with box order **I→C→F→A→D**

(87) zaps (37) adding (39) & pending (19)
(39) zaps (59) adding (58)
(39) zaps (33) adding (11) zaps (61) adding (63)

Subpattern-3 = (87),(39),(58),(11),(63)
 I F C A D

3 G6	042	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1	7 ₁₂₃						P		7
	row2						X			
	row3			7				7 ₁₂		7 ₃
	row4				X					
	row5								7 ₂₃	7 ₁
	row6	7		7 ₁₂₃						
	row7					X				
	row8							7 ₃	7 ₁	7 ₂
	row9		X							

Pattern 3.042, continued.

A		C
D		F
		I

Subpattern-3 begins in **(87)** with box order **I→C→F→A→D**

Due to pending condition in C, subpattern-4 must
begin in same square **(87)** and follow same squares as subpattern-3
until pending box, where it must include pending square **(19)**

(19) zaps (59) adding **(58)**

(19) zaps (11) adding **(33)** zaps (63) adding **(61)**

Subpattern-4 = **(87),(19),(58),(33),(61)**

I C F A D

Back at the starting box I, nothing remains pending and no boxes remain unclaimed.
The analysis is complete.

3 G6	042	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1	7 ₁₂₃						P		7 ₄
	row2						X			
	row3			7 ₄				7 ₁₂		7 ₃
	row4				X					
	row5								7 ₂₃₄	7 ₁
	row6	7 ₄		7 ₁₂₃						
	row7					X				
	row8							7 ₃₄	7 ₁	7 ₂
	row9		X							

Pattern 3.038	Box Orientation	Patterns with the same box code
3 - 3 - 2	C - B - A	none
2 - 2	H - I	

A	B	C
	H	I

Subpattern-1 is started in (39) with box order C→I→H→B→A

(39) zaps (79) adding (98) zaps (96) adding (76)
(39) zaps (35) adding (25) and pending (15)
(25) zaps (21) adding (11)

Subpattern-1 = (39),(98),(76),(25),(11)
C I H B A

3	038	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
G4	row1	4 ₁				4			4	4
	row2	4				4 ₁				
	row3					4				4 ₁
	row4				X					
	row5		X							
	row6							X		
	row7						4 ₁			4
	row8			X						
	row9						4		4 ₁	

Pattern 3.038, continued.

A	B	C
	H	I

Due to pending condition in box B, subpattern-2 must
start in same square **(39)** as subpattern-1
share same squares **(98)** & **(96)** in boxes leading up to pending square
include pending square **(15)**

(15) zaps (11 adding **(21)**)

Subpattern-2 = **(39),(98),(96),(15),(21)**
 C I H B A

3 G4	038	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1	4 ₁				4 ₂			4	4
	row2	4 ₂				4 ₁				
	row3					4				4 ₁₂
	row4				X					
	row5		X							
	row6							X		
	row7						4 ₁₂			4
	row8			X						
	row9						4		4 ₁₂	

Pattern 3.038, continued.

A	B	C
	H	I

Subpattern-3 is started in **(18)** with box order **C→I→H→A→B**

(18) zaps (98) adding **(79)** zaps (76) adding **(96)**

(18) zaps (11) adding **(21)**

(21) zaps (25) and **(18)** zaps (15) adding (35)

Subpattern-3 = **(18),(79),(96),(21),(35)**

C I H A B

3 G4	038	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1	4 ₁				4 ₂			4 ₃	4
	row2	4 ₂₃				4 ₁				
	row3					4 ₃				4 ₁₂
	row4				X					
	row5		X							
	row6							X		
	row7						4 ₁₂			4 ₃
	row8			X						
	row9						4 ₃		4 ₁₂	

Pattern 3.038, continued.

A	B	C
	H	I

Subpattern-4 is started in **(19)** with box order **C→I→H→A→B**

(19) zaps (79) adding **(98)** zaps (96) adding **(76)**

(19) zaps (11) adding **(21)**

(19) zaps (15) and **(21)** zaps (25) adding (35)

Subpattern-4 = **(19),(98),(76),(21),(35)**
 C I H A B

Back at the starting box C, nothing is pending and no squares are unclaimed,
so the pattern analysis is complete.

3
G4

038	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	4 ₁				4 ₂			4 ₃	4 ₄
row2	4 ₂₃₄				4 ₁				
row3					4 ₃₄				4 ₁₂
row4				X					
row5		X							
row6							X		
row7						4 ₁₂₄			4 ₃
row8			X						
row9						4 ₃		4 ₁₂₄	

Pattern 3.005	Box Orientation	Patterns with the same box code
$\begin{array}{c} 2-2 \\ \\ 3-3 \\ \\ 2 \end{array}$	$\begin{array}{c} F-C \\ \\ H-E \\ \\ G \end{array}$	none

		C
	E	F
G	H	

Subpattern-1 begins in **(44)** with box order **E→F→C→H→G**

(44) zaps (47) adding **(69)** zaps (39) adding **(37)**
(44) zaps (74) & (84) adding **(76)** zaps (72) adding **(82)**

Subpattern-1 = **(44),(69),(37),(76),(82)**
E F C H G

3	005	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A5	row1					X				
	row2			X						
	row3							5 ₁		5
	row4				5 ₁			5		
	row5	X								
	row6				5		5			5 ₁
	row7		5		5		5 ₁			
	row8		5 ₁		5					
	row9								X	

Pattern 3.005

		C
	E	F
G	H	

Subpattern-2 begins in **(64)** with box order **E→F→C→H→G**

(64) zaps (69) adding **(47)** zapping (37) adding **(39)**
(64) zaps (74) & (84) adding **(76)** zaps (72) adding **(82)**

Subpattern-2 = **(64),(47),(39),(76),(82)**

E F C H G

3	005	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A5	row1					X				
	row2			X						
	row3							5 ₁		5 ₂
	row4				5 ₁			5 ₂		
	row5	X								
	row6				5 ₂		5			5 ₁
	row7		5		5		5 ₁₂			
	row8		5 ₁₂		5					
	row9								X	

Pattern 3.005

		C
	E	F
G	H	

Subpattern-3 begins in **(66)** with box order **E→F→C→H→G**

(66) zaps (69) adding **(47)** zaps (37) adding **(39)**

(66) zaps (76) adding **(74)** and pending **(84)**

(74) zaps (72) adding **(82)**

Subpattern-3 = **(66),(47),(39),(74),(82)**

E F C H G

3	005	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A5	row1					X				
	row2			X						
	row3							5 ₁		5 ₂₃
	row4				5 ₁			5 ₂₃		
	row5	X								
	row6				5 ₂		5 ₃			5 ₁
	row7		5		5 ₃		5 ₁₂			
	row8		5 ₁₂₃		5					
	row9					P			X	

Pattern 3.005

		C
	E	F
G	H	

Due to pending condition in box H, subpattern-4 must
begin in same square **(66)** as subpattern-3
and share same squares **(47)** and **(39)** as subpattern-3 until pending box
include pending square **(84)**

(84) zaps (82) adding **(72)**

Subpattern-4 = **(66),(47),(39),(84),(72)**
 E F C H G

Back at the starting box E, nothing is pending, and no squares are unclaimed, so the analysis is complete.

3		005	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A5		row1					X				
		row2			X						
		row3							5 ₁		5 ₂₃₄
		row4				5 ₁			5 ₂₃₄		
		row5	X								
		row6				5 ₂		5 ₃₄			5 ₁
		row7		5 ₄		5 ₃		5 ₁₂			
		row8		5 ₁₂₃		5 ₄					
		row9					≠			X	

Pattern 3.035	Box Orientation	Patterns with the same box code
2 3-3 2	C E-F H	038

		C
	E	F
	H	

We'll start subpattern-1 in (45) of box E with box order E→H→F→C

(45) zaps (47) and (49) adding (69) zaps (39) adding (17)
(45) zaps (85) adding (96)

Subpattern-1 = (45),(69),(17),(96)
 E H F C

3
B4

035	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							2 ₁		2
row2	X								
row3				X					
row4					2 ₁	2	2		2
row5			X						
row6					2				2 ₁
row7								X	
row8					2	2 ₁			
row9		X							

Pattern 3.035, continued.

		C
	E	F
	H	

We'll start subpattern-2 in (46) of box E with box order E→H→F→C

(46) zaps (47) & (49) adding (69) zaps (19) adding (17)
(46) zaps (86) adding (85)

Subpattern-2 = (46),(69),(17),(85)
 E H F C

3	035	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B4	row1							2 ₁₂		2
	row2	X								
	row3				X					
	row4					2 ₁	2 ₂	2		2
	row5			X						
	row6					2				2 ₁₂
	row7								X	
	row8					2 ₂	2 ₁			
	row9		X							

Pattern 3.035, continued.

		C
	E	F
	H	

We'll start subpattern-3 in (65) of box E with box order $E \rightarrow H \rightarrow F \rightarrow C$

(65) zaps (85) adding (86)
(65) zaps (69) adding (47) and pending (49)
(47) zaps (17) adding (19)

Subpattern-3 = (65),(86),(47),(19)
 E H F C

3 B4	035	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1							2 ₁₂		2 ₃
	row2	X								
	row3				X					
	row4					2 ₁	2 ₂	2 ₃		2
	row5			X					P	
	row6					2 ₃				2 ₁₂
	row7								X	
	row8					2 ₂	2 ₁₃			
	row9		X							

Pattern 3.035, continued.

		C
	E	F
	H	

Due to pending condition in box **F**, subpattern-4 must
 begin in same starting square **(65)** as subpattern-3
 follow same squares as subpattern-3 until pending box is reached
 include pending square **(49)**

(49) zaps (19) adding **(17)**

(65) zaps (85) adding **(86)**

Subpattern-4 = **(65),(86),(49),(17)**

E H F C

Back at the starting box E, nothing remains pending, and no squares are unclaimed, so the analysis is complete.

3	035	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B4	row1							2 ₁₂₄		2 ₃
	row2	X								
	row3				X					
	row4					2 ₁	2 ₂	2 ₃		2 ₄
	row5			X					≠	
	row6					2 ₃₄				2 ₁₂
	row7								X	
	row8					2 ₂	2 ₁₃₄			
	row9		X							

Pattern 3.012	Box Orientation	Patterns with the same box code
2 2-2 3-3 2	I B-C D-E G	none

	B	C
D	E	
G		I

Subpattern-1 begins in (54) with box order E→D→G→B→C→I

(54) zaps (51) adding (61) and pending (62)

(61) zaps (71) adding (72)

(54) zaps (24) adding (36) zaps (38) adding (29) zaps (99) adding (98)

Subpattern-1 = (54),(61),(72),(36),(29),(98)

E D G B C I

3	012	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A6	row1			X						
	row2				8					8 ₁
	row3						8 ₁		8	
	row4		P					X		
	row5	8			8 ₁		8			
	row6	8 ₁	8		8					
	row7	8	8 ₁							
	row8					X				
	row9								8 ₁	8

Pattern 3.012, continued.

	B	C
D	E	
G		I

Due to pending condition in D, subpattern-2 must
begin in same starting square **(54)** as subpattern-1
follow same squares as subpattern-1 until pending box
include pending square **(62)**

(62) zaps (72) adding **(71)**
(54) zaps (24) adding **(36)** zaps (38) adding **(29)** zaps (99) adding **(98)**

Subpattern-2 = **(54),(62),(71),(36),(29),(98)**
E D G B C I

3	012	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A6	row1			X						
	row2				8					8 ₁₂
	row3						8 ₁₂		8	
	row4		P					X		
	row5	8			8 ₁₂		8			
	row6	8 ₁	8 ₂		8					
	row7	8 ₂	8 ₁							
	row8					X				
	row9								8 ₁₂	8

Pattern 3.012, continued.

	B	C
D	E	
G		I

Subpattern-3 begins in **(56)** with box order **E→D→G→B→C→I**

(56) zaps (51) adding **(61)** and pending **(62)**
(61) zaps (71) adding **(72)**
(56) zaps (36) adding **(24)** zaps (29) adding **(38)** zaps (98) adding **(99)**

Subpattern-3 = **(56),(62),(72),(24),(38),(99)**
E D G B C I

3 A6	012	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1			X						
	row2				8 ₃					8 ₁₂
	row3						8 ₁₂		8 ₃	
	row4		P					X		
	row5	8			8 ₁₂		8 ₃			
	row6	8 ₁₃	8 ₂		8					
	row7	8 ₂	8 ₁₃							
	row8					X				
	row9								8 ₁₂	8 ₃

Pattern 3.012, continued.

	B	C
D	E	
G		I

Due to pending condition in box **D**, subpattern-4 must
start in same square **(56)** as subpattern-3
follow same squares as subpattern-3 until pending box is reached
include pending square **(62)**

(62) zaps (72) adding **(71)**
(56) zaps (36) adding **(24)** zaps (29) adding **(38)** zaps (98) adding **(99)**

Subpattern-4 = **(56),(62),(71),(24),(38),(99)**
 E D G B C I

3		012	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A6		row1			X						
		row2				8 ₃₄					8 ₁₂
		row3						8 ₁₂		8 ₃₄	
		row4		≠					X		
		row5	8			8 ₁₂		8 ₃₄			
		row6	8 ₁₃	8 ₂₄		8					
		row7	8 ₂₄	8 ₁₃							
		row8					X				
		row9								8 ₁₂	8 ₃₄

Pattern 3.012, continued.

	B	C
D	E	
G		I

Subpattern-5 begins in **(64)** with box order **E→D→G→B→C→I**

(64) zaps **(61)** & **(62)** adding **(51)** zaps **(71)** adding **(72)**
(64) zaps **(24)** adding **(36)** zaps **(38)** adding **(29)** zaps **(99)** adding **(98)**

Subpattern-5 = **(64),(51),(72),(36),(29),(98)**
E D G B C I

Back at the starting box E, no box remains pending, no square remains unclaimed. The analysis is complete.

3	012	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A6	row1			X						
	row2				8 ₃₄					8 ₁₂₅
	row3						8 ₁₂₅		8 ₃₄	
	row4		P					X		
	row5	8 ₅			8 ₁₂		8 ₃₄			
	row6	8 ₁₃	8 ₂₄		8 ₅					
	row7	8 ₂₄	8 ₁₃₅							
	row8					X				
	row9								8 ₁₂₅	8 ₃₄

Pattern 3.030	Box Orientation	Patterns with the same box code
2 3-3-2 2 2	C D-F-E G H	none

		C
D	E	F
G	H	

Subpattern-1 starts in (41) with box order **D→G→E→H→F→C**

(41) zaps (71) adding (73)
(41) zaps (46) adding (64) zaps (84) adding (86)
(64) zaps (67) & (69) adding (57) zaps (37) adding (39)

Subpattern-1 = (41),(73),(64),(86),(57),(39)
 D G E H F C

3	030	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A7	row1				X					
	row2		X							
	row3							1		1 ₁
	row4	1 ₁		1			1			
	row5			1				1 ₁		
	row6				1 ₁			1		1
	row7	1		1 ₁						
	row8				1		1 ₁			
	row9								X	

Pattern 3.030, continued.

		C
D	E	F
G	H	

Subpattern-2 starts in (43) with box order **D→G→E→H→F→C**

(43) zaps (73) adding (71)
(43) zaps (46) adding (64) zaps (84) adding (86)
(64) zaps (67) & (69) adding (57) zaps (37) adding (39)

Subpattern-2 = (43),(71),(64),(86),(57),(49)
 D G E H F C

3 A7	030	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1					X				
	row2		X							
	row3							1		1 ₁₂
	row4	1 ₁		1 ₂			1			
	row5			1				1 ₁₂		
	row6				1 ₁₂			1		1
	row7	1 ₂		1 ₁						
	row8				1		1 ₁₂			
	row9								X	

Pattern 3.030, continued.

		C
D	E	F
G	H	

Subpattern-3 starts in (53) with box order **D→G→F→C→E→H**

- (53) zaps (73) adding (71)
- (53) zaps (57) adding (67) and pending (69)
- (67) zaps (64) adding (46) zaps (86) adding (84)
- (67) zaps (37) adding (39)

Subpattern-3 = (53),(71),(67),(39).(46),(84)
 D G F C E H

3 A7	030	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1					X				
	row2		X							
	row3							1		1 ₁₂₃
	row4	1 ₁		1 ₂			1 ₃			
	row5			1 ₃				1 ₁₂		
	row6				1 ₁₂			1 ₃		1
	row7	1 ₂₃		1 ₁						
	row8				1 ₃		1 ₁₂			
	row9								X	

Pattern 3.030, continued.

		C
D	E	F
G	H	

Due to pending condition in box **F**, subpattern-4 must
begin in the same starting square **(53)** as subpattern-3
follow the same square **(71)** as subpattern-3 between starting and pending box
include the pending square **(69)**

(69) zaps (39) adding **(37)**

(69) zaps (64) adding **(46)** zaps (86) adding **(84)**

Subpattern-4 = (53),(71),(69),(37),(46),(84)

D G F C E H

Back at the starting box D, no pending situation remain, and no squares are unclaimed. The analysis is complete.

3	030	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A7	row1					X				
	row2		X							
	row3							1 ₄		1 ₁₂₃
	row4	1 ₁		1 ₂			1 ₃₄			P
	row5			1 ₃₄				1 ₁₂		
	row6				1 ₁₂			1 ₃		1 ₄
	row7	1 ₂₃₄		1 ₁						
	row8				1 ₃₄		1 ₁₂			
	row9								X	

Pattern 3.061	Box Orientation	Patterns with the same box code
$\begin{array}{c} 2 \\ \\ 3-2-3 \\ \\ 2-2 \end{array}$	$\begin{array}{c} D \\ \\ A-B-C \\ \\ I-H \end{array}$	none

A	B	C
D		
	H	I

Subpattern-1 begins in (12) with box order **A→D→C→B→I→H**

- (12) zaps (42) adding (41)
- (12) zaps (15) adding (35)
- (12) zaps (17) while (35) zaps (39) adding (27)
- (27) zaps (97) adding (89) zaps (86) adding (96)

Subpattern-1 = (12),(41),(35),(27),(89),(96)
 A D C B I H

3 061	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A3	row1	8 ₁			8		8		
	row2	8					8 ₁		
	row3	8			8 ₁				8
	row4	8 ₁	8						
	row5							X	
	row6			X					
	row7		X						
	row8					8			8 ₁
	row9					8 ₁	8		

Pattern 3.061, continued.

A	B	C
D		
	H	I

Subpattern-2 begins in (22) with box order **A→D→C→B→I→H**

- (22) zaps (42) adding (41)
- (22) zaps (27) adding (17) and pending (39)
- (17) zaps (15) adding (35)
- (17) zaps (97) adding (89) zaps (86) adding (96)

Subpattern-2 = (22),(41),(17),(35),(89),(96)
A D C B I H

3 061
A3

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		8 ₁			8		8 ₂		P
row2		8 ₂					8 ₁		
row3	8				8 ₁₂				8 _P
row4	8 ₁₂	8							
row5								X	
row6				X					
row7			X						
row8						8			8 ₁₂
row9						8 ₁₂	8		

Pattern 3.061, continued.

A	B	C
D		
	H	I

Due to pending condition in C, subpattern-3 must
begin in same square **(22)** as subpattern-2
include square **(41)**
include pending square **(39)**

(39) zaps (35) adding **(15)**
(39) zaps (89) adding **(97)** zaps (96) adding **(86)**

Subpattern-3 = **(22),(41),(39),(15),(97),(86)**

3 061
A3

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		8 ₁			8 ₃		8 ₂		P
row2		8 ₂₃					8 ₁		
row3	8				8 ₁₂				8 ₃
row4	8 ₁₂₃	8							
row5								X	
row6				X					
row7			X						
row8						8 ₃			8 ₁₂
row9						8 ₁₂	8 ₃		

Pattern 3.061, continued.

A	B	C
D		
	H	I

Subpattern-4 begins in (31) with box order **A→D→B→C→I→H**

(31) zaps (41) adding (42)
(31) zaps (35) adding (15)
(31) zaps (39) and (15) zaps (17) adding (39) zaps (89) adding (97) zaps (96)
adding (86)

Subpattern-4 = (31),(42),(15),(39),(97),(86)
A D B C I H

Back at the starting box A, nothing is pending and no squares are unclaimed,
so the pattern analysis is complete.

3 061
A3

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		8 ₁			8 ₃₄		8 ₂		
row2		8 ₂₃					8 ₁₄		
row3	8 ₄				8 ₁₂				8 ₃
row4	8 ₁₂₃	8 ₄							
row5								X	
row6				X					
row7			X						
row8						8 ₃			8 ₁₂₄
row9						8 ₁₂₄	8 ₃		

Pattern 3.004	Box Orientation	Patterns with the same box code
3 - 2	G - D	024
2 - 3 - 2	I - F - C	
2	H	

		C
D		F
G	H	I

Subpattern-1 is begun in (72) with box order **G→I→H→D→F→C**

(72) zaps (78) adding (89) zaps (86) adding (96)
(72) zaps (62) adding (53) zaps (59) adding (67) and pending (68)
(67) zaps (17) adding (18)

Subpattern-1 = (72),(89),(96),(53),(67),(18)
G I H D F C

3 004	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C8	row1						2	2 ₁	
	row2				X				
	row3	X							
	row4			X			P		
	row5		2 ₁						2
	row6	2					2 ₁	2 _P	
	row7	2 ₁						2	
	row8		2			2			2 ₁
	row9		2			2 ₁			

Pattern 3.004, continued.

		C
D		F
G	H	I

Due to pending situation in **F**, subpattern-2 must
begin in same starting square **(72)** as subpattern-1
include pending square **(68)**
share same squares **(53)** as subpattern-3 between starting and pending boxes
(72) zaps (78) adding **(89)** zaps (86) adding **(96)**
(68) zaps (18) adding **(17)**

Subpattern-2 = **(72),(89),(96),(53),(68),(17)**
G I H D F C

3 C8	004	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		row1						2 ₂	2 ₁	
		row2				X				
		row3	X							
		row4				X		<u>P</u>		
		row5			2 ₁₂					2
		row6		2				2 ₁	2 ₂	
		row7		2 ₁₂					2	
		row8			2		2			2 ₁₂
		row9			2		2 ₁₂			

Pattern 3.004, continued.

		C
D		F
G	H	I

Subpattern-3 begins in (83) with box order **G→H→I→C→D→F**

(83) zaps (86) adding (96)
(83) zaps (89) adding (78) zaps (18) adding (17)
(83) zaps (53) adding (62) zaps (67) & (68) adding (59)

Subpattern-3 = (83),(96),(78),(17),(62),(59)
 G H I C D F

3 004
C8

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							2 ₂₃	2 ₁	
row2					X				
row3	X								
row4				X					
row5			2 ₁₂						2 ₃
row6		2 ₃					2 ₁	2 ₂	
row7		2 ₁₂						2 ₃	
row8			2 ₃			2			2 ₁₂
row9			2			2 ₁₂₃			

Pattern 3.004, continued.

		C
D		F
G	H	I

Subpattern-4 begins in (83) with box order **G→H→D→F→I→C**

(83) zaps (86) adding **(96)**
(83) zaps (53) adding **(62)** zaps (67) & (68) adding **(59)** zaps (89) adding **(78)**
zaps (18) adding **(17)**

Subpattern-4 = **(83),(96),(62),(59),(78),(17)**
G H D F I C

Back at the starting box G, no box is pending and no square unclaimed. The analysis is complete.

3 004
C8

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							2 ₂₃₄	2 ₁	
row2					X				
row3	X								
row4				X					
row5			2 ₁₂						2 ₃₄
row6		2 ₃₄					2 ₁	2 ₂	
row7		2 ₁₂						2 ₃₄	
row8			2 ₃			2 ₄			2 ₁₂
row9			2 ₄			2 ₁₂₃			

Pattern 3.017	Box Orientation	Patterns with the same box code
3 - 2 - 2	G - D - A	none
2 - 3	I - F	
2	E	

A		
D	E	F
G		I

Subpattern-1 begins in (71) with box order G→I→F→E→D→A

(71) zaps (77) adding (99) zaps (49) adding (57) and pending (67)
(57) zaps (54) adding (64) zaps (61) adding (42) zaps (32) adding (33)

Subpattern-1 = (71),(99),(57),(64),(42),(33)
G I F E D A

3 C9	017	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1						X			
	row2								X	
	row3		2	2 ₁						
	row4		2 ₁							2
	row5				2			2 ₁		
	row6	2			2 ₁			2 _P		P
	row7	2 ₁						2		
	row8					X				
	row9		2	2						2 ₁

Pattern 3.017, continued.

A		
D	E	F
G		I

Due to the pending situation in **F**, subpattern-2 must
begin in the same starting square **(71)** as subpattern-1
include the pending square **(67)**
follow same square **(99)** as subpattern-1 between starting and pending squares

(67) zaps (64) adding **(54)**

(67) zaps (61) adding **(42)** zaps (32) adding **(33)**

Subpattern-2 = **(71),(99),(67),(54),(42),(33)**

G I F E D A

3 C9	017	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1						X			
	row2								X	
	row3		2	2 ₁₂						
	row4		2 ₁₂							2
	row5				2 ₂			2 ₁		
	row6	2			2 ₁			2 ₂		P
	row7	2 ₁₂						2		
	row8					X				
	row9		2	2						2 ₁₂

Pattern 3.017, continued.

A		
D	E	F
G		I

Subpattern-3 begins in **(92)** with box order **G→I→F→D→C→A**

(92) zaps (99) adding **(77)** zaps(67) & (57) adding **(49)** zaps (42) adding **(61)**
(61) zaps (64) adding **(54)**
(92) zaps (32) adding **(33)**

Subpattern-3 = **(92),(77),(49),(61),(54),(33)**
G I F D C A

3 C9	017	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1						X			
	row2								X	
	row3		2	2 ₁₂₃						
	row4		2 ₁₂							2 ₃
	row5				2 ₂₃			2 ₁		
	row6	2 ₃			2 ₁			2 ₂		
	row7	2 ₁₂						2 ₃		
	row8					X				
	row9		2 ₃	2						2 ₁₂

Pattern 3.017, continued.

A		
D	E	F
G		I

Subpattern-4 begins in **(93)** with box order **G→I→F→D→C→A**

(93) zaps (99) adding **(77)** zaps (67) & (57) adding **(49)** zaps (42) adding **(61)** zaps (64)
adding **(54)**

(93) zaps (33) adding **(32)**

Subpattern-4 = **(93),(77),(49),(61),(54),(32)**

G I F D C A

Back at the starting box G, no boxes are pending and no squares are unclaimed. The analysis is complete.

3	017	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C9	row1						X			
	row2								X	
	row3		2 ₄	2 ₁₂₃						
	row4		2 ₁₂							2 ₃₄
	row5				2 ₂₃₄			2 ₁		
	row6	2 ₃₄			2 ₁			2 ₂		
	row7	2 ₁₂						2 ₃₄		
	row8					X				
	row9		2 ₃	2 ₄						2 ₁₂

Pattern 3.059	Box Orientation	Patterns with the same box code
3 - 2 - 3	D - F - E	none
2 - 3	G - I	
2	C	

		C
D	E	F
G		I

Subpattern-1 starts in (43) with box order D→G→I→F→C→E

(43) zaps (93) adding (71) zaps (77) & (78) adding (99) zaps (49) adding (68)
(68) zaps (18) adding (17)
(43) zaps (44) adding (54)

Subpattern-1 = (43),(71),(99),(68),(17),(54)
D G I F C E

3	059	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C9	row1							1 ₁	1	
	row2		X							
	row3						X			
	row4			1 ₁	1					1
	row5			1	1 ₁					
	row6	1							1 ₁	
	row7	1 ₁						1	1	
	row8					X				
	row9			1						1 ₁

Pattern 3.059 continued.

		C
D	E	F
G		I

Subpattern-2 starts in (53) with box order **D→G→I→F→C→E**

(53) zaps (93) adding (71) zaps (77) & (78) adding (99) zaps (49) adding (68)
zaps (18) adding (17)
(53) zaps (54) adding (44)

Subpattern-2 = (53),(71),(99),(68),(17),(44)
 D G I F C E

3	059	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C9	row1							1 ₁₂	1	
	row2		X							
	row3						X			
	row4			1 ₁	1 ₂					1
	row5			1 ₂	1 ₁					
	row6	1							1 ₁₂	
	row7	1 ₁₂						1	1	
	row8					X				
	row9			1						1 ₁₂

Pattern 3.059 continued.

		C
D	E	F
G		I

Subpattern-3 starts in **(61)** with box order **D→G→I→F→C→E**

(61) zaps (71) adding **(93)** zaps (99) adding **(77)** and pending **(78)**
(77) zaps (17) adding **(18)** zaps (68) adding **(49)** zaps (44) adding **(54)**

Subpattern-3 = **(61),(93),(77),(18),(49),(54)**

D G I F C E

3 C9	059	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1							1 ₁₂	1 ₃	
	row2		X							
	row3						X			
	row4			1 ₁	1 ₂					1 ₃
	row5			1 ₂	1 ₁₃					
	row6	1 ₃							1 ₁₂	
	row7	1 ₁₂						1 ₃	1 _P	
	row8					X				
	row9			1 ₃				P		1 ₁₂

Pattern 3.059 continued.

		C
D	E	F
G		I

Due to the pending condition in I, subpattern-4 must
 begin in the same starting square **(61)** as subpattern-3
 share the same square **(93)** with subpattern-3 between starting and pending square
 include the pending square **(78)**

(78) zaps (68) adding **(49)**

(78) zaps (18) adding **(17)**

(49) zaps (44) adding **(54)**

Subpattern-4 = **(61),(93),(78),(49),(17),(54)**

D G I F C E

Back at the starting box D, nothing is pending and no squares are unclaimed. The analysis is complete

3	059	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C9	row1							1 ₁₂₄	1 ₃	
	row2		X							
	row3						X			
	row4			1 ₁	1 ₂					1 ₃₄
	row5			1 ₂	1 ₁₃₄					
	row6	1 ₃₄							1 ₁₂	
	row7	1 ₁₂						1 ₃	1 ₄	
	row8					X				
	row9			1 ₃₄				P		1 ₁₂

Pattern 3.006	Box Orientation	Patterns with the same box code
3 – 3	E – F	019, 021, 023, 028, 036.
3 – 2	H – I	

	E	F
	H	I

Subpattern-1 begins in (54) with box order E→F→I→H
(54) zaps (57) adding (67) and pending (68)
(67) zaps (87) adding (98)
(54) zaps (84) and (98) zaps (96) adding (86)

Subpattern-1 = (54),(67),(98),(86)
E F I H

3	006	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
D1	row1									X
	row2				X					
	row3		X							
	row4	X							P	
	row5				1 ₁		1	1		
	row6				1			1 ₁	1 _P	
	row7			X						
	row8				1		1 ₁	1		
	row9						1		1 ₁	

Pattern 3.006, continued.

	E	F
	H	I

Due to pending situation in **F**, subpattern-2 must
begin in the same square **(54)** as subpattern-1
follow the same squares as subpattern-1 until pending box is reached
include the pending square **(68)**

(68) zaps (98) adding **(87)** zaps (84) & (86) adding **(96)**

Subpattern-2 = **(54),(68),(87),(96)**

E F I H

3	006	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
D1	row1									X
	row2					X				
	row3		X							
	row4	X							P	
	row5				1₁₂		1₃	1₄		
	row6				1₄			1₁₃	1₂	
	row7			X						
	row8				1₃		1₁₄	1₂		
	row9						1₂		1₁₃₄	

Pattern 3.006, continued.

	E	F
	H	I

Subpattern-3 begins in (56) with box order E→H→I→F

(56) zaps (86) & (96) adding (84) zaps (87) adding (98)
(56) zaps (57) while (98) zaps (68) adding (67)

Subpattern-3 = (56),(84),(98),(67)

E H I F

3	006	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
D1	row1									X
	row2					X				
	row3		X							
	row4	X								
	row5				1 ₁₂		1 ₃	1		
	row6				1			1 ₁₃	1 ₂	
	row7			X						
	row8				1 ₃		1 ₁	1 ₂		
	row9						1 ₂		1 ₁₃	

Pattern 3.006, continued.

	E	F
	H	I

Subpattern-4 begins in **(64)** with box order **E→H→I→F**

(64) zaps (67) & (68) adding **(57)** zaps (87) adding **(98)**

(64) zaps (84) while **(98)** zaps (96) adding **(86)**

Subpattern-4 = **(64),(57),(98),(86)**

E H I F

Back at the starting box E, nothing is pending and no squares are unclaimed, so the analysis is complete.

3	006	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
D1										
row1										X
row2					X					
row3		X								
row4	X									
row5				1 ₁₂		1 ₃	1 ₄			
row6				1 ₄			1 ₁₃	1 ₂		
row7			X							
row8				1 ₃		1 ₁₄	1 ₂			
row9						1 ₂		1 ₁₃₄		

Pattern 3.025	Box Orientation	Patterns with the same box code
2 3-3-3 2-2	E G-A-D I-C	none

A		C
D	E	
G		I

Subpattern-1 begins in (11) with box order **A→D→E→C→I→G**

(11) zaps (61) adding (53) and pending (63)
(53) zaps (55) adding (65)
(11) zaps (17) adding (39) zaps (79) adding (87) zaps (82) & (83) adding (72)

Subpattern-1 = (11),(53),(65),(39),(87),(72)
A D E C I G

3	025	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
D2	row1	1 ₁						1		
	row2						X			
	row3	1	1							1 ₁
	row4			P					X	
	row5			1 ₁		1				
	row6	1		1		1 ₁				
	row7		1 ₁							1
	row8		1	1				1 ₁		
	row9				X					

Pattern 3.025, continued.

A		C
D	E	
G		I

Due to the pending situation in **E**, subpattern-2 must
begin in the same square **(11)** as subpattern-1
follow the same squares as subpattern-1 until pending box is reached
include the pending square **(63)**

(63) zaps (65) adding **(55)**

(11) zaps (17) adding **(39)** zaps (79) adding **(87)** zaps (82) & (83) adding **(72)**

Subpattern-2 = **(11),(63),(55),(39),(87),(72)**

A D E C I G

3	025	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
D2	row1	1 ₁₂						1		
	row2						X			
	row3	1	1							1 ₁₂
	row4			P					X	
	row5			1 ₁		1 ₂				
	row6	1		1 ₂		1 ₁				
	row7		1 ₁₂							1
	row8		1	1				1 ₁₂		
	row9				X					

Pattern 3.025, continued.

A		C
D	E	
G		I

Subpattern-3 begins in (31) with box order **A→D→E→C→I→G**

(31) zaps (61) adding (53) and pending (63)
(53) zaps (55) adding (65)
(31) zaps (39) adding (17) zaps (87) adding (79)
(79) zaps (72) while (53) zaps (83) adding (82)

Subpattern-3 = (31),(53),(65),(17),(79),(82)
A D E C I G

3	025	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
D2	row1	1 ₁₂						1 ₃		
	row2						X			
	row3	1 ₃	1							1 ₁₂
	row4			P					X	
	row5			1 ₁₃		1 ₂				
	row6	1		1 ₂		1 ₁₃				
	row7		1 ₁₂							1 ₃
	row8		1 ₃	1				1 ₁₂		
	row9				X					

Pattern 3.025, continued.

A		C
D	E	
G		I

Due to the pending situation in **D**, subpattern-4 must
begin in the same square **(31)** as subpattern-3
follow the same squares as subpattern-3 until pending box is reached
include the pending square **(63)**

(63) zaps (65) adding **(55)**
(31) zaps (39) adding **(17)** zaps (87) adding **(79)**
(79) zaps (72) while **(63)** zaps (83) adding **(82)**

Subpattern-4 = **(31),(63),(55),(17),(79),(82)**

		A	D	E	C	I	G			
3	025	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
D2	row1	1 ₁₂						1 ₃₄		
	row2						X			
	row3	1 ₃₄	1							1 ₁₂
	row4			P					X	
	row5			1 ₁₃		1 ₂₄				
	row6	1		1 ₂₄		1 ₁₃				
	row7		1 ₁₂							1 ₃₄
	row8		1 ₃₄	1				1 ₁₂		
	row9				X					

Pattern 3.025, continued.

A		C
D	E	
G		I

Subpattern-5 begins in **(32)** with order of boxes **A→G→D→E→I→C**

(32) zaps (72) & (82) adding **(83)** zaps (63) & (53) adding **(61)** zaps (65) adding **(55)**
(83) zaps (87) adding **(79)** zaps (39) adding **(17)**

Subpattern-5 = **(32),(83),(61),(55),(79),(17)**

A G D E I C

Back at the starting box A, nothing is pending and no squares are unclaimed.
 The pattern analysis is complete.

3	025	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
D2	row1	1 ₁₂						1 ₃₄₅		
	row2						X			
	row3	1 ₃₄	1 ₅							1 ₁₂
	row4			P					X	
	row5			1 ₁₃		1 ₂₄₅				
	row6	1 ₅		1 ₂₄		1 ₁₃				
	row7		1 ₁							1 ₃₄₅
	row8		1 ₃₄	1 ₅				1 ₁₂		
	row9				X					

Pattern 3.026	Box Orientation	Patterns with the same box code
3 - 3 - 3	A - C - B	none
3 - 2	G - I	

A	B	C
G		I

Subpattern-1 starts in (12 with box order A→B→C→I→G

(12 zaps (14) adding (24) and pending (34)
(12) zaps (14) while (24) zaps (29) adding (39)
(39) zaps (89) adding (78) zaps (71) & (72) adding (81)

Subpattern-1 = (12,(24),(39),(78),(81)
 A B C I G

3	026	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
D3	row1		1 ₁		1		P		1	
	row2	1			1 ₁					1
	row3		1		1 _P					1 ₁
	row4						X			
	row5							X		
	row6			X						
	row7	1	1						1 ₁	
	row8	1 ₁								1
	row9					X				

Pattern 3.026, continued.

A	B	C
G		I

Due to pending condition in **B**, subpattern-2 must
begin in same square **(12)** as subpattern-1
follow same squares as subpattern-1 until pending box is reaches
include pending square **(34)**

(12) zaps **(18)** and **(34)** zaps **(39)** adding **(29)** zaps **(89)** adding **(78)**
(78) zaps **(71)** & **(72)** adding **(81)**

Subpattern-2 = **(12),(34),(29),(78),(81)**

A B C I G

3	026	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
D3	row1		1 ₁₂		1		<i>P</i>		1	
	row2	1			1 ₁					1 ₂
	row3		1		1 ₂					1 ₁
	row4						X			
	row5							X		
	row6			X						
	row7	1	1						1 ₁₂	
	row8	1 ₁₂								1
	row9					X				

Pattern 3.026, continued.

A	B	C
G		I

Subpattern-3 starts in **(21)** with box order **A→G→I→C→B**

(21) zaps (71) & (81) adding **(72)** zaps (78) adding **(89)**

(89) zaps (29) & (39) adding **(18)**

(18) zaps (34) while **(21)** zaps (24) adding **(14)**

Subpattern-3 = **(21),(72),(89),(18),(14)**

A G I C B

3	026	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
D3	row1		1 ₁₂		1				1 ₃	
	row2	1 ₃			1 ₁					1 ₂
	row3		1		1 ₂₃					1 ₁
	row4						X			
	row5							X		
	row6			X						
	row7	1	1 ₃						1 ₁₂	
	row8	1 ₁₂								1 ₃
	row9					X				

Pattern 3.026, continued.

A	B	C
G		I

Subpattern-4 starts in (32) with box order **A→B→C→I→G**

(32) zaps (34) adding (24) and pending (14)
(32) zaps (39) while (24) zaps (29) adding (18)
(18) zaps (78) adding (89)
(32) zaps (72) while (89) zaps (81) adding (72)

Subpattern-4 = (32),(24),(18),(89),(72)
A B C I G

3 D3	026	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1		1 ₁₂		1 _p				1 ₃₄	
	row2	1 ₃			1 ₁₄		P			1 ₂
	row3		1 ₄		1 ₂₃					1 ₁
	row4						X			
	row5							X		
	row6			X						
	row7	1	1 ₃₄						1 ₁₂	
	row8	1 ₁₂								1 ₃₄
	row9					X				

Pattern 3.026, continued.

A	B	C
G		I

Due to pending condition in **C**, subpattern-5 must
 start in same square **(32)** as subpattern-4
 follow same squares as subpattern-4 until pending box is reached
 include pending square **(14)**

(32) zaps (39) while **(14)** zaps (18) adding **(29)**
(29) zaps (89) adding **(78)** zaps (71) & (72) adding **(81)**

Subpattern-5 = **(32),(13),(29),(78),(81)**
A B C I G

Back at the starting box A, nothing remains pending and no squares remain unclaimed, so the pattern analysis is complete.

3	026	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
D3	row1		1 ₁₂		1 ₅				1 ₃₄	
	row2	1 ₃			1 ₁₄		P			1 ₂₅
	row3		1 ₄₅		1 ₂₃					1 ₁
	row4						X			
	row5							X		
	row6			X						
	row7	1 ₄	1 ₃						1 ₁₂₅	
	row8	1 ₁₂₅								1 ₃₄
	row9					X				

Pattern 3.001	Box Orientation	Patterns with the same box code
4 - 2 - 2	B - C - A	007, 022, 049.
2	H	

A	B	C
	H	

Subpattern-1 starts in **(14)** with box order **B→C→A→H**

(14) zaps (17) adding **(27)** zaps (12) adding **(32)**

(14) zaps (94) adding **(95)**

Subpattern-1 = **(14),(27),(32),(95)**

B C A H

3	001	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
E1	row1		6		6 ₁	6		6		
	row2				6			6 ₁		
	row3		6 ₁			6				
	row4						X			
	row5			X						
	row6								X	
	row7									X
	row8	X								
	row9				6	6 ₁				

Pattern 3.001, continued.

A	B	C
	H	

Subpattern-2 starts in (15) with box order **B→C→A→H**

(15) zaps (17) adds (27)

(15) zaps (12) adds (32)

(15) zaps (95) adds (94)

Subpattern-2 = (15),(27),(32),(94)
 B C A H

3 E1	001	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1		6 ₄		6 ₁	6 ₂		6 ₃		
	row2				6 ₃			6 ₁₂₄		
	row3		6 ₁₂₃			6 ₄				
	row4						X			
	row5			X						
	row6								X	
	row7									X
	row8	X								
	row9				6 ₂₄	6 ₁₃				

Pattern 3.001, continued.

A	B	C
	H	

Subpattern-3 starts in (24) with box order **B→C→A→H**

(24) zaps (27) adding (17) zaps (12) adding (32)

(24) zaps (94) adding (95)

Subpattern-3 = (24),(17),(32),(95)
 B C A H

3 E1	001	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1		6 ₄		6 ₁	6 ₂		6 ₃		
	row2				6 ₃			6 ₁₂₄		
	row3		6 ₁₂₃			6 ₄				
	row4						X			
	row5			X						
	row6								X	
	row7									X
	row8	X								
	row9				6 ₂₄	6 ₁₃				

Pattern 3.001, continued.

A	B	C
	H	

Subpattern-4 starts in (35) with box order **B→A→C→H**

(35) zaps (32) adding (12) zaps (17) adding (27)

(35) zaps (95) adding (94)

Subpattern-4 = (35),(12),(27),(94)

B A C H

Back at the starting box A, nothing is pending and no squares are unclaimed. The pattern analysis is complete.

3	001	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
E1	row1		6 ₄		6 ₁	6 ₂		6 ₃		
	row2				6 ₃			6 ₁₂₄		
	row3		6 ₁₂₃			6 ₄				
	row4						X			
	row5			X						
	row6								X	
	row7									X
	row8	X								
	row9				6 ₂₄	6 ₁₃				

Example 3.001 continued.

Pictorial view of zapping by subpattern-1:

	1	2	3	4	5	6	7	8	9
1		6		6	6		6		
2				6			6		
3		6			6				
4									
5									
6									
7									
8									
9				6	6				

Arbitrary choice of first member of subpattern-1 in box B..

	1	2	3	4	5	6	7	8	9
1		6		6	6		6		
2				6			6		
3		6			6				
4									
5									
6									
7									
8									
9				6	6				

After zapping by first member, showing zapped area in dark. Forced choice of second member of subpattern-1 in box C.

	1	2	3	4	5	6	7	8	9
1		6		6	6		6		
2				6			6		
3		6			6				
4									
5									
6									
7									
8									
9				6	6				

After zapping by second member of subpattern-1 in box C, showing zapped area in dark. Forced choice of third member of subpattern-1 in box A

	1	2	3	4	5	6	7	8	9
1		6		6	6		6		
2				6			6		
3		6			6				
4									
5									
6									
7									
8									
9				6	6				

After zapping by third member of subpattern-1 in box A, showing zapped area in dark. Forced choice of fourth member of subpattern-1 in box H.

continued on next page

Example 3.001 continued.

End of pictorial view of zapping by subpattern-1.

	1	2	3	4	5	6	7	8	9
1		6		6	6		6		
2				6			6		
3		6			6				
4									
5									
6									
7									
8									
9				6	6				

After zapping by final subpattern member, showing total zapped area. No choices left for further members in other boxes.

Pictorial view of zapping by subpattern-2:

	1	2	3	4	5	6	7	8	9
1		6		6	6		6		
2				6			6		
3		6			6				
4									
5									
6									
7									
8									
9				6	6				

Arbitrary choice of first member of subpattern-2 from remaining choices in box B.

	1	2	3	4	5	6	7	8	9
1		6		6	6		6		
2				6			6		
3		6			6				
4									
5									
6									
7									
8									
9				6	6				

After zapping by first member, showing zapped area in dark. Forced choice of second member of subpattern-2 in box C.

continued on next page

Example 3.001 continued.

Pictorial view of zapping by subpattern-2, continued;

	1	2	3	4	5	6	7	8	9
1		6		6	6		6		
2				6			6		
3		6			6				
4									
5									
6									
7									
8									
9				6	6				

After zapping by second member of subpattern-1 in box C, showing zapped area in dark. Forced choice of third member of subpattern-1 in box A

	1	2	3	4	5	6	7	8	9
1		6		6	6		6		
2				6			6		
3		6			6				
4									
5									
6									
7									
8									
9				6	6				

After zapping by third member of subpattern-1 in box A, showing zapped area in dark. Forced choice of fourth member of subpattern-1 in box H.

	1	2	3	4	5	6	7	8	9
1		6		6	6		6		
2				6			6		
3		6			6				
4									
5									
6									
7									
8									
9				6	6				

After zapping by final subpattern member, showing total zapped area. No choices left for further members in other boxes.

Example 3.001 continued.

Pictorial view of zapping by subpattern-3:

	1	2	3	4	5	6	7	8	9
1		6		6	6		6		
2				6			6		
3		6			6				
4									
5									
6									
7									
8									
9				6	6				

Arbitrary choice of first member of subpattern-3 from remaining choices in box B.

	1	2	3	4	5	6	7	8	9
1		6		6	6		6		
2				6			6		
3		6			6				
4									
5									
6									
7									
8									
9				6	6				

After zapping by first member, showing zapped area in dark. Forced choice of second member of subpattern-3 in box C.

	1	2	3	4	5	6	7	8	9
1		6		6	6		6		
2				6			6		
3		6			6				
4									
5									
6									
7									
8									
9				6	6				

After zapping by second member of subpattern-1 in box C, showing zapped area in dark. Forced choice of third member of subpattern-1 in box A

	1	2	3	4	5	6	7	8	9
1		6		6	6		6		
2				6			6		
3		6			6				
4									
5									
6									
7									
8									
9				6	6				

After zapping by third member of subpattern-1 in box A, showing zapped area in dark. Forced choice of fourth member of subpattern-1 in box H.

Example 3.001 continued.

End of pictorial view of zapping by subpattern-3.

	1	2	3	4	5	6	7	8	9
1		6		6	6		6		
2				6			6		
3		6			6				
4									
5									
6									
7									
8									
9				6	6				

After zapping by final subpattern member, showing total zapped area. No choices left for further members in other boxes.

Pictorial view of zapping by subpattern-4:

	1	2	3	4	5	6	7	8	9
1		6		6	6		6		
2				6			6		
3		6			6				
4									
5									
6									
7									
8									
9				6	6				

Forced choice of first member of subpattern-3 in box B

	1	2	3	4	5	6	7	8	9
1		6		6	6		6		
2				6			6		
3		6			6				
4									
5									
6									
7									
8									
9				6	6				

After zapping by first member, showing zapped area in dark. Forced choice of second member of subpattern-3 in box A.

continued on next page

Example 3.001 continued.

Pictorial view of zapping by subpattern-4, continued.

1	2	3	4	5	6	7	8	9
	6		6	6		6		
			6			6		
	6			6				
			6	6				

After zapping by second member of subpattern-1 in box C, showing zapped area in dark. Forced choice of third member of subpattern-1 in box C

1	2	3	4	5	6	7	8	9
	6		6	6		6		
			6			6		
	6			6				
			6	6				

After zapping by third member of subpattern-1 in box A, showing zapped area in dark. Forced choice of fourth member of subpattern-1 in box H.

1	2	3	4	5	6	7	8	9
	6		6	6		6		
			6			6		
	6			6				
			6	6				

After zapping by final subpattern member, showing total zapped area. No choices left for further members in other boxes.

Pattern 3.040	Box Orientation	Patterns with the same box code
4 - 2 - 2	F - E - D	none
2 - 2	I - H	

A	B	C
D	E	F
G	H	I

Subpattern-1 starts in (69) with box order **F→E→D→H→I**

- (69) zaps (66) adding (46)
- (69) zaps (63) adding (63)
- (69) zaps (79) adding (88) zaps (85) adding (75)

Subpattern-1 = (69),(46),(63),(88),(75)
F E D H I

3		040	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
G5		row1		X							
		row2							X		
		row3				X					
		row4						7 ₁		7	
		row5			7 ₁					7	7
		row6			7			7			7 ₁
		row7					7 ₁				7
		row8					7			7 ₁	
		row9	X								

Pattern 3.040, continued.

A	B	C
D	E	F
G	H	I

Subpattern-2 starts in **(48)** with box order **F→E→D→H→I**

(48) zaps (46) adding **(66)** zaps (63) adding **(53)**

(48) zaps (88) adding **(79)** zaps (75) adding **(85)**

Subpattern-2 = **(48),(66),(53),(79),(85)**

F E D H I

3	040	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
G5	row1		X							
	row2							X		
	row3				X					
	row4						7 ₁		7 ₂	
	row5			7 ₁₂					7	7
	row6			7			7 ₂			7 ₁
	row7					7 ₁				7 ₂
	row8					7 ₂			7 ₁	
	row9	X								

Pattern 3.040, continued.

A	B	C
D	E	F
G	H	I

Subpattern-3 starts in **(58)** with box order **F→E→D→H→I**

(58) zaps (53) adding **(63)** zaps (66) adding **(46)**
(58) zaps (88) adding **(79)** zaps (75) adding **(85)**

Subpattern-3 = **(58),(63),(46),(79),(85)**
F E D H I

3 G5	040	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1		X							
	row2							X		
	row3				X					
	row4						7 ₁₃₄		7 ₂	
	row5			7 ₁₂					7 ₃	7 ₄
	row6			7 ₃₄			7 ₂			7 ₁
	row7					7 ₁₄				7 ₂₃
	row8					7 ₂₃			7 ₁₄	
	row9	X								

Pattern 3.040, continued.

A	B	C
D	E	F
G	H	I

Subpattern-4 starts in **(59)** with box order **F→E→D→H→I**

(59) zaps (53) adding **(63)** zaps (66) adding **(46)**
(59) zaps (79) adding **(88)** zaps (85) adding **(75)**

Subpattern-4 = **(59),(63),(46),(88),(75)**
F E D H I

Back at the starting box, nothing is pending and no squares are unclaimed, so the pattern analysis is complete.

3 G5	040	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1		X							
	row2							X		
	row3				X					
	row4						7 ₁₃₄		7 ₂	
	row5			7 ₁₂					7 ₃	7 ₄
	row6			7 ₃₄			7 ₂			7 ₁
	row7					7 ₁₄				7 ₂₃
	row8					7 ₂₃			7 ₁₄	
	row9	X								

Pattern 3.060	Box Orientation	Patterns with the same box code
4 - 2 - 2	C - B - A	none
2 - 2	F - E	
2	I	

A	B	C
	E	F
		I

Subpattern-1 begins in (17) with box order C→I→F→E→B→A

(17) zaps (97) adding (98) zaps (58) adding (69) zaps (65) adding (69)
(69) zaps (66) adding (54) zaps (14) adding (25) zaps (21) adding (31)

Subpattern-1 = (17),(98),(69),(54),(25),(31)
C I F E B A

3	060	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
G8		row1			2			2 ₁	2	
		row2	2			2 ₁				2
		row3	2 ₁							2
		row4		X						
		row5			2 ₁				2	
		row6				2				2 ₁
		row7			X					
		row8					X			
		row9						2	2 ₁	

Pattern 3.060, continued.

A	B	C
	E	F
		I

Subpattern-2 begins in **(18)** with box order **C→F→I→E→B→A**

(18) zaps (98) adding **(97)**
(18) zaps (58) adding **(69)** zaps (65) adding **(54)** zaps (14) adding **(25)**
(25) zaps (21) adding **(31)**

Subpattern-2 = **(18),(97),(69),(54),(25),(31)**
C F I E B A

3 060
G8

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				2			2 ₁	2 ₂	
row2	2				2 ₁₂				2
row3	2 ₁₂								2
row4		X							
row5				2 ₁₂				2	
row6					2				2 ₁₂
row7			X						
row8						X			
row9							2 ₂	2 ₁	

Pattern 3.060, continued.

A	B	C
	E	F
		I

Subpattern-3 begins in **(29)** with box order **C→F→I→E→B→A**

(29) zaps (69) adding **(58)** zaps (98) adding **(97)**
(58) zaps (54) adding **(65)** zaps (25) adding **(14)**
(29) zaps (21) adding **(31)**

Subpattern-3 = **(29),(58),(97),(65),(14),(31)**
C F I E B A

3 060
G8

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				2 ₃			2 ₁	2 ₂	
row2	2				2 ₁₂				2 ₃
row3	2 ₁₂₃								2
row4		X							
row5				2 ₁₂				2 ₃	
row6					2 ₃				2 ₁₂
row7			X						
row8						X			
row9							2 ₂₃	2 ₁	

Pattern 3.060, continued.

A	B	C
	E	F
		I

Subpattern-4 begins in **(39)** with box order **C→F→I→E→B→A**

(39) zaps (69) adding **(58)** zaps (98) adding **(97)**

(58) zaps (54) adding **(65)** zaps (25) adding **(14)**

(39) zaps (31) adding **(21)**

Subpattern-4 = **(39),(58),(97),(65),(14),(21)**

C F I E B A

Back at the starting box A, nothing is pending and no squares are unclaimed. The pattern analysis is complete.

3 060
G8

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				2 ₃₄			2 ₁	2 ₂	
row2	2 ₄				2 ₁₂				2 ₃
row3	2 ₁₂₃								2 ₄
row4		X							
row5				2 ₁₂				2 ₃₄	
row6					2 ₃₄				2 ₁₂
row7			X						
row8						X			
row9							2 ₂₃₄	2 ₁	

Pattern 3.056	Box Orientation	Patterns with the same box code
4 - 3 - 2	F - E - D	
2	A	

		C
D	E	F

Subpattern-1 begins in square **(48)** with box order **F→C→D→E**

(48) zaps (38) adding **(39)**

(48) zaps (41) adding **(51)**

(48) zaps (45) and **(51)** zaps (55) adding **(65)**

Subpattern-1 = **(48),(39),(51),(65)**

F C D E

3	056	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
E4	row1				X					
	row2		X							
	row3								4	4 ₁
	row4	4				4			4 ₁	
	row5	4 ₁				4				4
	row6					4 ₁			4	4
	row7							X		
	row8						X			
	row9			X						

Pattern 3.056, continued.

		C
D	E	F

Subpattern-2 begins in **(59)** with box order **F→C→D→E**

- (59)** zaps (39) adding **(38)**
- (59)** zaps (51) adding **(41)**
- (59)** zaps (55) while **(41)** zaps (45) adding **(65)**

Subpattern-2 = **(59),(38),(41),(65)**
 F C D E

3	056	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
E4	row1				X					
	row2		X							
	row3								4 ₂	4 ₁
	row4	4 ₂				4			4 ₁	
	row5	4 ₁				4				4 ₂
	row6					4 ₁₂			4	4
	row7							X		
	row8						X			
	row9			X						

Pattern 3.056, continued.

		C
D	E	F

Subpattern-3 begins in **(68)** with box order **F→C→D→E**

- (68)** zaps (38) adding **(39)**
- (68)** zaps (65) adding **(55)** and pending **(45)**
- (55)** zaps (51) adding **(41)**

Subpattern-3 = **(68),(39),(55),(41)**
 F C D E

3 E4	056	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1				X					
	row2		X							
	row3								4 ₂	4 ₁₃
	row4	4 ₂₃				4 _P	P		4 ₁	
	row5	4 ₁				4 ₃				4 ₂
	row6					4 ₁₂			4 ₃	4
	row7							X		
	row8						X			
	row9			X						

Pattern 3.056, continued.

		C
D	E	F

Subpattern-4 begins in **(68)** with box order **F→C→D→E**

Due to pending situation in box E, subpattern-4 must
 start in same square **(68)** as subpattern-3
 follow same square **(39)** as subpattern-3 between starting and pending boxes
 include pending square **(45)**

(45) zaps (41) adding **(51)**

Subpattern-4 = **(68),(39),(45),(51)**

3	056	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
E4	row1				X					
	row2		X							
	row3								4 ₂	4 ₁₃₄
	row4	4 ₂₃				4 ₄	P		4 ₁	
	row5	4 ₁₄				4 ₃				4 ₂
	row6					4 ₁₂			4 ₃₄	4
	row7							X		
	row8						X			
	row9			X						

Pattern 3.056, continued.

		C
D	E	F

Subpattern-5 begins in **(69)** with box order **F→C→D→E**

(69) zaps (39) adding **(38)**
(69) zaps (65) adding **(55)** and pending **(45)**
(55) zaps (51) adding **(41)**

Subpattern-5 = **(69),(38),(55),(45)**
 F C D E

3	056	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
E4	row1				X					
	row2		X							
	row3								4 ₂₅	4 ₁₃₄
	row4	4 ₂₃₅				4 _{4P}	P		4 ₁	
	row5	4 ₁₄				4 ₃₅				4 ₂
	row6					4 ₁₂			4 ₃₄	4 ₅
	row7							X		
	row8						X			
	row9			X						

Pattern 3.056, continued.

		C
D	E	F

Due to pending condition in box F, subpattern-5 must
 start in same square **(68)** as subpattern-4
 follow same square **(38)** as subpattern-4 between starting and pending boxes
 include pending square **(45)**

(45) zaps (41) adding **(51)**

Subpattern-6 = **(68),(38),(45),(51)**
 F C D E

Back at the starting box F, no box is pending, and no squares are unclaimed, so the pattern analysis is complete.

3	056	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
E4	row1				X					
	row2		X							
	row3								4 ₂₅₆	4 ₁₃₄
	row4	4 ₂₃₅				4 ₄₆	P		4 ₁	
	row5	4 ₁₄₆				4 ₃₅				4 ₂
	row6					4 ₁₂			4 ₃₄	4 ₅₆
	row7							X		
	row8						X			
	row9			X						

Pattern 3.062	Box Orientation	Patterns with the same box code
$\begin{array}{c} 2 \\ \\ 4-3 \\ \\ 2 \end{array}$	$\begin{array}{c} C \\ \\ H-B \\ \\ G \end{array}$	none

A	B	C
D	E	F
G	H	I

Box order: $H(\rightarrow G)\rightarrow B\rightarrow C$

Subpattern-1 begins in (74) zaps (72) adding (82)
(74) zaps (14) adding (16) and pending (26)
(16) zaps (18) adding (28)

Subpattern-1 = (74),(82),(16),(28)
H G B C

3	062	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
E5	row1				2		2 ₁		2	
	row2						2 _P		2 ₁	
	row3	X				P				
	row4					X				
	row5			X						
	row6									X
	row7		2		2 ₁		2			
	row8		2 ₁		2		2			
	row9							X		

Pattern 3.062, continued.

A	B	C
D	E	F
G	H	I

Box order: **H**→**G**→**B**→**C**

Due to pending condition in box **B**, subpattern-2 must
begin in the same square **(74)** as subpattern-1
share **(82)** with subpattern-1
include the pending square **(26)**

(26) zaps (28) adding **(18)**

subpattern-2 = **(74),(82),(26),(18)**
H G B C

3	062	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
E5	row1				2		2 ₁		2 ₂	
	row2						2 ₂		2 ₁	
	row3	X				P				
	row4					X				
	row5			X						
	row6									X
	row7		2		2 ₁₂		2			
	row8		2 ₁₂		2		2			
	row9							X		

Pattern 3.062, continued.

A	B	C
D	E	F
G	H	I

Box order: **H→G→B→C**

Subpattern-3 begins in **(76)** zaps (72) adding **(82)**
(76) zaps (16) & (26) adding **(14)** zaps (18) adding **(28)**

Subpattern-3 = **(76),(82),(14),(28)**
H G B C

3 E5	062	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1				2 ₃		2 ₁		2 ₂	
	row2						2 ₂		2 ₁₃	
	row3	X								
	row4					X				
	row5			X						
	row6									X
	row7		2		2 ₁₂		2 ₃			
	row8		2 ₁₂₃		2		2			
	row9							X		

Pattern 3.062, continued.

A	B	C
D	E	F
G	H	I

Box order: **H→G→B→C**

Subpattern-4 begins in **(84)** zaps (82) adding **(72)**

(84) zaps (14) adding **(16)** and pending **(26)**

(16) zaps (18) adding **(28)**

Subpattern-4 = **(84),(72),(16),(28)**

H G B C

3 E5	062	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1				2 ₃		2 ₁₄		2 ₂	
	row2						2 ₂		2 ₁₃₄	
	row3	X				P				
	row4					X				
	row5			X						
	row6									X
	row7		2 ₄		2 ₁₂		2 ₃			
	row8		2 ₁₂₃		2 ₄		2			
	row9							X		

Pattern 3.062, continued.

A	B	C
D	E	F
G	H	I

Box order: **H→G→B→C**

Due to the pending condition in **B**, subpattern-5 must
start in the same square **(84)** as subpattern-4
share square **(72)** with subpattern-4
include the pending square **(26)**

(26) zaps (28) adding **(18)**

Subpattern-5 = **(84),(72),(26),(18)**
H G B C

3 E5	062	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1				2 ₃₆		2 ₁₄		2 ₂₅	
	row2						2 ₂₅		2 ₁₃₄₆	
	row3	X				P				
	row4					X				
	row5			X						
	row6									X
	row7		2 ₄₅₆		2 ₁₂		2 ₃			
	row8		2 ₁₂₃		2 ₄₅		2 ₆			
	row9							X		

Pattern 3.062, continued.

A	B	C
D	E	F
G	H	I

Box order: **H→G→B→C**

Subpattern-6 starts in **(86)** zaps (82) adding **(72)**
(86) zaps (16) & (26) adding **(14)** zaps (18) adding **(28)**

Subpattern-6 = **(86),(72),(14),(28)**

H G B C

Back at the starting box I, nothing is pending and no squares unclaimed, so the pattern analysis is complete.

3	062	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
E5	row1				2 ₃₆		2 ₁₄		2 ₂₅	
	row2						2 ₂₅		2 ₁₃₄₆	
	row3	X								
	row4					X				
	row5			X						
	row6									X
	row7		2 ₄₅₆		2 ₁₂		2 ₃			
	row8		2 ₁₂₃		2 ₄₅		2 ₆			
	row9							X		

Pattern 3.003	Box Orientation	Patterns with the same box code
4 – 3	D – F	053
2 – 3	A – C	

A		C
D		F

Subpattern-1 starts in (51) with box order **D→A→F→C**

(51) zaps (11) adding **(33)**
(51) zaps (58) & (59) adding **(69)**
(69) zaps (19) while **(33)** zaps (38) adding **(18)**

Subpattern-1 = **(51),(33),(69),(18)**

3	003	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
G1		row1	2						2 ₁	2
		row2					X			
		row3			2 ₁				2	
		row4			X					
		row5	2 ₁		2				2	2
		row6	2		2					2 ₁
		row7				X				
		row8		X						
		row9						X		

Pattern 3.003, continued.

A		C
D		F

Subpattern-2 starts in (53) with box order **D→A→C→F**

(53) zaps (33) adding (11) zaps (18) & (19) adding (38)

(53) zaps (58) & (59) adding (69)

Subpattern-2 = (53),(11),(38),(69)

D A C F

3 003
G1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	2 ₂							2 ₁	2
row2						X			
row3			2 ₁					2 ₂	
row4				X					
row5	2 ₁		2 ₂					2	2
row6	2		2						2 ₁₂
row7					X				
row8		X							
row9							X		

Pattern 3.003, continued.

A		C
D		F

Subpattern-3 starts in (61) with box order **D→A→C→F**

(61) zaps (11) adding (33) zaps (38) adding (19) and pending (18)
(19) zaps (59) & (69) adding (58)

Subpattern-3 = (63),(11),(19),(58)
 D A C F

3 003
G1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	2 ₂							2 ₁	2 ₃
row2						X			P
row3			2 ₁₃					2 ₂	
row4				X					
row5	2 ₁		2 ₂					2 ₃	2
row6	2 ₃		2						2 ₁₂
row7					X				
row8		X							
row9							X		

Pattern 3.003, continued.

A		C
D		F

Due to the pending situation in **C**, subpattern-4 must start in the same square **(61)** as subpattern-3 share square **(33)** with subpattern-3 include the pending square **(18)**

(18) zaps (58) & **(61)** zaps (69) adding **(59)**

Subpattern-4 = **(61),(33),(18),(59)**

Back at the starting box D, nothing is pending and no squares are unclaimed. The pattern analysis is complete.

3 003
G1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	2 ₂₅							2 ₁₄	2 ₃
row2						X			P
row3			2 ₁₃₄					2 ₂₅	
row4				X					
row5	2 ₁		2 ₂					2 ₃	2 ₄₅
row6	2 ₃₄		2 ₅						2 ₁₂
row7					X				
row8		X							
row9							X		

Pattern 3.057	Box Orientation	Patterns with the same box code
4 - 3 - 2	D - E - F	058
3 - 3	A - B	

A	B	C
D	E	F
G	H	I

Subpattern-1 begins in square **(43)** with box order **D→A→B→E→F**

(43) zaps **(23)** & **(33)** adding **(21)** zaps **(24)** & **(26)** adding **(36)**

(36) zaps **(46)** & **(56)** adding **(54)**

(43) zaps **(68)** adding **(48)**

Subpattern-1 = **(43),(21),(36),(54),(48)**

D A B E F

3	057	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
E6										
row1								X		
row2	8 ₁		8	8		8				
row3			8			8 ₁				
row4			8 ₁			8		8		
row5	8		8	8 ₁		8				
row6	8							8 ₁		
row7										X
row8		X								
row9					X					

Pattern 3.057, continued.

A	B	C
D	E	F
G	H	I

Subpattern-2 starts in **(51)** with box order **D→E→F→B→A**

(51) zaps (54) & (56) adding **(46)** zaps (48) adding **(68)**
(46) zaps (26) & (36) adding **(24)** zaps (21) & (23) adding **(33)**

Subpattern-2 = **(51),(46),(68),(24),(33)**
D E F B A

3 057
E6

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							X		
row2	8 ₁		8	8 ₂		8			
row3			8 ₂			8 ₁			
row4			8 ₁			8 ₂		8	
row5	8 ₂		8 _K	8 ₁		8			
row6	8							8 ₁₂	
row7									X
row8		X							
row9					X				

Pattern 3.057, continued.

A	B	C
D	E	F
G	H	I

Subpattern-3 begins in (53) with box order $D \rightarrow A \rightarrow B \rightarrow E \rightarrow F$
 (53) zaps (23) & (33) adding (21) zaps (24) & (26) adding (36)
 (36) zaps (46) & (56) adding (54)

These evaluations have all been forced, and now we have both (53) and (54) in the same row 5, and in the same subpattern-3. Therefore (53) cannot have a candidate, and we must give it the K subscript (for killer).

We'll retry subpattern-3 in a different starting square (61) (the only remaining choice in box D). We'll use the box order $D \rightarrow A \rightarrow B \rightarrow F \rightarrow E$.

(61) zaps (21) adding (23) and pending (33)
 (61) zaps (68) adding (48)
 (23) zaps (24) & (26) adding (36) zaps (46) & (56) adding (54)
 (61) zaps (68) adding (48)

Subpattern-3 = (61),(23),(36),(48),(54)

3	057	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
E6			P					X		
	row1									
	row2	8 ₁		8 ₃	8 ₂		8			
	row3			8 ₂			8 ₁₃			
	row4			8 ₁			8 ₂		8 ₃	
	row5	8 ₂		8 _K	8 ₁₃		8			
	row6	8 ₃							8 ₁₂	
	row7									X
	row8		X							
	row9					X				

Pattern 3.057, continued.

A	B	C
D	E	F
G	H	I

Due to the pending situation in **A**, subpattern-4 must
begin in the same square **(61)** as subpattern-3
follow the same squares **(34)** as subpattern-3 between starting and pending boxes
include the pending square **(33)**

(33) zaps **(36)** adding **(26)** and pending **(24)**
(As the pending situation in A is now resolved, B is the only remaining pending box)

(61) zaps **(68)** adding **(48)**
(26) zaps **(46)** & **(56)** adding **(54)**

Subpattern-4 = **(61),(33),(26),(48),(54)**

D A B E F

3 057
E6

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					<i>P</i>		<i>X</i>		
row2	8 ₁		8 ₃	8 _{2p}		8 ₄			
row3			8 ₂₄			8 ₁₃			
row4			8 ₁			8 ₂		8 ₃₄₅	
row5	8 ₂		8 _K	8 ₁₃₄		8 ₅			
row6	8 ₃₄₅							8 ₁₂	
row7									<i>X</i>
row8		<i>X</i>							
row9					<i>X</i>				

Pattern 3.057, continued.

A	B	C
D	E	F
G	H	I

Due to the pending situation in **B**, subpattern-5 must start in the same square **(61)** as subpattern-4 share square **(33)** with subpattern-4 include the pending square **(24)**

(61) zaps (68) adding **(48)**
(48) zaps (46) and **(24)** zaps (54) adding **(56)**

Subpattern-5 = **(61),(33),(24),(48),(56)**

Back at the starting box D, no box is pending and no squares are unclaimed, so the analysis is complete.

3 057		col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
E6										
row1								X		
row2	8 ₁		8 ₃	8 ₂₅		8 ₄				
row3			8 ₂₄₅			8 ₁₃				
row4			8 ₁			8 ₂		8 ₃₄₅		
row5	8 ₂		8 _K	8 ₁₃₄		8 ₅				
row6	8 ₃₄₅							8 ₁₂		
row7										X
row8		X								
row9					X					

Pattern 3.027	Box Orientation	Patterns with the same box code
4 - 3 - 3	I - C - F	none
2 - 2	H - B	
2-----2	G-----D	

	B	C
D		F
G	H	I

Subpattern-1 started in (77) with box order I→G→H→B→C→F→D

(77) zaps (71) adding (93) zaps (94) adding (86) zaps (16) adding (34)
(34) zaps (38) while (77) zaps (17) adding (18)
(18) zaps (48) while (77) zaps (67) adding (49)
(93) zaps (43) adding (61)

Subpattern-1 = (77),(93),(86),(34),(18),(49),(61)
I G H B C F D

3	027	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
E8	row1						9	9	9 ₁	
	row2		X							
	row3				9 ₁				9	
	row4			9					9	9 ₁
	row5					X				
	row6	9 ₁						9		
	row7	9						9 ₁	9	
	row8						9 ₁			9
	row9			9 ₁	9					9

Pattern 3.027, continued.

	B	C
D		F
G	H	I

Subpattern-2 is started in (78) with box order I→G→H→B→C→F→D

(78) zaps (71) adding (93) zaps (94) adding (86) zaps (16) adding (34).

(78) zaps (18) & (38), adding (17)

(78) zaps (48) while (17) zaps (67) adding (49)

(93) zaps (43) adding (61)

Subpattern-2 = (78),(93),(86),(34),(17),(49)

I G H B C F

3	027	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
E8	row1						9	9 ₂	9 ₁	
	row2		X							
	row3				9 ₁₂				9	
	row4			9					9	9 ₁₂
	row5					X				
	row6	9 ₁₂						9		
	row7	9						9 ₁	9 ₂	
	row8						9 ₁₂			9
	row9			9 ₁₂	9					9

Pattern 3.027, continued.

	B	C
D		F
G	H	I

Subpattern-3 is started in **(89)** with box order **I→H→G→D→F→B→C**

(89) zaps **(86)** adding **(94)** zaps **(93)** adding **(71)** zaps **(61)** adding **(43)**
(43) zaps **(48)** & **(49)** adding **(67)**
(94) zaps **(34)** adding **(16)** zaps **(17)** & **(18)** adding **(38)**

Subpattern-3 = **(89),(94),(71),(43),(67),(16),(38)**
I H G D F B C

3 E8	027	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1						9 ₃	9 ₂	9 ₁	
	row2		X							
	row3				9 ₁₂				9 ₃	
	row4			9 ₃					9	9 ₁₂
	row5					X				
	row6	9 ₁₂						9 ₃		
	row7	9 ₃						9 ₁	9 ₂	
	row8						9 ₁₂			9 ₃
	row9			9 ₁₂	9 ₃					9

Pattern 3.027, continued.

	B	C
D		F
G	H	I

Subpattern-4 is started in **(89)** with box order **I→G→D→F→H→B→C**

(99) zaps (93) adding **(71)** zaps (61) adding **(43)** zaps (48) & (49) adding **(67)**
(99) zaps (94) adding **(86)** zaps (16) adding **(34)**
(34) zaps (38) while **(67)** zaps (17) adding **(18)**

Subpattern-4 = **(99),(71),(43),(67),(86),(34),(18)**
I G D F H B C

Back at the starting box I, nothing is pending, and no squares are unclaimed, so the pattern analysis is complete.

3 E8	027	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1						9 ₃	9 ₂	9 ₁₄	
	row2		X							
	row3				9 ₁₂₄				9 ₃	
	row4			9 ₃₄					9 _K	9 ₁₂
	row5					X				
	row6	9 ₁₂						9 ₃₄		
	row7	9 ₃₄						9 ₁	9 ₂	
	row8						9 ₁₂₄			9 ₃
	row9			9 ₁₂	9 ₃					9 ₄

Pattern 3.034	Box Orientation	Patterns with the same box code
5 – 2 – 2	E – B – H	none
2	F	

	B	
	E	F
	H	

Subpattern-1 starts in (44) with box order E→H→B→F

(44) zaps (75) adding (74) zaps (14) adding (16)
(44) zaps (48) adding (58)

Subpattern-1 = (44),(74),(16),(58)
 E H B F

3	034	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
F1	row1				2		2 ₁			
	row2			X						
	row3							X		
	row4	X			2 ₁	2	2		2	
	row5					2	2		2 ₁	
	row6									
	row7				2	2 ₁				
	row8									X
	row9		X							

Pattern 3.034, continued.

	B	
	E	F
	H	

Subpattern-2 starts in **(45)** with box order **E→H→B→F**

(45) zaps (75) adding **(74)** zaps (14) adding **(16)**

(45) zaps (48) adding **(58)**

Subpattern-2 = **(45),(74),(16),(58)**

E H B F

3	034	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
F1	row1				2		2 ₁₂			
	row2			X						
	row3							X		
	row4	X			2 ₁	2 ₂	2		2	
	row5					2	2		2 ₁₂	
	row6									
	row7				2 ₂	2 ₁				
	row8									X
	row9		X							

Pattern 3.034, continued.

	B	
	E	F
	H	

Subpattern-2 starts in **(45)** with box order **E→H→B→F**

(45) zaps (75) adding **(74)** zaps (13) adding **(16)**

(45) zaps (48) adding **(58)**

Subpattern-2 = **(45),(74),(16),(58)**

E H B F

3	034	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
F1	row1				2		2 ₁₂			
	row2			X						
	row3							X		
	row4	X			2 ₁	2 ₂	2		2	
	row5					2	2		2 ₁₂	
	row6									
	row7				2 ₂	2 ₁				
	row8									X
	row9		X							

Pattern 3.034, continued.

	B	
	E	F
	H	

Subpattern-3 starts in **(46)** with box order **E→B→H→F**

(46) zaps (16) adding **(14)** zaps (74) adding **(75)**

(46) zaps (48) adding **(58)**

Subpattern-3 = **(46),(14),(75),(58)**

E B H F

3	034	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
F1	row1				2 ₃		2 ₁₂			
	row2			X						
	row3							X		
	row4	X			2 ₁	2 ₂	2 ₃		2	
	row5					2	2		2 ₁₂₃	
	row6									
	row7				2 ₂	2 ₁₃				
	row8									X
	row9		X							

Pattern 3.034, continued.

	B	
	E	F
	H	

Subpattern-4 starts in **(55)** with box order **E→H→B→F**

(55) zaps **(75)** adding **(74)** zaps **(14)** adding **(16)**

(55) zaps **(58)** adding **(48)**

Subpattern-4 = **(55),(74),(16),(48)**

E H B F

3	034	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
F1	row1				2 ₃		2 ₁₂₄			
	row2			X						
	row3							X		
	row4	X			2 ₁	2 ₂	2 ₃		2 ₄	
	row5					2 ₄	2		2 ₁₂₃	
	row6									
	row7				2 ₂₄	2 ₁₃				
	row8									X
	row9		X							

Pattern 3.034, continued.

	B	
	E	F
	H	

Subpattern-5 starts in **(56)** with box order **E→B→H→F**

(56) zaps (16) adding **(14)** zaps (74) adding **(75)**

(56) zaps (58) adding **(48)**

Subpattern-5 = **(56),(14),(75),(48)**

E B H F

Back at the starting box E, nothing is pending and no squares unclaimed, so the pattern analysis is complete.

3	034	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
F1	row1				2 ₃₅		2 ₁₂₄			
	row2			X						
	row3							X		
	row4	X			2 ₁	2 ₂	2 ₃		2 ₄₅	
	row5					2 ₄	2 ₅		2 ₁₂₃	
	row6									
	row7				2 ₂₄	2 ₁₃₅				
	row8									X
	row9		X							

Pattern 3.002	Box Orientation	Patterns with the same box code
2 5 - 2 - 2 2	F H - I - G B	013, 016.

	B	
		F
G	H	I

Subpattern-1 begins in (75) with box order H→G→I→B→F

(75) zaps (72) adding (82)
(75) zaps (77) adding (99) zaps (49) adding (47)
(75) zaps (35) adding (36)

Subpattern-1 = (75),(82),(99),(47),(36)
 H G I B F

3 F2	002	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1								X	
	row2			X						
	row3					3	3 ₁			
	row4							3 ₁		3
	row5	X								
	row6				X					
	row7		3			3 ₁		3		
	row8		3 ₁			3	3			
	row9					3	3			3 ₁

Pattern 3.002, continued.

	B	
		F
G	H	I

Subpattern-2 begins in **(85)** with box order **H→G→I→F→B**

(85) zaps (82) adding **(72)** zaps (77) adding **(99)** zaps (49) adding **(47)**
(85) zaps (35) adding **(36)**

Subpattern-2 = **(85),(72),(99),(47),(36)**
H G I F B

3	002	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
F2	row1								X	
	row2			X						
	row3					3	3 ₁₂			
	row4							3 ₁₂		3
	row5	X								
	row6				X					
	row7		3 ₂			3 ₁		3		
	row8		3 ₁			3 ₂	3			
	row9					3	3			3 ₁₂

Pattern 3.002, continued.

	B	
		F
G	H	I

Subpattern-3 begins in **(86)** with box order **H→G→I→F→B**

(86) zaps (82) adding **(72)** zaps (77) adding **(99)** zaps (49) adding **(47)**
(86) zaps (36) adding **(35)**

Subpattern-3 = **(86),(72),(99),(47),(35)**
H G I F B

3 F2	002	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1								X	
	row2			X						
	row3					3 ₃	3 ₁₂			
	row4							3 ₁₂₃		3
	row5	X								
	row6				X					
	row7		3 ₂₃			3 ₁		3		
	row8		3 ₁			3 ₂	3 ₃			
	row9					3	3			3 ₁₂₃

Pattern 3.002, continued.

	B	
		F
G	H	I

Subpattern-4 begins in **(95)** with box order **H→I→F→G→B**

(95) zaps (99) adding **(77)** zaps (47) adding **(49)**

(77) zaps (72) adding **(82)**

(95) zaps (35) adding **(36)**

Subpattern-4 = **(95),(77),(49),(82),(36)**

H I F G B

3 F2	002	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1								X	
	row2			X						
	row3					3₃	3₁₂₄			
	row4							3₁₂₃		3₄
	row5	X								
	row6				X					
	row7		3₂₃			3₁		3₄		
	row8		3₁₄			3₂	3₃			
	row9					3₄	3			3₁₂₃

Pattern 3.002, continued.

	B	
		F
G	H	I

Subpattern-5 begins in **(96)** with box order **H→I→G→F→B**

(96) zaps (99) adding **(77)** zaps (47) adding **(49)**

(77) zaps (72) adding **(92)**

(96) zaps (36) adding **(35)**

Subpattern-5 = **(96),(77),(49),(92),(35)**

H I G F B

Back at the starting box H, nothing is pending, and no squares are unclaimed, so the pattern analysis is complete.

3	002	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
F2	row1								X	
	row2			X						
	row3					3 ₃₅	3 ₁₂₄			
	row4							3 ₁₂₃		3 ₄₅
	row5	X								
	row6				X					
	row7		3 ₂₃			3 ₁		3 ₄₅		
	row8		3 ₁₄₅			3 ₂	3 ₃			
	row9					3 ₄	3 ₅			3 ₁₂₃

Chapter 4. Patterns with four subscripts.

Pattern 4.019	Box Orientation	Patterns with the same box code
3 – 3 – 2	H – G – I	none
2 – 3	D – E	

D	E	
G	H	I

Box order: H→E→D→G→I
Since the top three rows aren't involved, we'll get them out of our visual way.

Subpattern-1 begins in (95) zaps (65) & (45) adding (44) zaps (42) adding (62)
(95) zaps (91) adding (71) and pending (81)
(71) zaps (78) adding (88)

Subpattern-1 = (95),(44),(62),(71),(88)
H E D G I

Due to the pending situation, subpattern-2 must
begin in the same starting square (95) as subpattern-1
share squares (44) and (62) with subpattern-1
include the pending square (81)

(81) zaps (88) adding (78)

Subpattern-2 = (95),(44),(62),(81),(78)
H E D G I

4	019	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row4		3		3 ₁₂	3					
row5										X
row6		3 ₁₂			3					
row7	3 ₁		P		3				3 ₂	
row8	3 ₂			3					3 ₁	
row9	3				3 ₁₂					

Pattern 4.019, continued.

D	E	
G	H	I

Box order: H→E→D→G→I

Subpattern-3 begins in (75) zaps (65) and (45) adding (44)
(44) zaps (42) adding (62)
(75) zaps (78) adding (88)
(88) zaps (81) while (75) zaps (71) adding (91)

Subpattern-3 = (75),(44),(62),(88),(91)
 H E D G I

Subpattern-4 begins in (84) zaps (88) adding (78)
(78) zaps (71) while (84) zaps (81) adding (91)
(84) zaps (44) adding (45) and pending (65)
(45) zaps (42) adding (62)

Subpattern-4 = (84),(78),(91),(45),(62)
 H E D G I

4	019	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row4		3		3 ₁₂₃	3 ₄	P			
	row5									X
	row6		3 ₁₂₃₄			3				
	row7	3 ₁				3 ₃			3 ₂₄	
	row8	3 ₂			3 ₄				3 ₁₃	
	row9	3 ₃₄				3 ₁₂				

Pattern 3.019, continued.

D	E	
G	H	I

Due to the pending situation in **E**, subpattern-5 must:
begin in the same starting square (84) as subpattern-4
share squares **(78)** and **(91)** with subpattern-4
include pending square **(65)**

(65) zaps (62) adding **(42)**

Subpattern-5 = **(84),(78),(91),(65),(42)**
H E D G I

Back at the starting box, nothing is pending and no boxes remain unclaimed. The pattern analysis is complete.

4	019	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A3	row1			X						
	row2							X		
	row3						X			
	row4		3 ₅		3 ₁₂₃	3 ₄	P			
	row5									X
	row6		3 ₁₂₃₄			3 ₅				
	row7	3 ₁				3 ₃			3 ₂₄₅	
	row8	3 ₂			3 ₄₅				3 ₁₃	
	row9	3 ₃₄₅				3 ₁₂				

Pattern 4.020	Box Orientation	Patterns with the same box code
$\begin{array}{c} 3-2 \\ \\ 3-2 \\ \\ 2 \end{array}$	$\begin{array}{c} I-H \\ \\ A-C \\ \\ D \end{array}$	none

A		C
D		
	H	I

Subpattern-1 starts in (22) with box order **A→C→I→H→D**

(22) zaps (27) adding (39) zaps (79) & (89) adding (77) zaps (75) adding (85)
(22) zaps (42) adding (43)

Subpattern-1 = (22),(39),(77),(85),(43)
 A C I H D

4	020	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A4	row1				X					
	row2		2 ₁					2		
	row3		2	2						2 ₁
	row4		2	2 ₁						
	row5						X			
	row6								X	
	row7					2		2 ₁		2
	row8					2 ₁				2
	row9	X								

Pattern 4.020, continued.

A		C
D		
	H	I

Subpattern-2 starts in (32) with box order **A→C→I→H→D**

(32) zaps (39) adding (27) zaps (77) adding (79) and pending (89)
(79) zaps (75) adding (85)
(32) zaps (42) adding (43)

Subpattern-2 = (32),(27),(79),(85),(43)
 A C I H D

4 A4	020	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1				X					
	row2		2 ₁					2 ₂		
	row3		2 ₂	2						2 ₁
	row4		2	2 ₁₂						
	row5						X			
	row6								X	
	row7					2		2 ₁		2 ₂
	row8					2 ₁₂				2 _P
	row9	X								P

Pattern 4.020, continued.

A		C
D		
	H	I

Subpattern-3 starts in **(32)** with box order **A→C→I→H→D**

Due to the pending situation in **I**, subpattern-3 must
 begin in the same starting square **(32)** as subpattern-2
 follow the same squares **(27)** as subpattern-2 between starting & pending boxes
 include pending square **(89)**

(32) zaps (42) adding **(43)**

(89) zaps (85) adding **(75)**

Subpattern-3 = **(32),(27),(89),(75),(43)**

A C I H D

4	020	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A4	row1				X					
	row2		2 ₁					2 ₂₃		
	row3		2 ₂₃	2						2 ₁
	row4		2	2 ₁₂₃						
	row5						X			
	row6								X	
	row7					2 ₃		2 ₁		2 ₂
	row8					2 ₁₂				2 ₃
	row9	X								≠

Pattern 4.020, continued.

A		C
D		
	H	I

Subpattern-4 starts in (33) with box order **A→C→I→H→D**

(33) zaps (39) adding (27) zaps (77) adding (79) and pending (89)

(79) zaps (75) adding (85)

(33) zaps (43) adding (42)

Subpattern-4 = (33),(27),(79),(85),(42)

A C I H D

4	020	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A4	row1				X					
	row2		2 ₁					2 ₂₃₄		
	row3		2 ₂₃	2 ₄						2 ₁
	row4		2 ₄	2 ₁₂₃						
	row5						X			
	row6								X	
	row7					2 ₃		2 ₁		2 ₂₄
	row8					2 ₁₂₄				2 ₃
	row9	X								P

Pattern 4.020, continued.

A		C
D		
	H	I

Subpattern-4 starts in **(33)** with box order **A→C→I→H→D**

Due to pending condition in **I**, subpattern-5 must
begin in same starting **(33)** square as subpattern-4
share same square **(27)** with subpattern-3
include pending square **(89)**

(89) zaps (85) adding **(75)**

(33) zaps (43) adding **(42)**

Subpattern-5 = **(33),(27),(89),(75),(42)**

A C I H D

Back at the starting box A, no pending condition remains, and no squares are unclaimed, so the pattern analysis is complete.

4	020	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A4	row1				X					
	row2		2 ₁					2 ₂₃₄₅		
	row3		2 ₂₃	2 ₄₅						2 ₁
	row4		2 ₄₅	2 ₁₂₃						
	row5						X			
	row6								X	
	row7					2 ₃₅		2 ₁		2 ₂₄
	row8					2 ₁₂₄				2 ₃₅
	row9	X								≠

Pattern 4.036	Box Orientation	Patterns with the same box code
$\begin{array}{c} 3-2 \\ \\ 3-3 \\ \\ 2 \end{array}$	$\begin{array}{c} B-C \\ \\ G-H \\ \\ D \end{array}$	none

	B	C
D		
G	H	

Subpattern-1 starts in (14) with box order **B→H→G→D→C**

(14) zaps (94) adding (75) and pending (95)
(75) zaps (72) & (73) adding (93) zaps (43) adding (42)
(14) zaps (17) adding (37)

Subpattern-1 = (14),(75),(93),(42),(37)
 B H G D C

4	036	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A5	row1				2 ₁	2		2		
	row2	X								
	row3					2		2 ₁		
	row4		2 ₁	2						
	row5						X			
	row6								X	
	row7		2	2		2 ₁				
	row8						P			X
	row9			2 ₁	2	2				

Pattern 4.036, continued.

	B	C
D		
G	H	

Box order **B→H→G→D→C**

Due to the pending condition in **H**, subpattern-2 must
begin in the same starting square **(14)** as subpattern-1
include the pending square **(95)**

(95) zaps (93) adding **(72)** and pending **(73)**

(72) zaps (42) adding **(43)**

(14) zaps (17) adding **(37)**

Subpattern-2 = **(14),(95),(72),(43),(37)**

B H G D C

4	036	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A5	row1				2 ₁₂	2		2		
	row2	X								
	row3					2		2 ₁₂		
	row4		2 ₁	2 ₂						
	row5						X			
	row6								X	
	row7	P ₂	2 ₂	2 _P		2 ₁				
	row8						≠			X
	row9			2 ₁	2	2 ₂				

Pattern 4.036, continued.

	B	C
D		
G	H	

Box order **B→H→G→D→C**

Due to the pending condition in **G**, subpattern-3 must
begin in the same starting square **(14)** as subpattern-2
share square **(95)** with subpattern-2
include the pending square **(73)**

(73) zaps (43) adding **(42)**

(14) zaps (17) adding **(37)**

Subpattern-3 = **(14),(95),(73),(42),(37)**

B H G D C

4	036	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A5	row1				2 ₁₂₃	2		2		
	row2	X								
	row3					2		2 ₁₂₃		
	row4		2 ₁₃	2 ₂						
	row5						X			
	row6								X	
	row7	P₂	2 ₂	2 ₃		2 ₁				
	row8									X
	row9			2 ₁	2	2 ₂₃				

Pattern 4.036, continued.

	B	C
D		
G	H	

Box order **B→H→G→D→C**

Subpattern-4 begins in **(15)** zaps (75) & (95) adding **(94)**
(94) zaps (93) adding **(72)** and pending **(73)**
(72) zaps (42) adding **(43)**
(15) zaps (17) adding **(37)**

Subpattern-4 = **(15),(94),(72),(43),(37)**
B H G D C

4	036	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A5	row1				2 ₁₂₃	2 ₄		2		
	row2	X								
	row3					2		2 ₁₂₃₄		
	row4		2 ₁₃	2 ₂₄						
	row5						X			
	row6								X	
	row7	P3	2 ₂₄	2 _{3P}		2 ₁				
	row8									X
	row9			2 ₁	2 ₄	2 ₂₃				

Pattern 4.036, continued.

	B	C
D		
G	H	

Box order **B**→**H**→**G**→**D**→**C**

Since a pending situation exists in **G**, subpattern-5 must
begin in the same starting square **(15)** as subpattern-4
share square **(94)** with subpattern-4
include the pending square **(73)**

(73) zaps (43) adding **(42)**

(15) zaps (17) adding **(37)**

Subpattern-5 = **(15),(94),(73),(42),(37)**

4	036	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A5	row1				2 ₁₂₃	2 ₄₅		2		
	row2	X								
	row3					2		2 ₁₂₃₄₅		
	row4		2 ₁₃₅	2 ₂₄						
	row5						X			
	row6								X	
	row7	p3	2 ₂₄	2 ₃₅		2 ₁				
	row8									X
	row9			2 ₁	2 ₄₅	2 ₂₃				

Pattern 4.036, continued.

	B	C
D		
G	H	

Box order **B→H→G→D→C**

Subpattern-6 starts in **(35)** zaps (75) & (95) adding **(94)**
(35) zaps (37) adding **(17)**
(94) zaps (93) adding **(72)** and pending **(73)**
(72) zaps (42) adding **(43)**

Subpattern-6 = **(35),(94),(72),(43),(17)**
B H G D C

4	036	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A5	row1				2 ₁₂₃	2 ₄₅		2 ₆		
	row2	X								
	row3					2 ₆		2 ₁₂₃₄₅		
	row4		2 ₁₃₅	2 ₂₄₆						
	row5						X			
	row6								X	
	row7	P3	2 ₂₄₆	2 ₃₅		2 ₁				
	row8									X
	row9			2 ₁	2 ₄₅₆	2 ₂₃				

Pattern 4.036, continued.

	B	C
D		
G	H	

Box order **B**→**H**→**G**→**D**→**C**

Due to pending condition in **G**, subpattern-7 must
 begin in same starting square **(35)** as subpattern-6
 share square **(94)** with subpattern-6
 include pending square **(73)**

(35) zaps (37) adding **(17)**

(73) zaps (43) adding **(42)**

Subpattern-7 = **(35),(94),(73),(42),(17)**

B H G D C

Back at the starting box, nothing is pending, and no squares unclaimed, so the pattern analysis is complete.

4	036	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A5	row1				2 ₁₂₃	2 ₄₅		2 ₆₇		
	row2	X								
	row3					2 ₆₇		2 ₁₂₃₄₅		
	row4		2 ₁₃₅₇	2 ₂₄₆						
	row5						X			
	row6								X	
	row7	P3	2 ₂₄₆	2 ₃₅₇		2 ₁				
	row8									X
	row9			2 ₁	2 ₄₅₆₇	2 ₂₃				

Pattern 4.004	Box Orientation	Patterns with the same box code
3-2 3-2 2-3	B-A F-E G-I	none

A	B	
	E	F
G		I

Subpattern-1 starts in (47) with box order **F→I→G→E→B→A**

(47) zaps (77) adding (78) and pending (98)
(78) zaps (72) adding (92)
(47) zaps (44) adding (66) zaps (36) & (26) adding (24) zaps (23) adding (33)

Subpattern-1 = (47),(78),(92),(66),(24),(33)
F I G E B A

4	004	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1										X
row2			5	5 ₁		5				
row3			5 ₁			5				
row4				5			5 ₁	5		
row5	X									
row6						5 ₁		5		
row7		5					5	5 ₁	P	
row8					X					
row9		5 ₁						5 _P		

Pattern 4.004, continued.

A	B	
	E	F
G		I

Box order is **F→I→G→E→B→A**

Due to pending condition in **I**, subpattern-2 must
begin in the same starting square **(47)** as subpattern-1
include the pending square **(98)**

(98) zaps (92) adding **(72)**
(47) zaps (44) adding **(66)** zaps (26) & (36) adding **(24)** zaps (23) adding **(33)**
Subpattern-2 = **(47),(92),(72),(66),(24),(33)**
F I G E B A

4 004	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A6									
row 1									X
row 2			5	5 ₁₂		5			
row 3			5 ₁₂			5			
row 4				5			5 ₁₂	5	
row 5	X								
row 6						5 ₁₂		5	
row 7		5 ₂					5	5 ₁	P
row 8					X				
row 9		5 ₁						5 ₂	

Pattern 4.004, continued.

A	B	
	E	F
G		I

Subpattern-3 begins in **(48)** with box order **F→I→G→E→B→A**

(48) zaps (78) & (98) adding **(77)** zaps (92) adding **(72)**

(48) zaps (44) adding **(66)** zaps (26) & (36) adding **(24)** zaps (23) adding **(33)**

Subpattern-3 = **(48),(77),(72),(66),(24),(33)**

F I G E B A

4 004	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A6 row 1									X
row 2			5	5 ₁₂₃		5			
row 3			5 ₁₂₃			5			
row 4				5			5 ₁₂	5 ₃	
row 5	X								
row 6						5 ₁₂₃		5	
row 7		5 ₂					5 ₃	5 ₁	
row 8					X				
row 9		5 ₁₃						5 ₂	

Pattern 4.004, continued.

A	B	
	E	F
G		I

Subpattern-4 begins in **(68)** with box order **F→I→G→E→B→A**

(68) zaps (78) & (98) adding **(77)** zaps (72) adding **(92)**
(68) zaps (66) adding **(44)** zaps (24) adding **(26)** and pending **(36)**
(26) zaps (23) adding **(33)**

Subpattern-4 = **(68),(77),(92),(44),(26),(33)**
F I G E B A

4 004	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A6 row 1						<i>P</i>			<i>X</i>
row 2			5	5 ₁₂₃		5 ₄			
row 3			5 ₁₂₃₄			5 _P			
row 4				5 ₄			5 ₁₂	5 ₃	
row 5	<i>X</i>								
row 6						5 ₁₂₃		5 ₄	
row 7		5 ₂					5 ₃₄	5 ₁	
row 8					<i>X</i>				
row 9		5 ₁₃₄						5 ₂	

Pattern 4.004, continued.

A	B	
	E	F
G		I

Subpattern-5 begins in **(68)** with box order **F→I→G→E→B→A**

Due to pending situation in box **B**, subpattern-5 must
begin in same starting square **(68)** as subpattern-4
share squares **(77)**, **(92)**, **(44)** with subpattern-4
include pending square **(36)**
(36) zaps **(23)** adding **(23)**

Subpattern-5 = **(68),(77),(92),(44),(36),(23)**

F I G E B A

At the starting box, nothing is pending and no squares unclaimed. We are done.

4 004	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A6									
row 1						<i>P</i>			<i>X</i>
row 2			5 ₅	5 ₁₂₃		5 ₄			
row 3			5 ₁₂₃₄			5 ₅			
row 4				5 ₄₅			5 ₁₂	5 ₃	
row 5	<i>X</i>								
row 6						5 ₁₂₃		5 ₄₅	
row 7		5 ₂					5 ₃₄₅	5 ₁	
row 8					<i>X</i>				
row 9		5 ₁₃₄₅						5 ₂	<i>P</i>

Pattern 4.008	Box Orientation	Patterns with the same box code
3 - 3 - 2	G - I - H	011, 031
3 - 2	A - C	

A		C
G	H	I

Box order **A→C→I→H→G**

Subpattern-1 begins in **(12)** zaps (17) adds **(39)** zaps (89) & (99) adding **(77)**
(12) zaps (72) & (92) adding **(93)**

Subpattern-1 = **(12),(39),(77),(86),(99)**
A C I H G

4	008	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		4 ₁					4			
row2					X					
row3		4	4							4 ₁
row4	X									
row5									X	
row6				X						
row7		4				4	4 ₁			
row8						4 ₁				4
row9		4	4 ₁							4

Pattern 4.008, continued.

A		C
G	H	I

Subpattern-2 starts in (32) with box order **A→C→G→I→H**

- (32) zaps (39) adding (17)
- (32) zaps (72) & (92) adding (93)
- (17) zaps (77) while (93) zaps (99) adding (89)
- (89) zaps (86) adding (76)

Subpattern-2 = (32),(17),(93),(89),(76)
 A C G I H

4 008	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A8									
row 1		4 ₁					4 ₂		
row 2					X				
row 3		4 ₂	4						4 ₁
row 4	X								
row 5								X	
row 6				X					
row 7		4				4 ₂	4 ₁		
row 8						4 ₁			4 ₂
row 9		4	4 ₁₂						4

Pattern 4.008, continued.

A		C
G	H	I

Subpattern-3 starts in (32) with box order **A→C→G→I→H**

- (32) zaps (39) adding (17)
- (32) zaps (72) & (92) adding (93)
- (17) zaps (71) while (93) zaps (99) adding (89)

Subpattern-3 = (32),(17),(93),(89),(76)
 A C G I H

4 008	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A8									
row 1		4 ₁					4 ₂₃		
row 2					X				
row 3		4 ₂₃	4						4 ₁
row 4	X								
row 5								X	
row 6				X					
row 7		4				4 ₂₃	4 ₁		
row 8						4 ₁			4 ₂₃
row 9		4	4 ₁₂₃						4

Pattern 4.008, continued.

A		C
G	H	I

Subpattern-4 starts in **(33)** with box order **A→C→G→I→H**

(33) zaps (39) adding **(17)**

(33) zaps (93) adding **(92)** and pending **(72)**

(92) zaps (99) and **(17)** zaps (77) adding **(89)**

Subpattern-4 = **(33),(17),(92),(89),(76)**

A C G I H

4 008	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A8									
row 1		4 ₁					4 ₂₃₄		
row 2					X				
row 3		4 ₂₃	4 ₄						4 ₁
row 4	X								
row 5								X	
row 6				X					
row 7		4 _p				4 ₂₃₄	4 ₁		
row 8						4 ₁			4 ₂₃₄
row 9	P	4 ₄	4 ₁₂₃						4

Pattern 4.008, continued.

A		C
G	H	I

Subpattern-5 starts in **(33)** with box order **A→C→G→H→I**

Due to the pending situation in **G**, subpattern-5 must
begin in the same starting square **(33)** as subpattern-4
share square **(86)** with subpattern-4 between starting and pending boxes
include the pending square **(72)**

(33) zaps (39) adding **(17)**

(72) zaps (76) adding **(86)**

(72) zaps (77) and **(86)** zaps (89) adding **(99)**

Subpattern-5 = **(33),(72),(86),(99),(17)**

A C G H I

At the starting box, nothing pending and no squares unclaimed. Analysis complete.

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		4 ₁					4 ₂₃₄₅		
row2					X				
row3		4 ₂₃	4 ₄₅						4 ₁
row4	X								
row5								X	
row6				X					
row7		4 ₅				4 ₂₃₄	4 ₁		
row8						4 ₁₅			4 ₂₃₄
row9	X	4 ₄	4 ₁₂₃						4 ₅

Pattern 4.039	Box Orientation	Patterns with the same box code
2 3-3-2 2-2 2	B D-F-E G-I A	none

A	B	
D	E	F
G		I

Subpattern-1 starts in (43) with box order **D→E→B→F→I→G→A**

(43) zaps (46) adding (64) zaps (34) adding (36)
(64) zaps (76) while (43) zaps (47) adding (58)
(43) zaps (93) adding (81) zaps (21) adding (22)

Subpattern-1 = (43),(64),(36),(58),(97),(81),(22)
D E B F I G A

4	039	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1										X
row2		8	8 ₁							
row3					8		8 ₁			
row4				8 ₁			8	8		
row5		8	8						8 ₁	
row6					8 ₁			8		
row7						X				
row8		8 ₁							8	
row9				8				8 ₁		

Pattern 4.039, continued.

A	B	
D	E	F
G		I

Subpattern-2 starts in (51) with box order **D→A→G→I→F→E→B**

(51) zaps (21) adding (22)
(51) zaps (81) adding (93) zaps (97) adding (88) zaps (58) adding (47) and pending (67)
(47) zaps (46) adding (64) zaps (34) adding (36)

Subpattern-2 = (51),(22),(93),(88),(47),(64),(36)
D A G I F E B

4	039	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1									X
	row2	8	8 ₁₂							
	row3				8		8 ₁₂			
	row4			8 ₁			8	8 ₂		
	row5	8 ₂	8						8 ₁	P
	row6				8 ₁₂			8		
	row7					X				
	row8	8 ₁							8 ₂	
	row9			8 ₂				8 ₁		

Pattern 4.039, continued.

A	B	
D	E	F
G		I

Box order: D→A→G→I→F→E→B

Due to the pending condition in **F**, subpattern-3 must
begin in the same starting square **(51)** as subpattern-2
share squares **(22),(93),(88)** with subpattern-2 between starting and pending boxes
include the pending square **(67)**

(67) zaps (64) adding **(46)** zaps (36) adding **(34)**

Subpattern-3 = **(51),(22),(93),(88),(67),(46),(34)**
 D A G I F E B

4	039	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1									X
	row2	8	8 ₁₂₃							
	row3				8 ₃		8 ₁₂			
	row4			8 ₁			8 ₃	8 ₂		
	row5	8 ₂₃	8						8 ₁	P
	row6				8 ₁₂			8 ₃		
	row7					X				
	row8	8 ₁							8 ₂₃	
	row9			8 ₂₃				8 ₁		

Pattern 4.039, continued.

A	B	
D	E	F
G		I

Subpattern-4 begins in (52) with box order **D→A→G→I→F→E→B**

(52) zaps (22) adding (21) zaps (81) adding (93) zaps (97) adding (88)
(88) zaps (58) adding (47) and pending (67)
(47) zaps (46) adding (64) zaps (34) adding (36)

Subpattern-4 = (52),(21),(93),(88),(47),(64),(36)
D A G I F E B

4 039	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A9									
row 1									X
row 2	8 ₄	8 ₁₂₃							
row 3				8 ₃		8 ₁₂₄			
row 4			8 ₁			8 ₃	8 ₂₄		
row 5	8 ₂₃	8 ₄						8 ₁	
row 6				8 ₁₂₄			8 _{3P}		P
row 7					X				
row 8	8 ₁							8 ₂₃₄	
row 9			8 ₂₃₄				8 ₁		

Pattern 4.039, continued.

A	B	
D	E	F
G		I

Due to the pending condition in F, subpattern-5 must
begin in the same starting square (52) as subpattern-4
share squares (21),(93),(88) with subpattern-4
include pending square (67)

(67) zaps (64) adding (46) zaps (36) adding (34)

Subpattern-5 = (52),(21),(93),(88),(67),(46),(34)
D A G I F E B

Back at the starting box, nothing pending, no squares unclaimed, analysis complete.

4 039	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A9									
row 1									X
row 2	8 ₄₅	8 ₁₂₃							
row 3				8 ₃₅		8 ₁₂₄			
row 4			8 ₁			8 ₃₅	8 ₂₄		
row 5	8 ₂₃	8 ₄₅						8 ₁	
row 6				8 ₁₂₄			8 ₃₅		P
row 7					X				
row 8	8 ₁							8 ₂₃₄₅	
row 9			8 ₂₃₄₅				8 ₁		

Pattern 4.003	Box Orientation	Patterns with the same box code
4 – 3 – 2	H – E – B	016,022
2	I	

	B	
	E	
	H	I

Box order: **H→I→E→B**

Subpattern-1 startx in **(74)** zaps **(77)** adding **(87)**
(74) zaps **(64)** adding **(65)** and pending **(66)**
(65) zaps **(15)** adding **(16)**

Subpattern-1 = **(74),(87),(65),(16)**
H I E B

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					2	2 ₁			
row2		X							
row3									X
row4			X						
row5				<i>P</i>				X	
row6				2	2 ₁	2 _p			
row7				2 ₁		2	2		
row8				2		2	2 ₁		
row9	X								

Pattern 4.003, continued.

	B	
	E	
	H	I

Box order: **H→I→E→B**

Due to the pending situation in **E**, subpattern-2 must
begin in the same starting square, **(74)** as subpattern-1
share square **(87)** with subpattern-1
include pending square **(66)**

(66) zaps (16) adding **(15)**

Subpattern-2 = **(74),(87),(66),(15)**
H I E B

4 003	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B1									
row 1					2 ₂	2 ₁			
row 2		X							
row 3									X
row 4			X	P					
row 5								X	
row 6				2	2 ₁	2 ₂			
row 7				2 ₁₂		2	2		
row 8				2		2	2 ₁₂		
row 9	X								

Pattern 4.003, continued.

	B	
	E	
	H	I

Box order: **H→I→B→E**

Subpattern-3 will start in **(84)** zaps (87) adding **(77)**
(84) zaps (64) adding **(65)** and pending **(66)**

Subpattern-3 = **(84),(77),(65),(16)**
H I B E

4 003	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B1									
row 1					2 ₂	2 ₁₃			
row 2		X							
row 3									X
row 4			X			P			
row 5								X	
row 6				2	2 ₁₃	2 _p			
row 7				2 ₁₂		2	2 ₃		
row 8				2 ₃		2	2 ₁₂		
row 9	X								

Pattern 4.003, continued.

	B	
	E	
	H	I

Box order: **H→I→B→E**

Due to the pending situation in **E**, subpattern-4 must
begin in the same starting square **(84)** as subpattern-3
share square **(77)** with subpattern-3
include pending square **(66)**

(66) zaps (16) adding **(15)**

Subpattern-4 = **(84),(77),(66),(15)**
H I B E

4 003	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B1									
row 1					2 ₂₄	2 ₁₃			
row 2		X							
row 3									X
row 4			X			P			
row 5								X	
row 6				2	2 ₁₃	2 ₂₄			
row 7				2 ₁₂		2	2 ₃₄		
row 8				2 ₃₄		2	2 ₁₂		
row 9	X								

Pattern 4.003, continued.

	B	
	E	
	H	I

Box order: **H→I→B→E**

Subpattern-5 begins in **(76)** zaps (77) adding **(87)**
(76) zaps (16) adding **(15)**
(15) zaps (65) while **(76)** zaps (66) adding **(64)**

Subpattern-5 = **(76),(97),(15),(64)**
H I B E

4 003	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B1									
row 1					2 ₂₄₅	2 ₁₃			
row 2		X							
row 3									X
row 4			X						
row 5								X	
row 6				2 ₅	2 ₁₃	2 ₂₄			
row 7				2 ₁₂		2 ₅	2 ₃₄		
row 8				2 ₃₄		2	2 ₁₂₅		
row 9	X								

Pattern 4.003, continued.

	B	
	E	
	H	I

Box order: **H**→**I**→**B**→**E**

Subpattern-6 begins in **(86)** zaps (87) adding **(77)**

(86) zaps (16) adding **(15)**

(86) zaps (66) and **(15)** zaps (65) adding **(64)**

Subpattern-6 = **(86),(77),(15),(64)**

H I B E

Back at the starting box H, nothing is pending and no squares are unclaimed. Done.

4 003 col 1 col 2 col 3 col 4 col 5 col 6 col 7 col 8 col 9

B1									
row 1					2 ₂₄₅₆	2 ₁₃			
row 2		X							
row 3									X
row 4			X						
row 5								X	
row 6				2 ₅₆	2 ₁₃	2 ₂₄			
row 7				2 ₁₂		2 ₅	2 ₃₄₆		
row 8				2 ₃₄		2 ₆	2 ₁₂₅		
row 9	X								

Pattern 4.027	Box Orientation	Patterns with the same box code
2 4-3 2	A E-D H	038

A		
D	E	
	H	

Subpattern-1 starts in (44) with box order E→H→D→A

(44) zaps (84) adding (85)
(44) zaps (41) & (42) adding (62) zaps (12) adding (11)

Subpattern-1 = (44),(85),(62),(11)
 E H D A

4	027	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B2	row1	3 ₁	3							
	row2							X		
	row3						X			
	row4	3	3		3 ₁	3				
	row5									X
	row6		3 ₁		3	3				
	row7								X	
	row8				3	3 ₁				
	row9			X						

Pattern 4.027, continued.

A		
D	E	
	H	

Subpattern-2 starts in (45) with box order E→H→D→A

(45) zaps (85) adding (84)
(45) zaps (41) & (42) adding (62) zaps (12) adding (11)

Subpattern-2 = (45),(84),(62),(11)

Subpattern-3 starts in (64) with box order E→H→D→A

(64) zaps (84) adding (85)
(64) zaps (62) adding (41) and pending (42)
(41) zaps (11) adding (12)

Subpattern-3 = (64),(85),(41),(12)
 E H D A

4	027	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B2	row1	3 ₁₂	3 ₃							
	row2							X		
	row3						X			
	row4	3 ₃	3		3 ₁	3 ₂				
	row5									X
	row6	P	3 ₁₂		3 ₃	3				
	row7								X	
	row8				3 ₂	3 ₁₃				
	row9			X						

Pattern 4.027, continued.

A		
D	E	
	H	

Box order: **E→H→D→A**

Due to the pending condition in **D**, subpattern-4 must
begin in the same starting square **(64)** as subpattern-3
share **(85)** with subpattern-3
include the pending square **(62)**

(62) zaps **(12)** adding **(11)**

Subpattern-4 = **(64),(85),(62),(11)**
E H D A

4 027		col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B2	row1	3 ₁₂₄	3 ₃							
	row2							X		
	row3						X			
	row4	3 ₃	3 ₄		3 ₁	3 ₂				
	row5									X
	row6	≠	3 ₁₂		3 ₃₄	3				
	row7								X	
	row8				3 ₂	3 ₁₃₄				
	row9			X						

Pattern 4.027, continued.

A		
D	E	
	H	

Subpattern-5 begins in **(65)** with box order **E→H→D→A**

(65) zaps (85) adding **(84)**
(65) zaps (62) adding **(41)** and pending **(42)**
(41) zaps (11) adding **(12)**

Subpattern-5 = **(65),(84),(41),(12)**
 E H D A

4 B2	027	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1	3 ₁₂₄	3 ₃₅							
	row2							X		
	row3						X			
	row4	3 ₃₅	3 ₄		3 ₁	3 ₂				
	row5									X
	row6	p	3 ₁₂		3 ₃₄	3 ₅				
	row7								X	
	row8				3 ₂₅	3 ₁₃₄				
	row9			X						

Pattern 4.027, continued.

A		
D	E	
	H	

Box order is E→H→D→A

Due to pending situation in **D**, subpattern-6 must
 begin in same starting square **(65)** as subpattern-5
 share **(84)** with subpattern-5, as it lies between starting and pending boxes
 include the pending square **(62)**

(62) zaps (12) adding **(11)**

Subpattern-6 = **(65),(84),(62),(11)**

E H D A

Back at the starting box, nothing is pending and no squares are unclaimed. The pattern analysis is complete

4	027	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B2	row1	3 ₁₂₄₆	3 ₃₅							
	row2							X		
	row3						X			
	row4	3 ₃₅	3 ₄₆		3 ₁	3 ₂				
	row5									X
	row6	P	3 ₁₂		3 ₃₄	3 ₅₆				
	row7								X	
	row8				3 ₂₅₆	3 ₁₃₄				
	row9			X						

Pattern 4.026	Box Orientation	Patterns with the same box code
2 4-3-2 2	C D-A-G E	028, 033

A		C
D	E	
G		

Subpattern-1 starts in (51) with box order **D→E→A→C→G**

(51) zaps (55) adding (65)
(51) zaps (11) & (13) adding (12) zaps (18) adding (38)
(51) zaps (71) adding (73)

Subpattern-1 = (51),(65),(73),(38),(73)
D E A C G

4	026	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B3	row1	9	9 ₁						9	
	row2						X			
	row3	9							9 ₁	
	row4									X
	row5	9 ₁	9	9		9				
	row6			9		9 ₁				
	row7	9		9 ₁						
	row8							X		
	row9				X					

Pattern 4.026, continued.

A		C
D	E	
G		

Subpattern-2 starts in (52) with box order **D→E→A→C→G**

- (52) zaps (55) adding (65)
- (52) zaps (12) adding (11) and pending (31)
- (11) zaps (18) adding (38)
- (11) zaps (71) adding (73)

Subpattern-2 = (52),(65),(11),(38),(73)
 D E A C G

4	026	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B3	row1	9 ₂	9 ₁						9	
	row2						X			
	row3	9 ₃		P					9 ₁₂	
	row4									X
	row5	9 ₁	9 ₂	9		9				
	row6			9		9 ₁₂				
	row7	9		9 ₁₂						
	row8							X		
	row9				X					

Pattern 4.026, continued.

A		C
D	E	
G		

Subpattern-3 will keep the same box order **D→E→A→C→G**

Due to the pending situation in A, subpattern-3 must
 begin in the same starting square **(52)** as subpattern-2
 share **(65)** [between starting & pending boxes] with subpattern-2
 include the pending square **(31)**

(31) zaps (38) adding **(18)**

(31) zaps (71) adding **(73)**

Subpattern 3 = **(52),(65),(31),(18),(73)**

D E A C G

4	026	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B3	row1	9 ₂	9 ₁						9 ₃	
	row2						X			
	row3	9 ₃							9 ₁₂	
	row4									X
	row5	9 ₁	9 ₂₃	9		9				
	row6			9		9 ₁₂₃				
	row7	9		9 ₁₂₃						
	row8							X		
	row9				X					

Pattern 4.026, continued.

A		C
D	E	
G		

Subpattern-4 starts in (53) with box order **D→E→G→A→C**

(53) zaps (55) adding (65)
(53) zaps (73) adding (71) zaps (11) & (13) adding (12) zaps (18) adding (38)

Subpattern-4 = (53),(65),(71),(12),(38)

D E G A C

4		026	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B3		row1	9 ₂	9 ₁₄						9 ₃	
		row2						X			
		row3	9 ₃							9 ₁₂₄	
		row4									X
		row5	9 ₁	9 ₂₃	9 ₄		9				
		row6			9		9 ₁₂₃₄				
		row7	9 ₄		9 ₁₂₃						
		row8							X		
		row9				X					

Pattern 4.026, continued.

A		C
D	E	
G		

Subpattern-5 starts in **(63)** with box order **D→E→G→A→C**

(63) zaps (65) adding **(55)**

(63) zaps (73) adding **(71)** zaps (11)&(13) adding **(12)** zaps(18) adding **(38)**

Subpattern-5 = **(63)(55),(71),(12),(38)**

D E G A C

Back at the starting box D, nothing is pending and no squares are unclaimed.

The pattern analysis is complete.

4	026	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B3	row1	9 ₂	9 ₁₄₅						9 ₃	
	row2						X			
	row3	9 ₃							9 ₁₂₄₅	
	row4									X
	row5	9 ₁	9 ₂₃	9 ₄		9 ₅				
	row6			9 ₅		9 ₁₂₃₄				
	row7	9 ₄₅		9 ₁₂₃						
	row8							X		
	row9				X					

Pattern 4.017	Box Orientation	Patterns with the same box code
$\begin{array}{c} 3-2 \\ \\ 4-2 \\ \\ 2 \end{array}$	$\begin{array}{c} D-F \\ \\ H-G \\ \\ B \end{array}$	none

	B	
D		F
G	H	

Box order: **H→G→D→F→B**

Subpattern-1 starts in **(75)** zaps (72) adding **(81)** zaps (51)&(61) adding **(52)**
(52) zaps (58) adding **(68)**
(75) zaps (25) adding **(26)**

Subpattern-1 = **(75),(81),(52),(68),(26)**
H G D F B

4	017	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B4	row1									X
	row2					1	1 ₁			
	row3			X						
	row4				X					
	row5	1	1 ₁						1	
	row6	1							1 ₁	
	row7		1			1 ₁	1			
	row8	1 ₁				1	1			
	row9							X		

Pattern 4.017, continued.

	B	
D		F
G	H	

Box order: **H→G→D→F→B**

Subpattern-2 starts in **(76)** zaps (72) adding **(81)** zaps (61)&(51) adding **(52)**
(52) zaps (58) adding **(68)**
(76) zaps (26) adding **(25)**

Subpattern-2 = **(76),(81),(52),(68),(25)**
H G D F B

Subpattern-3 starts in **(85)** zaps (81) adding **(72)** zaps (52) adding **(51)** and pending **(61)**
(51) zaps (58) adding **(68)**
(85) zaps (25) adding **(26)**

Subpattern-3 = **(85),(72),(51),(68),(26)**
H G D F B

4	017	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B4	row1									X
	row2					1₂	1₁₃			
	row3			X						
	row4			P	X					
	row5	1₃	1₁₂						1	
	row6	1							1₁₂₃	
	row7		1₃			1₁	1₂			
	row8	1₁₂				1₃	1			
	row9							X		

Pattern 4.017, continued.

	B	
D		F
G	H	

Box order: **H→G→D→F→B**

Due to the pending condition in **D**, subpattern-4 must
begin in the same starting square **(85)** as subpattern-3
share **(72)** with subpattern-3 [between starting and pending boxes]
include the pending square **(61)**

(61) zaps (68) adding **(58)**

(85) zaps (25) adding **(26)**

Subpattern-4 = **(85),(72),(61),(58),(26)**

H→G→D→F→B

4		017	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B4		row1									X
		row2					1₂	1₁₃₄			
		row3			X						
		row4			P	X					
		row5	1₃	1₁₂						1₄	
		row6	1₄							1₁₂₃	
		row7		1₃₄			1₁	1₂			
		row8	1₁₂				1₃₄	1			
		row9							X		

Pattern 4.017, continued.

	B	
D		F
G	H	

Box order: **H→G→D→F→B**

Subpattern-5 starts in **(86)** zaps (81) adding **(72)** zaps (52) adding **(51)** and pending **(61)**
(51) zaps (58) adding **(68)**
(86) zaps (26) adding **(25)**

Subpattern-5 = **(86),(72),(51),(68),(25)**
H G D F B

4		017	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B4	row1										X
	row2					1 ₂₅	1 ₁₃₄				
	row3			X							
	row4				X						
	row5	1 ₃₅	1 ₁₂							1 ₄	
	row6	1 ₄		P						1 ₁₂₃₅	
	row7		1 ₃₄₅			1 ₁	1 ₂				
	row8	1 ₁₂				1 ₃₄	1 ₅				
	row9								X		

Pattern 4.017, continued.

	B	
D		F
G	H	

Box order: **H**→**G**→**D**→**F**→**B**

Due to the pending condition in **D**, subpattern-6 must
begin in the same starting square **(86)** as subpattern-5
share the same square **(72)** with subpattern-5 [between starting & pending boxes]
include the pending square **(61)**

(61) zaps (68) adding **(58)**

(86) zaps (26) adding **(25)**

Subpattern-6 = **(86),(72),(61),(58),(25)**

H G D F B

Back at the starting box H, nothing is pending & no boxes unclaimed. We are done.

4	017	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B4	row1									X
	row2					1 ₂₅₆	1 ₁₃₄			
	row3			X						
	row4				X					
	row5	1 ₃₅	1 ₁₂						1 ₄₆	
	row6	1 ₄₆		p					1 ₁₂₃₅	
	row7		1 ₃₄₅₆			1 ₁	1 ₂			
	row8	1 ₁₂				1 ₃₄	1 ₅₆			
	row9							X		

Pattern 4.023	Box Orientation	Patterns with the same box code
2 4-4-2 2	D I-F-C G	034

		C
D		F
G		I

Box order: F→C→I→G→D

Subpattern-1 starts in (57) zaps (17) adds (18)
[(18) zaps (78) & (88) and (57) zaps (77)] adding (89) zaps (82) adding (72)
(57) zaps (53) adding (63)

Subpattern-1 = (57),(18),(89),(72),(63)
F C I G D

4	023	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B5	row1							2	2 ₁	
	row2	X								
	row3					X				
	row4									
	row5			2				2 ₁	2	
	row6			2 ₁				2		2
	row7		2 ₁					2	2	
	row8		2						2	2 ₁
	row9				X					

Pattern 4.023, continued.

		C
D		F
G		I

Box order: F→C→I→G→D

Subpattern-2 starts in (58) zaps (18) adding (17)
(17) zaps (77) and (58) zaps (78) & (88) adding (89) zaps (82) adding (72)
(58) zaps (53) adding (63)

Subpattern-2 = (58),(17),(89),(72),(63)
F C I G D

Subpattern-3 starts in (67) zaps (17) adding (18)
(18) zaps (78) & (88) while (67) zaps (77) adding (89)
(89) zaps (82) adding (72)
(67) zaps (63) adding (53)

Subpattern-3 = (67),(18),(89),(72),(53)
F C I G D

4	023	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B5	row1							2 ₂	2 ₁₃	
	row2	X								
	row3					X				
	row4									
	row5			2 ₃				2 ₁	2 ₂	
	row6			2 ₁₂				2 ₃		2
	row7		2 ₁₂₃					2	2	
	row8		2						2	2 ₁₂₃
	row9				X					

Pattern 4.023, continued.

		C
D		F
G		I

Box order: F→C→I→G→D

Subpattern-4 starts in (69) zaps (19) adding (18) and pending (17)
(18) zaps (78) & (88) while (69) zaps (89) adding (77) zaps (72) adding (82)
(69) zaps (63) adding (53)

Subpattern-4 = (69),(18),(77),(82),(53)
F C I G D

4	023	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B5	row1							2 _{2p}	2 ₁₃₄	P ₁
	row2	X								
	row3					X				
	row4									
	row5			2 ₃₄				2 ₁	2 ₂	
	row6			2 ₁₂				2 ₃		2 ₄
	row7		2 ₁₂₃					2 ₄	2	
	row8		2 ₄						2 _p	2 ₁₂₃
	row9				X					P ₂

Pattern 4.023, continued.

		C
D		F
G		I

Box order: F→C→I→G→D

Due to the pending condition in **I**, subpattern-5 must
begin in the same starting square **(69)** as subpattern-4
include pending square **(17)**

(18) zaps **(78)** & **(88)** while **(69)** zaps **(89)** adding **(78)** and pending **(88)**

(78) zaps **(72)** adding **(82)**

(69) zaps **(63)** adding **(53)**

Subpattern-5 = **(69),(18),(78),(82),(53)**

F C I G D

4	023	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B5	row1							2 ₂₅	2 ₁₃₄	
	row2	X								
	row3					X				
	row4									
	row5			2 ₃₄₅				2 ₁	2 ₂	
	row6			2 ₁₂				2 ₃		2 ₄₅
	row7		2 ₁₂₃					2 ₄	2 ₅	
	row8		2 ₄₅						2	2 ₁₂₃
	row9				X					P ₂

Pattern 4.023, continued.

		C
D		F
G		I

Box order: F→C→I→G→D

Due to the pending condition in **I**, subpattern-6 must
begin in the same starting square **(69)** as subpattern-5
share square **(17)** with subpattern-5 [between starting and pending boxes]
include the pending square **(88)**

(88) zaps (82) adding **(72)**

(69) zaps (63) adding **(53)**

Subpattern-6 = **(69),(17),(88),(72),(53)**

F C I G D

Back at the starting box F, nothing is pending and no squares are unclaimed. The pattern analysis is complete.

4	023	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B5										
row1								2 ₂₅₆	2 ₁₃₄	
row2		X								
row3						X				
row4										
row5				2 ₃₄₅₆				2 ₁	2 ₂	
row6				2 ₁₂				2 ₃		2 ₄₅₆
row7			2 ₁₂₃₆					2 ₄	2 ₅	
row8			2 ₄₅						2 ₆	2 ₁₂₃
row9					X					P ₂

Pattern 4.021	Box Orientation	Patterns with the same box code
$\begin{array}{c} 4-2 \\ \\ 3-2 \\ \\ 2 \end{array}$	$\begin{array}{c} A-B \\ \\ F-D \\ \\ I \end{array}$	none

A	B	
D		F
		I

Box order: **A→B→D→F→I**

Subpattern-1 begins in **(11)** zaps (14) adding **(24)**
(11) zaps (61) adding **(43)** zaps (49) adding **(68)** and pending **(69)**
(68) zaps (88) adding **(89)**

Subpattern-1 = **(11),(24),(43),(68),(89)**
A B D F I

4	021	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B6	row1	4 ₁		4	4					
	row2	4		4	4 ₁					
	row3							X		
	row4			4 ₁						4
	row5					X				P
	row6	4							4 ₁	4 _p
	row7		X							
	row8								4	4 ₁
	row9						X			

Pattern 4.021, continued.

A	B	
D		F
		I

Box order: **A→B→D→F→I**

Due to the pending condition in **A**, subpattern-2 must
begin in the same starting square **(11)** as subpattern-1
share the same squares **(24)**, **(43)**, between starting and pending boxes
include the pending square **(69)**

(69) zaps (89) adding **(88)**

Subpattern-2:= **(11),(24),(43),(69),(88)**
A B D F I

4		021	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B6	row1		4 ₁₂		4	4					
	row2		4		4	4 ₁₂					
	row3								X		
	row4				4 ₁₂						4
	row5						X				P
	row6		4							4 ₁	4 ₂
	row7			X							
	row8									4 ₂	4 ₁
	row9							X			

Pattern 4.021, continued.

A	B	
D		F
		I

Box order: A→B→D→F→I

Subpattern-3 begins in (13) zaps (14) adding (24)
(13) zaps (61) adding (43) zaps (68) & (69) adding (49) zaps (89) adding (88)

Subpattern-3 = (13),(24),(43),(49),(88)

		A	B	D	F	I				
4	021	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B6	row1	4 ₁₂		4 ₃	4					
	row2	4		4	4 ₁₂₃					
	row3							X		
	row4			4 ₁₂						4 ₃
	row5					X				
	row6	4 ₃							4 ₁	4 ₂
	row7		X							
	row8								4 ₂₃	4 ₁
	row9						X			

Pattern 4.021, continued.

A	B	
D		F
		I

Box order: **A**→**B**→**D**→**F**→**I**

Subpattern-4 begins in **(21)** zaps **(24)** adding **(14)**

(21) zaps **(61)** adding **(43)** zaps **(49)** adding **(68)** and pending **(69)**

(68) zaps **(88)** adding **(89)**

Subpattern-4 = **(21),(14),(43),(68),(89)**

A B D F I

Due to the pending condition in **F**, subpattern-5 must

start in the same square **(21)** as subpattern-4

share squares **(14)** & **(43)** with subpattern-4 [all squares betw start & pend boxes]

include pending square **(69)**

(69) zaps **(89)** adding **(88)**

Subpattern-5 = **(21),(14),(43),(69),(88)**

A B D F I

4	021	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B6	row1	4 ₁₂		4 ₃	4 ₄₅					
	row2	4 ₄₅		4	4 ₁₂₃					
	row3							X		
	row4			4 ₁₂₄₅						4 ₃
	row5					X				P
	row6	4 ₃							4 ₁₄	4 ₂₅
	row7		X							
	row8								4 ₂₃₅	4 ₁₄
	row9						X			

Pattern 4.021, continued.

A	B	
D		F
		I

Box order: **A**→**B**→**D**→**F**→**I**

Subpattern-6 starts in **(23)** zaps (24) adding **(14)**

(23) zaps (43) adding **(61)** zaps (68) & (69) adding **(49)** zaps (89) adding **(88)**

Subpattern-6 = **(23),(14),(61),(49),(88)**

Back at the starting box A, nothing is pending and no squares are unclaimed, so the pattern analysis is complete.

4	021	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B6	row1	4 ₁₂		4 ₃	4 ₄₅₆					
	row2	4 ₄₅		4 ₆	4 ₁₂₃					
	row3							X		
	row4			4 ₁₂₄₅						4 ₃₆
	row5					X				
	row6	4 ₃₆							4 ₁₄	4 ₂₅
	row7		X							
	row8								4 ₂₃₅₆	4 ₁₄
	row9						X			

Pattern 4.029	Box Orientation	Patterns with the same box code
4 - 2 - 2	G - D - A	none
2 - 3	E - H	

A		
D	E	
G	H	

Subpattern-1 begins in (71) with box order G→A→D→H→E

(71) zaps (21) adding (22)
(71) zaps (61) adding (63)
(71) zaps (74) & (76) adding (94) zaps (54) adding (56)

Subpattern-1 = (71).(22).(64).(94).(56)

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
4 029									
B7 row1								X	
row2	8	8 ₁							
row3					X				
row4									X
row5				8		8 ₁			
row6	8		8 ₁						
row7	8 ₁	8	8	8		8			
row8							X		
row9			8	8 ₁					

Pattern 4.029, continued.

A		
D	E	
G	H	

Subpattern-2 begins in (72) with box order $G \rightarrow A \rightarrow D \rightarrow H \rightarrow E$

(72) zaps (22) adding (21) zaps (61) adding (63)

(72) zaps (74) & (76) adding (54) zaps (74) & (94) adding (76)

Subpattern-2 = (72),(21),(63),(54),(76)

G A D H E

Subpattern-3 begins in (73) with box order $G \rightarrow D \rightarrow A \rightarrow H \rightarrow E$

(73) zaps (63) adding (61) zaps (21) adding (22)

(73) zaps (74) & (76) adding (94) zaps (54) adding (56)

Subpattern-3 = (73),(61),(22),(94),(56)

G A D H E

		col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
4	029									
B7	row1								X	
	row2	8 ₂	8 ₁₃₄₅							
	row3					X				
	row4									X
	row5				8 ₄		8 ₁₂₃₅			
	row6	8 ₃₄₅		8 ₁₂						
	row7	8 ₁	8 ₂	8 ₃	8 ₅		8 ₄			
	row8							X		
	row9			8 ₄₅	8 ₁₂₃					

Pattern 4.029, continued.

A		
D	E	
G	H	

box order is $G \rightarrow D \rightarrow A \rightarrow H \rightarrow E$

Subpattern-4 begins in **(93)** zaps (63) adding **(61)** zaps (21) adding **(22)**
(93) zaps (94) adding (74) and pending **(76)**

Subpattern-4 = **(93),(61),(22),(94),(56)**
G D A H E

Due to the pending condition in **H**, subpattern-5 must
begin in the same starting square **(93)** as subpattern-4
share squares **(61)**& **(22)** with subpattern-5 [between starting & pending boxes]
include the pending square **(76)**
(76) zaps (56) adding **(54)**

Subpattern-5 = **(93),(61),(22),(76),(54)**
G D A H E

Back at the starting box, nothing is pending & no squares unclaimed. We are done.

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
4 029									
B7 row1								X	
row2	8 ₂	8 ₁₃₄₅							
row3					X				
row4									X
row5				8 ₅		8 ₁₂₃₄			
row6	8 ₃₄₅		8 ₁₂						
row7	8 ₁	8 ₂	8 ₃	8 ₄		8 ₅			
row8					P		X		
row9			8 ₄₅	8 ₁₂₃					

Pattern 4.024	Box Orientation	Patterns with the same box code
2 - 4	I - G	none
3 - 2 - 2	D - E - F	

D	E	F
G		I

Box order: G→I→D→E→F

Subpattern-1 is begun in (72) zaps (77) adding (87)
 (72) zaps (62) & (42) adding (53) zaps (56) adding (46)
 (46) zaps (48) adding (68)
 (72) zaps (77) adding (87)

Subpattern-1 = (72),(87),(53),(46),(68)
 G I D E F

4	024	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B8										
row1				X						
row2										X
row3		X								
row4		6				6 ₁		6		
row5			6 ₁			6				
row6		6						6 ₁		
row7		6 ₁	6				6			
row8		6	6				6 ₁			
row9					X					

Pattern 4.024, continued.

D	E	F
G		I

Box order: G→I→D→F→E

Subpattern-2 begins in (73) zaps (77) adding (87)

(73) zaps (53) adding (42) and pending (62)

(42) zaps (46) adding (56)

(42) zaps (48) adding (68)

Subpattern-2 = (73),(87),(42),(68),(56)

G I D F E

Due to the pending situation in D, subpattern-3 must

begin in the same starting square (73) as subpattern-2

share square (87) with subpattern-2 [between starting & pending boxes]

include the pending square (62)

(62) zaps (68) adding (48) zaps (46) adding (56)

Subpattern-3 = (73),(87),(42),(48),(56)

G I D F E

4	024	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B8	row1				X					
	row2									X
	row3	X								
	row4		6 ₂				6 ₁		6 ₃	
	row5	P		6 ₁			6 ₂₃			
	row6		6 ₃						6 ₁₂	
	row7		6 ₁	6 ₂₃				6		
	row8		6	6				6 ₁₂₃		
	row9					X				

Pattern 4.024, continued.

D	E	F
G		I

Box order: G→I→D→F→E

Subpattern-4 starts in **(82)** zaps (87) adding **(77)**
(82) zaps (62) & (42) adding **(53)** zaps (56) adding **(46)** zaps (48) adding **(68)**

Subpattern-4 = **(82),(77),(53),(46),(68)**
G I D F E

Subpattern-5 starts in **(83)** zaps (87) adding **(77)**
(83) zaps (53) adding **(42)** and pending **(62)**
(42) zaps (48) adding **(68)**
(42) zaps (46) adding **(56)**

Subpattern-5 = **(83),(77),(42),(68),(56)**
G I D F E

4	024	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B8	row1				X					
	row2									X
	row3	X								
	row4		6 ₂₅				6 ₁₄		6 ₃	
	row5			6 ₁₄			6 ₂₃₅			
	row6		6 ₃	P					6 ₁₂₄₅	
	row7		6 ₁	6 ₂₃				6 ₄₅		
	row8		6 ₄	6 ₅				6 ₁₂₃		
	row9					X				

Pattern 4.024, continued.

D	E	F
G		I

Box order: G→I→D→F→E

Due to the pending condition in **D**, subpattern-6 must

begin in the same starting square **(83)** as subpattern-5

share **(77)** with subpattern-5 [all squares between starting & pending boxes]

include the pending square **(62)**

(62) zaps **(68)** adding **(48)** zaps **(46)** adding **(56)**

Subpattern-6 = **(83),(77),(62),(48),(56)**

G I D F E

Back at the starting box G, nothing is pending, and no squares are unclaimed.

The pattern analysis is complete.

4	024	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B8										
row1				X						
row2										X
row3		X								
row4		6 ₂₅					6 ₁₄		6 ₃₆	
row5			6 ₁₄				6 ₂₃₅₆			
row6		6 ₃₆	P						6 ₁₂₄₅	
row7		6 ₁	6 ₂₃					6 ₄₅₆		
row8		6 ₄	6 ₅₆					6 ₁₂₃		
row9					X					

Pattern 4.025	Orientation	Patterns with the same box code
4 – 3	C – B	032
3 – 3	I – H	

	B	C
	H	I

Box order: C→B→H→I

Subpattern-1 begins in **(17)** zaps (15) adding **(25)** and pending **(26)**

(25) zaps (75) & (95) adding **(76)**

(76) zaps (79) while **(17)** zaps (97) adding **(99)**

Subpattern-1 = **(17),(25),(76),(99)**

C B H I

4	025	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C2	row1					7		7 ₁₂		7
	row2				P ₁	7 ₁	7 ₂	7		7
	row3		X							
	row4			X						
	row5								X	
	row6				X					
	row7					7 ₂	7 ₁			7
	row8	X			P ₂					
	row9					7 _p		7 ₂		7 ₁

Pattern 4.025, continued.

	B	C
	H	I

Box order: C→B→H→I

Due to the pending condition in H, subpattern-2 must
begin in the same starting squjare **(17)** as subpattern-1
include the pending square **(26)**

(26) zaps (76) adding **(75)** and pending **(76)**
(75) zaps (79) while **(17)** zaps (97) adding **(97)**

Subpattern-2 = **(17),(26),(75),(97)**
C B H I

4	025	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C2	row1					7		7 ₁₂		7
	row2				P ₁	7 ₁	7 ₂	7		7
	row3		X							
	row4			X						
	row5								X	
	row6				X					
	row7					7 ₂	7 ₁			7
	row8	X			P ₂					
	row9					7 _p		7 ₂		7 ₁

Pattern 4.025, continued.

	B	C
	H	I

Box order: C→B→H→I

Due to the pending condition in H, subpattern-3 must
 start in the same square **(17)** as subpattern-2
 share **(26)** with subpattern-2 [between starting & pending squares]
 include the pending square **(95)**

(95) zaps **(97)** & **(99)** adding **(79)**

Subpattern-3 = **(17),(26),(95),(79)**
 C B H I

Subpattern-4 begins in **(19)** zaps **(15)** adding **(25)** and pending **(26)**
(25) zaps **(75)** & **(95)** adding **(76)**
(19) zaps **(79)** & **(99)** adding **(97)**

Subpattern-4 = **(19),(25),(76),(97)**
 C B H I

4	025	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C2	row1					7		7 ₁₂₃		7 ₄
	row2					7 ₁₄	7 _{23P}	7		7
	row3		X		P₄					
	row4			X						
	row5								X	
	row6				X					
	row7					7 ₂	7 ₁₄			7 ₃
	row8	X			P₂					
	row9					7 ₃		7 ₄		7 ₁₂

Pattern 4.025, continued.

	B	C
	H	I

Box order: C→B→H→I

Due to the pending condition in B, subpattern-5 must
start in the same square **(19)** as subpattern-4
include the pending square **(26)**

(26) zaps (76) adding **(75)** and pending **(95)**
(19) zaps (79) & (99) adding **(97)**

Subpattern-5 = **(19),(26),(75),(97)**
C B H I

4		025	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C2		row1					7		7 ₁₂₃		7 ₄₅
		row2				P ₄	7 ₁₄	7 ₂₃₅	7		7
		row3		X							
		row4			X						
		row5								X	
		row6				X					
		row7					7 ₂₅	7 ₁₄			7 ₃
		row8	X			P ₅					
		row9					7 ₃		7 ₄₅		7 ₁₂

Pattern 4.025, continued.

	B	C
	H	I

Box order: C→B→H→I

Due to the pending condition in **H**, subpattern-6 must
 begin in the same square **(19)** as subpattern-5
 share **(26)** with subpattern-5]between starting & pending boxes]
 include the pending square **(95)**

(95) zaps (97) & (99) adding (79)

But now, two squares of subpattern-6 [(19) & (79)] are in the same column. This is a violation of sudoku rules. Therefore we cannot begin subpattern-6 in (19), but must choose a square in row 2 of box C for the beginning of subpattern-6.

4	025	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C2	row1					7		7 ₁₂₃		7 ₄₅₆
	row2				P ₄	7 ₁₄	7 ₂₃₅₆	7		7
	row3		X							
	row4			X						
	row5								X	
	row6				X					
	row7					7 ₂₅	7 ₁₄			7 ₃₆
	row8	X			P ₅					
	row9					7 ₃₆		7 ₄₅		7 ₁₂

Pattern 4.025, continued.

	B	C
	H	I

Because subpattern-6, as well as any ensuing subpatterns, will all start in row 2, their continuations must all be in square (15), which is in the same column as the pending P in square (95). This means that square (95) cannot be a member of any future subpatterns, so we shall erase the pending P in square (95) before continuing any further. See the next page for the continuation of this pattern analysis. Due to the erasure of the pending P in square (95), there is no longer a pending situation for subpattern-6 to be affected by. The sudoku below is as it was before beginning subpattern-6, except for the erasures of the pending P in box H and the pending subscript in square (95). It is from this point that we shall, on the next page, develop the correct subpattern-6.

4	025	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C2	row1					7		7 ₁₂₃		7 ₄₅
	row2					7 ₁₄	7 ₂₃₅	7		7
	row3		X							
	row4			X						
	row5								X	
	row6				X					
	row7					7 ₂₅	7 ₁₄			7 ₃
	row8	X								
	row9					7 ₃		7 ₄₅		7 ₁₂

Pattern 4.025, continued.

	B	C
	H	I

Box order: C→B→H→I

Subpattern-6 is begun anew in square **(27)**

(27) zaps **(25)** & **(26)** adding **(15)** zaps **(75)** & **(95)** adding **(76)**

(76) zaps **(79)** while **(27)** zaps **(97)** adding **(99)**

Subpattern-6 = **(27),(15),(76),(99)**

C B H I

Subpattern-7 is begun in **(29)** zaps **(25)** & **(26)** adding **(15)**

(15) zaps **(75)** & **(95)** adding **(76)**

(29) zaps **(79)** & **(99)** adding **(97)**

Subpattern-7 = **(29),(15),(76),(97)**

C B H I

At the starting box C, nothing is pending and no squares are unclaimed. Done.

4	025	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C2	row1					7 ₆₇		7 ₁₂₃		7 ₄₅
	row2					7 ₁₄	7 ₂₃₅	7 ₆		7 ₇
	row3		X							
	row4			X						
	row5								X	
	row6				X					
	row7					7 ₂₅	7 ₁₄₆₇			7 ₃
	row8	X								
	row9					7 ₃		7 ₄₅₇		7 ₁₂₆

Pattern 4.012	Orientation	Patterns with the same box code
$\begin{array}{c} 2 \\ \\ 4-3-2 \\ \\ 2 \end{array}$	$\begin{array}{c} H \\ \\ A-G-D \\ \\ B \end{array}$	none

A	B	
D		
G	H	

Box order: A→B→G→H→D

Subpattern-1 starts in **(11)** zaps (15) adding **(35)**
(11) zaps (81) adding **(83)** and pending **(93)**
(83) zaps (43) adding **(42)**

Subpattern-1 = **(11),(35),(83),(94),(42)**
A B G H D

4	012	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		8 ₁	8			8				
row2									X	
row3			8	8		8 ₁				
row4			8 ₁	8						
row5								X		
row6							X			
row7		P ₁								X
row8		8		8 ₁	8					
row9				8 _P	8 ₁					

Pattern 4.012, continued.

A	B	
D		
G	H	

Box order: A→B→G→H→D

Due to the pending situation in G, subpattern-2 must
start in the same square (11)
share (42) with subpattern-1 [between starting & pending boxes]
include pending square (93)

(11) zaps (15) adding (35)

(93) zaps (94) adding (84)

Subpattern-2 = (11),(35),(93),(84),(42)

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	8 ₁₂	8			8				
row2								X	
row3		8	8		8 ₁₂				
row4		8 ₁₂	8						
row5							X		
row6						X			
row7		P ₁							X
row8	8		8 ₁	8 ₂					
row9			8 ₂	8 ₁					

Pattern 4.012, continued.

A	B	
D		
G	H	

Box order: A→B→D→G→H

Subpattern-3 starts in (12) zaps (15) adding (35)
(12) zaps (42) adding (43) zaps (83) & (93) adding (82) zaps (84) adding (94)
Subpattern-2 = (12),(35),(43),(82),(94)
A B D G H

Subpattern-4 starts in (32) zaps (35) adding (15)
(32) zaps (42) adding (43) zaps (83) & (93) adding (81) zaps (84) adding (94)
Subpattern-4 = (32),(15),(43),(81),(94)
A B D G H

4 012	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C3									
row 1	8 ₁₂	8 ₃			8				
row 2								X	
row 3		8	8		8 ₁₂₃				
row 4		8 ₁₂	8 ₃						
row 5							X		
row 6						X			
row 7									X
row 8	8 ₃		8 ₁	8 ₂					
row 9			8 ₂	8 ₁₃					

Pattern 4.012, continued.

A	B	
D		
G	H	

Box order: A→B→D→G→H

Subpattern-5 begins in (33) zaps (35) adding (15)
(33) zaps (43) adding (42)
(33) zaps (83) & (93) adding (81) zaps (84) adding (94)

Subpattern-5 = (33),(15),(42),(81),(94)
A B D G H

Back at the starting box A, nothing is pending and no squares are unclaimed, so the pattern analysis is complete.

4 012	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C3									
row 1	8 ₁₂	8 ₃			8 ₄₅				
row 2								X	
row 3		8 ₄	8 ₅		8 ₁₂₃				
row 4		8 ₁₂₅	8 ₃₄						
row 5							X		
row 6						X			
row 7									X
row 8	8 ₃₄₅		8 ₁	8 ₂					
row 9			8 ₂	8 ₁₃₄₅					

Pattern 4.002	Orientation	Patterns with the same box code
4 – 3 – 2	E – F – D	none
2 – 2	H – I	
2	B	

	B	
D	E	F
	H	I

Subpattern-1 starts in (45) with box order E→D→F→I→H→B

(45) zaps (43) adding (63)
(45) zaps (47) while (63) zaps (67) adding (58) zaps (78) adding (97)
(97) zaps (95) adding (76) zaps (36) adding (34)

Subpattern-1 = (45),(63),(58),(97),(76),(34)
 E D F I H B

4	002	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1		X							
	row2									X
	row3				4 ₁		4			
	row4			4		4 ₁		4		
	row5				4		4		4 ₁	
	row6			4 ₁		4		4		
	row7						4 ₁		4	
	row8	X								
	row9					4		4 ₁		

Pattern 4.002, continued.

	B	
D	E	F
	H	I

Box order: **E→B→H→I→F→D**

Subpattern-2 starts in **(54)** zaps (34) adding **(36)** zaps (76) adding **(95)**
(95) zaps (97) adding **(78)** zaps (58) adding **(47)** and pending **(67)**
(47) zaps (43) adding **(63)**

Subpattern-2 = **(54),(36),(95),(78),(47),(63)**
E B H I F D

4 002	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C0									
row 1		X							
row 2									X
row 3				4 ₁		4 ₂			
row 4			4		4 ₁		4 ₂		<i>P</i> ₂
row 5				4 ₂		4		4 ₁	
row 6			4 ₁₂		4		4 _p		
row 7						4 ₁		4 ₂	
row 8	X								
row 9					4 ₂		4 ₁		

Pattern 4.002, continued.

	B	
D	E	F
	H	I

Box order: **E→B→H→I→F→D**

Due to the pending condition in F, subpattern-3 must

begin in the same square **(54)** as subpattern-2

share **(36), (95), (78)** with subpattern-2 [between starting & pending boxes]

include pending square **(67)**

(67) zaps (63) adding **(43)**

Subpattern-3 = **(54),(36),(95),(78),(67),(43)**

E B H I F D

4 002	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C0									
row 1		X							
row 2									X
row 3				4_1		4_{23}			
row 4			4_3		4_1		4_2		P_2
row 5				4_{23}		4		4_1	
row 6			4_{12}		4		4_3		
row 7						4_1		4_{23}	
row 8	X								
row 9					4_{23}		4_1		

Pattern 4.002, continued.

	B	
D	E	F
	H	I

Box order: **E→B→H→I→F→D**

Subpattern-4 begins in **(56)** zaps (36) adding **(34)**
(56) zaps (76) adding **(95)** zaps (97) adding **(78)** zaps (58) adding **(47)** and pending **(67)**
(47) zaps (43) adding **(63)**

Subpattern-4 = **(56),(34),(95),(78),(47),(63)**
E B H I F D

4 002	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C0									
row 1		X							
row 2									X
row 3				4 ₁₄		4 ₂₃			
row 4			4 ₃		4 ₁		4 ₂₄		
row 5				4 ₂₃₄		4 ₄		4 ₁	
row 6			4 ₁₂		4		4 ₃		<i>P</i> ₄
row 7						4 ₁		4 ₂₃₄	
row 8	X								
row 9					4 ₂₃₄		4 ₁		

Pattern 4.002, continued.

	B	
D	E	F
	H	I

Box order for subpatterns 2 to 5: **E→B→H→I→F→D**

Due to the pending condition in F, subpattern-5 must
 start in the same square **(56)** as subpattern-4
 share **(34)**, **(95)**, **(78)** with subpattern-4 [between starting & pending boxes]
 include the pending square **(67)**

(67) zaps (63) adding **(43)**

Subpattern-5 = **(56),(34),(95),(78),(67),(43)**

E B H I F D

4 002	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C0									
row 1		X							
row 2									X
row 3				4 ₁₄₅		4 ₂₃			
row 4			4 ₃₅		4 ₁		4 ₂₄		
row 5				4 ₂₃₄		4 ₄₅		4 ₁	
row 6			4 ₁₂		4		4 ₃₅		<i>P</i> ₄
row 7						4 ₁		4 ₂₃₄₅	
row 8	X								
row 9					4 ₂₃₄₅		4 ₁		

Pattern 4.002, continued.

	B	
D	E	F
	H	I

Subpattern-6 starts in **(65)** with box order **E→D→F→I→H→B**

(65) zaps (63) adding **(43)**

(43) zaps (47) while **(65)** zaps (67) adding **(58)** zaps (78) adding **(97)**

(97) zaps (95) adding **(76)** zaps (36) adding **(34)**

Subpattern-6 = **(65),(43),(58),(97),(76),(34)**

E D F I H B

Back at the starting box E, nothing is pending and no squares are unclaimed, so the pattern analysis is complete.

4 002	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C0									
row 1		X							
row 2									X
row 3				4 ₁₄₅₆		4 ₂₃			
row 4			4 ₃₅₆		4 ₁		4 ₂₄		
row 5				4 ₂₃₄		4 ₄₅		4 ₁₆	
row 6			4 ₁₂		4 ₆		4 ₃₅		
row 7						4 ₁₆		4 ₂₃₄₅	
row 8	X								
row 9					4 ₂₃₄₅		4 ₁₆		

Pattern 4.005	Orientation	Patterns with the same box code
4 – 3 – 2	I – C – F	none
2 – 3	G – A	

A		C
		F
G		I

Subpattern-1 starts in (77) with box order I→F→C→G→A

(77) zaps (67) adding (69) zaps (19) & (29) adding (18)
(77) zaps (73) adding (91) zaps (11) & (21) adding (23)

Subpattern-1 = (77),(69),(18),(91),(23)
 I F C G A

4 005	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C4									
row 1	2							2 ₁	2
row 2	2		2 ₁						2
row 3					X				
row 4		X							
row 5				X					
row 6							2		2 ₁
row 7			2				2 ₁	2	
row 8						X			
row 9	2 ₁							2	2

Pattern 4.005, continued.

A		C
		F
G		I

Subpattern-2 starts in **(78)** with box order **I→G→A→C→F**

(78) zaps (73) adding **(91)** zaps (11) & (21) adding **(23)**
(23) zaps (29) while **(78)** zaps (18) adding **(19)** zaps (69) adding **(61)**

Subpattern-2 = **(78),(91),(23),(19),(61)**
I G A C F

4 005	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C4									
row 1	2							2 ₁	2 ₂
row 2	2		2 ₁₂						2
row 3					X				
row 4		X							
row 5				X					
row 6							2 ₂		2 ₁
row 7			2				2 ₁	2 ₂	
row 8						X			
row 9	2 ₁₂							2	2

Pattern 4.005, continued.

A		C
		F
G		I

Subpattern-3 starts in **(98)** with box order **I→G→A→C→F**

(98) zaps (91) adding **(73)** zaps (23) adding **(11)** and pending **(21)**

(11) zaps (18) & (19) adding **(29)** zaps (69) adding **(67)**

Subpattern-3 = **(98),(73),(11),(29),(67)**

I G A C F

4 005	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C4									
row 1	2 ₃							2 ₁	2 ₂₄
row 2	2 ₄		2 ₁₂						2 ₃
row 3		P ₃			X				
row 4		X							
row 5				X					
row 6							2 ₂₃₄		2 ₁
row 7			2 ₃₄				2 ₁	2 ₂	
row 8						X			
row 9	2 ₁₂							2 ₃₄	2

Pattern 4.005, continued.

A		C
		F
G		I

Box order for subpattern-4: **I→G→A→C→F**

Due to the pending condition in **A**, subpattern-4 must
start in the same square **(98)** as subpattern-3
share **(71)** with subpattern-3 [between starting & pending boxes]
include the pending square **(21)**

(21) zaps (29) while **(98)** zaps (18) adding **(19)** zaps (69) adding **(67)**

Subpatten-4 = **(98),(71),(21),(19),(67)**
 I G A C F

4 005	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C4									
row 1	2 ₃							2 ₁	2 ₂₄
row 2	2 ₄		2 ₁₂						2 ₃
row 3					X				
row 4		X							
row 5				X					
row 6							2 ₂₃₄		2 ₁
row 7			2 ₃₄				2 ₁	2 ₂	
row 8						X			
row 9	2 ₁₂							2 ₃₄	2

Pattern 4.005, continued.

A		C
		F
G		I

Subpattern-5 starts in **(99)** with box order **I→F→C→G→A**

(99) zaps (69) adding **(67)**

(99) zaps (19) & (29) adding **(18)**

(99) zaps (91) adding **(73)**

(73) zaps (23) while **(18)** zaps (11) adding **(21)**

Subpattern-5 = **(99),(67),(18),(73),(21)**

I F C G A

Back at the starting box I, nothing is pending and no squares are unclaimed. The pattern analysis is complete.

4 005	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C4									
row 1	2 ₃							2 ₁₅	2 ₂₄
row 2	2 ₄₅		2 ₁₂						2 ₃
row 3					X				
row 4		X							
row 5				X					
row 6							2 ₂₃₄₅		2 ₁
row 7			2 ₃₄₅				2 ₁	2 ₂	
row 8						X			
row 9	2 ₁₂							2 ₃₄	2 ₅

Pattern 4.018	Orientation	Patterns with the same box code
4 – 2 – 3	B – E – H	none
2 – 3	C – F	

	B	C
	E	F
	H	

Subpattern-1 begins in (24) with box order **B→E→H→C→F**

- (24) zaps (64) adds (55)
- (24) zaps (74) while (55) zaps (75) adding (76)
- (24) zaps (28) adding (39) zaps (55) & (65) adding (68)

Subpattern-1 = (24),(55),(76),(39),(68)
 B E H C F

4	018	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C5	row1	X								
	row2				9 ₁				9 ₂	
	row3				9 ₂	9	9			9 ₁
	row4		X							
	row5					9 ₁₂				9
	row6				9				9 ₁	9 ₂
	row7				9	9	9 ₁₂			
	row8			X						
	row9							X		

Pattern 4.018, continued.

	B	C
	E	F
	H	

Subpattern-2 begins in **(34)** with box order **B→E→H→C→F**

- (34)** zaps (64) adding **(55)**
- (34)** zaps (74) while **(55)** zaps (75) adding **(76)**
- (34)** zaps (39) adding **(28)**
- (28)** zaps (68) while **(55)** zaps (59) adding **(69)**

Subpattern-2 = **(34),(55),(76),(28),(69)**
 B E H C F

4	018	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C5	row1	X								
	row2				9 ₁				9 ₂	
	row3				9 ₂	9	9			9 ₁
	row4		X							
	row5					9 ₁₂				9
	row6				9				9 ₁	9 ₂
	row7				9	9	9 ₁₂			
	row8			X						
	row9							X		

Pattern 4.018, continued.

	B	C
	E	F
	H	

Subpattern-3 starts in **(35)** with box order **B→E→F→C→H**

(35) zaps **(55)** adding **(64)** zaps **(68)** & **(69)** adding **(59)** zaps **(39)** adding **(28)**
(35) zaps**75)** while **(64)** zaps **(74)** adding **(76)**

Subpattern-3 = **(35),(64),(59),(28),(76)**
B E F C H

Subpattern-4 starts in **(36)** with box order **B→H→E→C→F**

(36) zaps **(76)** adding **(74)** and pending **(75)**
(74) zaps **(64)** adding **(55)**
(36) zaps **(39)** adding **(28)**
(28) zaps **(68)** while **(55)** zaps **(59)** adding **(69)**

Subpattern-4 = **(36),(74),(55),(28),(69)**
B H E C F

4 C5	018	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1	X								
	row2				9 ₁				9 ₂₃₄	
	row3				9 ₂	9 ₃	9 ₄			9 ₁
	row4		X							
	row5					9 ₁₂₄				9 ₃
	row6				9 ₃				9 ₁	9 ₂₄
	row7				9 ₄	9 _P	9 ₁₂₃			
	row8			X		P				
	row9							X		

Pattern 4.018, continued.

	B	C
	E	F
	H	

Box order for subpattern-5: **B→H→E→F→C**

Due to the pending condition in **H**, subpattern-5 must start in the same square **(36)** as subpattern-4 include the pending square **(75)**

(75) zaps (55) adding **(64)** zaps (68) & (69) adding **(59)**

(36) zaps (39) adding **(28)**

Subpattern-5 = **(36),(75),(64),(59),(28)**

B H E F C

Back at the starting box B, nothing pending & no squares unclaimed. Done.

4	018	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C5	row1	X								
	row2				9 ₁				9 ₂₃₄₅	
	row3				9 ₂	9 ₃	9 ₄₅			9 ₁
	row4		X							
	row5					9 ₁₂₄				9 ₃₅
	row6				9 ₃₅				9 ₁	9 ₂₄
	row7				9 ₄	9 ₅	9 ₁₂₃			
	row8			X		P				
	row9							X		

Pattern 4.006	Orientation	Patterns with the same box code
$ \begin{array}{c} 2-2 \\ \\ 4-3-2 \\ \\ 2 \end{array} $	$ \begin{array}{c} C-B \\ \\ H-G-I \\ \\ D \end{array} $	none

	B	C
D		
G	H	I

Box order: H→I→G→D→B→C

Subpattern-1 begins in (75) zaps (79) adding (89)
 (89) zaps (81) while (75) zaps (73) adding (93)
 (93) zaps (53) adding (51)
 (75) zaps (15) adding (26) zaps (28) adding (18)

Subpattern-1 = (75),(89),(93),(51),(26),(18)
 H I G D B C

4	006	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					5				5 ₁	
row2						5 ₁			5	
row3		X								
row4								X		
row5		5 ₁		5						
row6				X						
row7			5		5 ₁	5				5
row8		5				5				5 ₁
row9			5 ₁		5					

Pattern 4.006, continued.

	B	C
D		
G	H	I

Box order: H→I→G→D→B→C

Subpattern-2 begins in **(75)** zaps (79) adding **(89)**
(89) zaps (81) while **(75)** zaps (73) adding **(93)**
(93) zaps (53) adding **(51)**
(75) zaps (15) adding **(26)** zaps (28) adding **(18)**

Subpattern-2 = **(75),(89),(93),(51),(26),(18)**
H I G D B C

4 006	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C6									
row 1					5 ₂			5 ₁	
row 2						5 ₁		5 ₂	
row 3		X							
row 4							X		
row 5	5 ₁₂		5						
row 6				X					
row 7			5		5 ₁	5 ₂			5
row 8	5					5			5 ₁₂
row 9			5 ₁₂		5				

Pattern 4.006, continued.

	B	C
D		
G	H	I

Box order: H→I→G→D→B→C

Subpattern-3 begins in (86) zaps (89) adding (79)
(79) zaps (73) while (86) zaps (81) adding (93)
(93) zaps (53) adding (51)
(86) zaps (26) adding (15) zaps (18) adding (28)

Subpattern-3 = (86),(79),(93),(51),(15),(28)
 H I G D B C

4 006	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C6									
row 1					5 ₂₃			5 ₁	
row 2						5 ₁		5 ₂₃	
row 3		X							
row 4							X		
row 5	5 ₁₂₃		5						
row 6				X					
row 7			5		5 ₁	5 ₂			5 ₃
row 8	5					5 ₃			5 ₁₂
row 9			5 ₁₂₃		5				

Pattern 4.006, continued.

	B	C
D		
G	H	I

Box order: H→I→G→D→B→C

Subpattern-4 begins in (95) zaps (nothing) adding (79) and pending (89)
(95) zaps (93) while (79) zaps (73) adding (81)
(81) zaps (51) adding (53)
(95) zaps (15) adding (26) zaps (28) adding (18)

Subpattern-4 = (95),(79),(81),(53),(26),(18)
 H I G D B C

4 006	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C6									
row 1					5 ₂₃			5 ₁₄	
row 2						5 ₁₄		5 ₂₃	
row 3		X							
row 4							X		
row 5	5 ₁₂₃		5 ₄						
row 6				X					
row 7			5		5 ₁	5 ₂			5 ₃₄
row 8	5 ₄					5 ₃			5 _{12P}
row 9			5 ₁₂₃		5 ₄			P	

Pattern 4.006, continued.

	B	C
D		
G	H	I

Box order: H→I→G→D→B→C

Due to the pending situation in box I, subpattern-5 must
begin in the same square (95) as subpattern-4
include the pending square (89)
(95) zaps (93) while (89) zaps (81) adding (73) zaps (53) adding (51)
(95) zaps (15) adding (26) zaps (28) adding (18)

Subpattern-5 = (95),(89),(73),(51),(26),(18)
H I G D B C

Back at the starting box H, nothing is pending, and no squares are unclaimed. Done.

4 006	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C6									
row 1					5 ₂₃			5 ₁₄₅	
row 2						5 ₁₄₅		5 ₂₃	
row 3		X							
row 4							X		
row 5	5 ₁₂₃₅		5 ₄						
row 6				X					
row 7			5 ₅		5 ₁	5 ₂			5 ₃₄
row 8	5 ₄					5 ₃			5 ₁₂₅
row 9			5 ₁₂₃		5 ₄₅			P	

Pattern 4.013	Orientation	Patterns with the same box code
$\begin{array}{c} 2 \\ \\ 4-3-3 \\ \quad \\ 2-2 \end{array}$	$\begin{array}{c} E \\ \\ H-I-G \\ \quad \\ C-A \end{array}$	014

A		C
	E	
G	H	I

Box order: **H→E→I→C→A→G**

Subpattern-1 starts in **(74)** zaps (54) adding **(56)**
(74) zaps (77) adding **(89)** and pending **(97)**
(89) zaps (29) adding **(17)** zaps (13) adding **(21)**
(21) zaps (81) while **(74)** zaps (73) adding **(93)**

Subpattern-1 = **(74),(56),(89),(17),(21),(93)**
H E I C A G

4	013	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			5					5 ₁		
row2		5 ₁								5
row3					X					
row4		X								
row5				5		5 ₁				
row6									X	
row7			5	5 ₁		5	5			
row8		5								5 ₁
row9			5 ₁	5		5	5 _p	P ₁		

Pattern 4.013, continued.

A		C
	E	
G	H	I

Box order: **H→E→I→C→A→G**

Due to the pending condition in I, subpattern-2 must
start in the same square **(74)** as subpattern-1
include the pending square **(97)**

(74) zaps (54) adding **(56)**

(97) zaps (17) adding **(29)** zaps (21) adding **(13)** zaps (73) & (93) adding **(81)**

Subpattern-2 = **(74),(56),(97),(29),(13),(81)**

H E I C A G

4	013	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			5 ₂					5 ₁		
row2		5 ₁								5 ₂
row3					X					
row4		X								
row5				5		5 ₁₂				
row6									X	
row7			5	5 ₁₂		5	5			
row8		5 ₂								5 ₁
row9			5 ₁	5		5	5 ₂	P ₁		

Pattern 4.013, continued.

A		C
	E	
G	H	I

Box order: **H→E→I→C→A→G**

Subpattern-3 starts in **(76)** zaps (54) adding **(56)**
(76) zaps (77) adding **(89)** and pending **(97)**
(89) zaps (29) adding **(17)** zaps (13) adding **(21)**
(21) zaps (81) while **(76)** zaps (73) adding **(93)**

Subpattern-3 = **(76),(56),(89),(17),(21),(93)**
H E I C A G

4	013	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1			5 ₂				5 ₁₃		
	row2	5 ₁₃								5 ₂
	row3					X				
	row4		X							
	row5				5		5 ₁₂₃			
	row6								X	
	row7			5	5 ₁₂		5 ₃	5		
	row8	5 ₂							P ₃	5 ₁₃
	row9			5 ₁₃	5		5	5 _{2P}		

Pattern 4.013, continued.

A		C
	E	
G	H	I

Box order: **H→E→I→C→A→G**

Due to the pending situation in **I**, subpattern-4 must start in the same square **(76)** as subpattern-3 include the pending square **(97)**

(76) zaps (56) adding **(54)**

(97) zaps (17) adding **(29)** zaps (21) adding **(13)** zaps (73) & (93) adding **(81)**

Subpattern-4 = **(76),(54),(97),(29),(13),(24)**

H E I C A G

4 013	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C7									
row 1			5 ₂₄				5 ₁₃		
row 2	5 ₁₃								5 ₂₄
row 3					X				
row 4		X							
row 5				5 ₄		5 ₁₂₃			
row 6								X	
row 7			5	5 ₁₂		5 ₃₄	5		
row 8	5 ₂₄							P₃	5 ₁₃
row 9			5 ₁₃	5		5	5 ₂₄		

Pattern 4.013, continued.

A		C
	E	
G	H	I

Box order: **H→E→I→C→A→G**

Subpattern-5 begins in **(94)** zaps (54) adding **(56)**
(94) zaps (97) adding **(77)** and pending **(89)**
(77) zaps (17) adding **(29)** zaps (21) adding **(13)** zaps (73) & (93) adding **(81)**

Subpattern-5 = **(94),(56),(77),(29),(13),(81)**
H E I C A G

4 013	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C7									
row 1			5 ₂₄₅				5 ₁₃		
row 2	5 ₁₃								5 ₂₄₅
row 3					X				
row 4		X							
row 5				5 ₃₄		5 ₁₂₅			
row 6								X	
row 7			5	5 ₁₂		5 ₃₄	5 ₅		
row 8	5 ₂₄₅								5 _{13P}
row 9			5 ₁₃	5 ₅		5	5 ₂₄	P ₅	

Pattern 4.013, continued.

A		C
	E	
G	H	I

Box order: $H \rightarrow E \rightarrow I \rightarrow C \rightarrow A \rightarrow G$

Due to the pending condition in **I**, subpattern-6 must start in the same square **(94)** as subpattern-5 include the pending square **(89)**

(94) zaps (54) adding **(56)**

(89) zaps (29) adding **(17)** zaps (13) adding **(21)**

(21) zaps (81) while (94) zaps (93) adding **(73)**

Subpattern-6 = **(94),(89),(56),(17),(21),(73)**

H E I C A G

4 013	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C7									
row 1			5 ₂₄₅				5 ₁₃₆		
row 2	5 ₁₃₆								5 ₂₄₅
row 3					X				
row 4		X							
row 5				5 ₃₄		5 ₁₂₅₆			
row 6								X	
row 7			5 ₆	5 ₁₂		5 ₃₄	5 ₅		
row 8	5 ₂₄₅								5 ₁₃₆
row 9			5 ₁₃	5 ₅₆		5	5 ₂₄	P₅	

Pattern 4.013, continued.

A		C
	E	
G	H	I

Box order: **H→E→I→C→A→G**

Subpattern-7 starts in **(96)** zaps (56) adding **(54)**
(96) zaps (97) adding **(77)** and pending **(89)**
(77) zaps (17) adding **(29)** zaps (21) adding **(13)** zaps (73) & (93) adding **(83)**

Subpattern-7 = **(96),(54),(77),(29),(13),(83)**
H E I C A G

4 013	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C7									
row 1			5 ₂₄₅₇				5 ₁₃₆		
row 2	5 ₁₃₆								5 ₂₄₅₇
row 3					X				
row 4		X							
row 5				5 ₃₄₇		5 ₁₂₅₆			
row 6								X	
row 7			5 ₆	5 ₁₂		5 ₃₄	5 ₅₇		
row 8	5 ₂₄₅₇								5 _{136P}
row 9			5 ₁₃	5 ₅₆		5 ₇	5 ₂₄		P ₇

Pattern 4.013, continued.

A		C
	E	
G	H	I

Box order: **H→E→I→C→A→G**

Due to the pending situation in **I**, subpattern-8 must start in the same square **(96)** as subpattern-7 include the pending square **(89)**

(96) zaps **(56)** adding **(54)**

(89) zaps **(29)** adding **(17)** zaps **(13)** adding **(21)**

(21) zaps **(81)** while **(96)** zaps **(93)** adding **(73)**

Subpattern-8 = **(96),(89),(54),(17),(21),(73)**

H E I C A G

Back at the starting box H, nothing is pending and no squares unclaimed, We are done.

4 013	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C7									
row 1			5 ₂₄₅₇				5 ₁₃₆₈		
row 2	5 ₁₃₆₈								5 ₂₄₅₇
row 3					X				
row 4		X							
row 5				5 ₃₄₇₈		5 ₁₂₅₆			
row 6								X	
row 7			5 ₆₈	5 ₁₂		5 ₃₄	5 ₅₇		
row 8	5 ₂₄₅₇								5 ₁₃₆₈
row 9			5 ₁₃	5 ₅₆		5 ₇₈	5 ₂₄		P ₇

Pattern 4.001	Orientation	Patterns with the same box code
4 - 3 - 2	I - F - C	009
3 - 2	G - D	
2	H	

		C
D		F
G	H	I

Box order: I→G→H→D→F→C

Subpattern-1 begins in (77) zaps (72) adding (83) and pending (93)

(83) zaps (86) adding (96)

(83) zaps (53) adding (62) zaps (67) & (68) adding (59)

(77) zaps (17) adding (18)

Subpattern-1 = (77),(83),(96),(62),(59),(18)

I G H D F C

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							1	1 ₁	
row2	X								
row3				X					
row4					X				
row5			1						1 ₁
row6		1 ₁					1	1	
row7		1					1 ₁	1	
row8	P ₁		1 ₁			1			1
row9			1 _p			1 ₁			1

Pattern 4.001, continued.

		C
D		F
G	H	I

Box order: I→G→H→D→F→C

Due to the pending condition in **G**, subpattern-2 must start in the same square **(77)** as subpattern-1 include the pending square **(93)**

(93) zaps (96) adding **(86)**
(93) zaps (53) adding **(62)** zaps (67) & (68) adding **(59)**
(77) zaps (17) adding **(18)**

Subpattern-2 = **(77),(93),(86),(62),(59),(18)**
 I G H D F C

4 001	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C8									
row 1							1	1 ₁₂	
row 2	X								
row 3				X					
row 4					X				
row 5			1						1 ₁₂
row 6		1 ₁₂					1	1	
row 7		1					1 ₁₂	1	
row 8	P₁		1 ₁			1 ₂			1
row 9			1 ₂			1 ₁			1

Pattern 4.001, continued.

		C
D		F
G	H	I

Box order: I→G→H→D→F→C

Subpattern-3 begins in (78) zaps (72) adding (83) and pending (93)
(83) zaps (86) adding (96)
(83) zaps (53) adding (62) zaps (67) & (68) adding (59)
(78) zaps (18) adding (17)

Subpattern-3 = (78),(83),(96),(62),(59),(17)
 I G H D F C

4 001	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C8									
row 1							1 ₃	1 ₁₂	
row 2	X								
row 3				X					
row 4					X				
row 5			1						1 ₁₂₃
row 6		1 ₁₂₃					1	1	
row 7		1					1 ₁₂	1 ₃	
row 8	P ₃		1 ₁₃			1 ₂			1
row 9			1 _{2P}			1 ₁₃			1

Pattern 4.001, continued.

		C
D		F
G	H	I

Box order: I→G→H→D→F→C

Due to the pending condition in **G**, subpattern-4 must begin in the same square **(78)** as subpattern-3 include the pending square **(93)**

(93) zaps (96) adding **(86)**

(93) zaps (53) adding **(62)** zaps (67) & (68) adding **(59)**

(78) zaps (18) adding **(17)**

Subpattern-4 = **(78),(93),(86),(62),(59),(17)**

I G H D F C

4 001	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C8									
row 1							1 ₃₄	1 ₁₂	
row 2	X								
row 3				X					
row 4					X				
row 5			1						1 ₁₂₃₄
row 6		1 ₁₂₃₄					1	1	
row 7		1					1 ₁₂	1 ₃₄	
row 8	<i>P</i> ₃		1 ₁₃			1 ₂₄			1
row 9			1 ₂₄			1 ₁₃			1

Pattern 4.001, continued.

		C
D		F
G	H	I

Box order is changed to: $I \rightarrow F \rightarrow C \rightarrow D \rightarrow G \rightarrow H$

Subpattern-5 starts in (89) zaps (59) adding (68) and pending (67)
(68) zaps (18) adding (17)
(68) zaps (62) adding (53) zaps (83) & (93) adding (72)
(89) zaps (86) adding (96)

Subpattern-5 = (89),(68),(17),(53),(72),(96)
I F C D G H

4 001	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C8									
row 1							1 ₃₄₅	1 ₁₂	
row 2	X								
row 3				X					
row 4					X		P ₅		
row 5			1 ₅						1 ₁₂₃₄
row 6		1 ₁₂₃₄					1 _p	1 ₅	
row 7		1 ₅					1 ₁₂	1 ₃₄	
row 8			1 ₁₃			1 ₂₄			1 ₅
row 9			1 ₂₄			1 ₁₃₅			1

Pattern 4.001, continued.

		C
D		F
G	H	I

Box order is: I→F→C→D→G→H

Due to the pending condition in **F**, subpattern-6 must
start in the same square **(89)** as subpattern-5
include the pending square **(67)**

(67) zaps (17) adding **(18)**
(67) zaps (62) adding **(53)** zaps (83) & (93) adding **(72)**
(89) zaps (86) adding **(96)**

Subpattern-6 = **(89),(67),(18),(53),(72),(96)**
 I F C D G H

4 001	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C8									
row 1							1 ₃₄₅	1 ₁₂₆	
row 2	X								
row 3				X					
row 4					X		P ₅		
row 5			1 ₅₆						1 ₁₂₃₄
row 6		1 ₁₂₃₄					1 ₆	1 ₅	
row 7		1 ₅₆					1 ₁₂	1 ₃₄	
row 8			1 ₁₃			1 ₂₄			1 ₅₆
row 9			1 ₂₄			1 ₁₃₅₆			1

Pattern 4.001, continued.

		C
D		F
G	H	I

Box order is: I→F→C→D→G→H

Subpattern-7 begins in (99) zaps (59) adding (67) and pending (68)
(67) zaps (17) adding (18)
(67) zaps (62) adding (53) zaps (83) & (93) adding (72)
(99) zaps (96) adding (86)

Subpattern-7 = (99),(67),(18),(53),(72),(86)
 I F C D G H

4 001	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C8									
row 1							1 ₃₄₅	1 ₁₂₆₇	
row 2	X								
row 3				X					
row 4					X		P ₇		
row 5			1 ₅₆₇						1 ₁₂₃₄
row 6		1 ₁₂₃₄					1 ₆₇	1 _{5P}	
row 7		1 ₅₆₇					1 ₁₂	1 ₃₄	
row 8			1 ₁₃			1 ₂₄₇			1 ₅₆
row 9			1 ₂₄			1 ₁₃₅₆			1 ₇

Pattern 4.001, continued.

		C
D		F
G	H	I

Box order is: I→F→C→D→G→H

Due to the pending condition in **F**, subpattern-8 must
begin in the same starting square **(99)** as subpattern-7
include the pending square **(68)**

(68) zaps (18) adding **(17)**

(68) zaps (62) adding **(53)** zaps (83) & (93) adding **(72)**

(99) zaps (96) adding **(86)**

Subpattern-8 = **(99),(68),(17),(53),(72),(86)**

I F C D G H

Back at the starting box I, nothing is pending and no squares are unclaimed. Done.

4 001	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C8									
row 1							1 ₃₄₅₈	1 ₁₂₆₇	
row 2	X								
row 3				X					
row 4					X		P₇		
row 5			1 ₅₆₇₈						1 ₁₂₃₄
row 6		1 ₁₂₃₄					1 ₆₇	1 ₅₈	
row 7		1 ₅₆₇₈					1 ₁₂	1 ₃₄	
row 8			1 ₁₃			1 ₂₄₇₈			1 ₅₆
row 9			1 ₂₄			1 ₁₃₅₆			1 ₇₈

Pattern 4.007	Orientation	Patterns with the same box code
<pre> 4 ----- 3 3 - 2 3 - 2 - 2 </pre>	<pre> H ----- G B - C E - F - D </pre>	none

A	B	C
D	E	F
G	H	I

Box order: H→G→D→E→F→C→B

Subpattern-1 begins in (74) zaps (71) & (72) adding (91) zaps (61) adding (52) (52) zaps (54) & (56) adding (45) zaps (48) adding (67) zaps (17) adding (28) (28) zaps (25) while (74) zaps (14) adding (16)

Subpattern-1 = (74),(91),(52),(45),(67),(28),(16)
H G D E F C B

4	007	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				5		5 ₁	5			
row2					5				5 ₁	
row3			X							
row4						5 ₁			5	
row5		5 ₁		5		5				
row6	5							5 ₁		
row7	5	5		5 ₁		5				
row8										X
row9	5 ₁			5		5				

Pattern 4.007, continued.

A	B	C
D	E	F
G	H	I

Box order: H→G→D→E→F→C→B

Subpattern-2 begins in square (76) zaps (71) & (72) adding (91) zaps (61) adding (52) (52) zaps (54) & (56) adding (45) zaps (48) adding (67) zaps (17) adding (28) (28) zaps (25) while (76) zaps (16) adding (14)

Subpattern-2 = (76),(91),(52),(45),(67),(28),(14)
H G D E F C B

4 007	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C9									
row 1				5 ₂		5 ₁	5		
row 2					5			5 ₁₂	
row 3			X						
row 4					5 ₁₂			5	
row 5		5 ₁₂		5		5			
row 6	5						5 ₁₂		
row 7	5	5		5 ₁		5 ₂			
row 8									X
row 9	5 ₁₂			5		5			

Pattern 4.007, continued.

A	B	C
D	E	F
G	H	I

Box order: H→G→D→E→F→C→B

Subpattern-3 begins in (94) zaps (91) adding (71) and pending (72)
(71) zaps (61) adding (52) zaps (54) & (56) adding (45) zaps (48) adding (67)
(67) zaps (17) adding (28)
(28) zaps (25) while (94) zaps (14) adding (16)

Subpattern-3 = (94),(71),(52),(45),(67),(28),(16)
 H G D E F C B

4 007	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C9									
row 1				5 ₂		5 ₁₃	5		
row 2					5			5 ₁₂₃	
row 3			X						
row 4					5 ₁₂₃			5	
row 5		5 ₁₂₃		5		5			
row 6	5						5 ₁₂₃		
row 7	5 ₃	5 _p		5 ₁		5 ₂			
row 8			P ₃						X
row 9	5 ₁₂			5 ₃		5			

Pattern 4.007, continued.

Box order: H→G→D→E→F→C→B

Due to the pending condition in **G**, subpattern-4 must
begin in the same square **(94)** as subpattern-3
include the pending square **(72)**

(72) zaps **(52)** adding **(61)**

(94) zaps **(54)** adding **(45)** and pending **(56)** *****

(45) zaps **(48)** adding **(67)**

But now, (61) and (67) are BOTH members of subpattern-4, and in the SAME row, so the addition of (45) leads to a contradiction. Therefore we must backtrack two lines to the zapping of (54) by (94), and add (56) instead of (45), removing the pending action. We'll do this on the next page.

4 007	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C9									
row 1				5 ₂		5 ₁₃	5		
row 2					5			5 ₁₂₃₄	
row 3			X						
row 4					5 ₁₂₃₄			5	
row 5		5 ₁₂₃		5		5 _P			
row 6	5 ₄						5 ₁₂₃₄		
row 7	5 ₃	5 ₄		5 ₁		5 ₂			
row 8			P ₃						X
row 9	5 ₁₂			5 ₃₄		5			

Pattern 4.007, continued.

A	B	C
D	E	F
G	H	I

Box order: H→G→D→E→F→C→B

Due to the pending condition in **G**, subpattern-4 must
begin in the same square **(94)** as subpattern-3
include the pending square **(72)**

(72) zaps (52) adding **(61)**

(94) zaps (54) adding **(56)** (*this time, the pending square is added to the subpattern*)

(61) zaps (67) adding **(48)** zaps (28) adding **(17)** zaps (14) & (16) adding **(25)**

Subpattern-4 = **(94),(72),(61),(56),(48),(17),(25)**

H G D E F C B

4 007	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C9									
row 1				5 ₂		5 ₁₃	5 ₄		
row 2					5 ₄			5 ₁₂₃	
row 3			X						
row 4					5 ₁₂₃			5 ₄	
row 5		5 ₁₂₃		5		5 ₄			
row 6	5 ₄						5 ₁₂₃		
row 7	5 ₃	5 ₄		5 ₁		5 ₂			
row 8			P ₃						X
row 9	5 ₁₂			5 ₃₄		5			

Pattern 4.007, continued.

A	B	C
D	E	F
G	H	I

Box order: H→G→D→E→F→C→B

Subpattern-5 is begun in **(96)** zaps (91) adding **(71)** and pending **(72)**
(71) zaps (61) adding **(52)** zaps (54) & (64) adding **(45)** zaps (48) adding **(67)**
(67) zaps (17) adding **(28)**
(28) zaps (25) while **(96)** zaps (16) adding **(14)**

Subpattern-5 = **(96),(71),(52),(45),(67),(28),(14)**
 H G D E F C B

4 007	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C9									
row 1				5 ₂₅		5 ₁₃	5 ₄		
row 2					5 ₄			5 ₁₂₃₅	
row 3			X						
row 4					5 ₁₂₃₅			5 ₄	
row 5		5 ₁₂₃₅		5		5 ₄			
row 6	5 ₄						5 ₁₂₃₅		
row 7	5 ₃₅	5 _{4P}		5 ₁		5 ₂			
row 8			P ₅						X
row 9	5 ₁₂			5 ₃₄		5 ₅			

Pattern 4.007, continued.

A	B	C
D	E	F
G	H	I

Box order: $H \rightarrow G \rightarrow D \rightarrow F \rightarrow E \rightarrow C \rightarrow B$ (note the switch of E & F, which, since it comes after the pending box, is within the rules.)

Due to the pending condition in **G**, subpattern-6 must
start in the same square **(96)** as subpattern-5
include the pending square **(72)**

(72) zaps (52) adding **(61)** zaps (67) adding **(48)**

(48) zaps (45) while **(96)** zaps (56) adding **(54)**

(48) zaps (28) adding **(17)** zaps (14) & (16) adding **(25)**

Subpattern-6 = **(96),(72),(61),(48),(54),(17),(25)**

H G D F E C B

Back at the starting box H, nothing is pending & no squares unclaimed. Done.

4 007 col 1 col 2 col 3 col 4 col 5 col 6 col 7 col 8 col 9

C9									
row 1				5 ₂₅		5 ₁₃	5 ₄₆		
row 2					5 ₄₆			5 ₁₂₃₅	
row 3			X						
row 4					5 ₁₂₃₅			5 ₄₆	
row 5		5 ₁₂₃₅		5 ₆		5 ₄			
row 6	5 ₄₆						5 ₁₂₃₅		
row 7	5 ₃₅	5 ₄₆		5 ₁		5 ₂			
row 8			P ₅						X
row 9	5 ₁₂			5 ₃₄		5 ₅₆			

Pattern 4.010	Orientation	Patterns with the same box code
5 - 3 - 2	D - F - E	none
2 - 2	C - A	

A	B	C
D	E	F
G	H	I

Subpattern-1 begins in **(41)** with box order **D→E→F→A→C**

(41) zaps (45) adding **(65)**

(41) zaps (49) while **(65)** zaps (69) adding **(59)**

(41) zaps (11) adding **(33)** zaps (38) adding **(18)**

Subpattern-1 = **(41),(65),(59),(33),(18)**

D E F A C

Since the bottom three rows of this sudoku are free of candidates, we'll omit these rows during the rest of this analysis, then include them on the final page.

4	010	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		1							1 ₁	
row2				X						
row3			1 ₁						1	
row4		1 ₁	1		1					1
row5		1								1 ₁
row6		1	1		1 ₁					1
row7								X		
row8							X			
row9		X								

Pattern 4.010, continued.

A		C
D	E	F

Subpattern-2 begins in (51) with box order **D→F→E→A→C**

- (51) zaps (59) adding (49) and pending (69)
- (49) zaps (45) adding (65)
- (51) zaps (11) adding (33) zaps (38) adding (18)

Subpattern-2 = (51),(49),(65),(33),(18)
 D F E A C

4 010	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
D1									
row 1	1							1 ₁₂	
row 2				X					
row 3			1 ₁₂					1	
row 4	1 ₁		1		1				1 ₂
row 5	1 ₂						<i>p</i>		1 ₁
row 6	1		1		1 ₁₂				1

Pattern 4.010, continued.

A		C
D	E	F

Box order: **D→F→E→A→C**

Due to the pending condition in **F**, subpattern-3 must
start in the same square **(51)** as subpattern-2
include the pending square **(69)**

(69) zaps (65) adding **(45)**
(51) zaps (11) adding **(33)** zaps (38) adding **(18)**

Subpattern-3 = **(51),(69),(45),(33),(18)**
 D F E A C

4 010	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
D1									
row 1	1							1 ₁₂₃	
row 2				X					
row 3			1 ₁₂₃					1	
row 4	1 ₁		1		1 ₃				1 ₂
row 5	1 ₂₃						<i>P</i>		1 ₁
row 6	1		1		1 ₁₂				1 ₃

Pattern 4.010, continued.

A		C
D	E	F

Subpattern-4 begins in **(61)** with box order **D→E→F→A→C**

(61) zaps (65) adding **(45)**
(61) zaps (69) while **(45)** zaps (49) adding **(59)**
(61) zaps (11) adding **(33)** zaps (38) adding **(18)**

Subpattern-4 = **(61),(45),(59),(33),(18)**
 D E F A C

4 010	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
D1									
row 1	1							1 ₁₂₃₄	
row 2				X					
row 3			1 ₁₂₃₄					1	
row 4	1 ₁		1		1 ₃₄				1 ₂
row 5	1 ₂₃						<i>P</i>		1 ₁
row 6	1 ₄		1		1 ₁₂				1 ₃

Pattern 4.010, continued.

A		C
D	E	F

Box order is D→E→F→A→C

Subpattern-5 starts in (43) zaps (45) adding (65)
(65) zaps (69) while (43) zaps (49) adding (59)
(43) zaps (33) adding (11) zaps (18) adding (38)

Subpattern-5 = (43),(65),(59),(11),(38)
 D E F A C

4 010	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
D1									
row 1	1 ₅							1 ₁₂₃₄	
row 2				X					
row 3			1 ₁₂₃₄					1 ₅	
row 4	1 ₁		1 ₅		1 ₃₄				1 ₂
row 5	1 ₂₃						P		1 ₁₄₅
row 6	1 ₄		1		1 ₁₂₅				1 ₃

Pattern 4.010, continued.

A		C
D	E	F

Box order: D→E→F→A→C

Subpattern-6 starts in (63) zaps (65) adding (45)
(65) zaps (69) while (45) zaps (49) adding (59)
(63) zaps (33) adding (11) zaps (18) adding (38)

Subpattern-6 = (63),(45),(59),(11),(38)
 D E F A C

Back at the starting box, nothing is pending and no squares unclaimed. We are done.

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row 1	1 ₅₆							1 ₁₂₃₄	
row 2				X					
row 3			1 ₁₂₃₄					1 ₅₆	
row 4	1 ₁		1 ₅		1 ₃₄₆				1 ₂
row 5	1 ₂₃						<i>P</i>		1 ₁₄₅₆
row 6	1 ₄		1 ₆		1 ₁₂₅				1 ₃
row 7							X		
row 8						X			
row 9		X							

Pattern 4.015	Orientation	Patterns with the same box code
5 - 3 - 2	G - D - A	none
2 - 2	F - I	
2	E	

A		
D	E	F
G		I

Box order: G→A→D→I→F→E

Subpattern-1 begins in (81) zaps (11) adding (12)
(12) zaps (52) while (81) zaps (51) adding (53)
(81) zaps (87) adding (98) zaps (68) adding (47) zaps (46) adding (66)

Subpattern-1 = (81),(12),(53).(98),(47),(66)
G A D I F E

4	015	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
D3	row1	7	7 ₁							
	row2									X
	row3				X					
	row4						7	7 ₁		
	row5	7	7	7 ₁						
	row6						7 ₁		7	
	row7					X				
	row8	7 ₁	7					7		
	row9	7	7	7					7 ₁	

Pattern 4.015, continued.

A		
D	E	F
G		I

Box order: **G→A→D→I→F→E**

Subpattern-2 begins in **(82)** zaps (12) adding **(11)**
(82) zaps (52) while **(11)** zaps (51) adding **(52)**
(82) zaps (87) adding **(98)** zaps (68) adding **(47)**

Subpattern-2 = **(82),(11),(52),(98),(47),(66)**
G A D I F E

4	015	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
D3	row1	7 ₂	7 ₁							
	row2									X
	row3				X					
	row4						7	7 ₁₂		
	row5	7	7	7 ₁₂						
	row6						7 ₁₂		7	
	row7					X				
	row8	7 ₁	7 ₂					7		
	row9	7	7	7					7 ₁₂	

Pattern 4.015, continued.

A		
D	E	F
G		I

Box order: **G→A→D→I→F→E**

Subpattern-3 begins in **(91)** zaps (11) adding **(12)**
(91) zaps (51) while **(12)** zaps (52) adding **(53)**
(91) zaps (98) adding **(87)** zaps (47) adding **(68)** zaps (66) adding **(46)**

Subpattern-3 = **(91),(12),(53),(87),(68),(46)**
G A D I F E

4 D3	015	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
	row1	7 ₂	7 ₁₃							
	row2									X
	row3				X					
	row4						7	7 ₁₂		
	row5	7	7	7 ₁₂₃						
	row6						7 ₁₂		7 ₃	
	row7					X				
	row8	7 ₁	7 ₂					7 ₃		
	row9	7 ₃	7	7					7 ₁₂	

Pattern 4.015, continued.

A		
D	E	F
G		I

Box order: **G→A→D→I→F→E**

Subpattern-4 begins in **(92)** zaps (12) adding **(11)**
(11) zaps (51) while **(92)** zaps (52) adding **(53)**
(92) zaps (98) adding **(87)** zaps (47) adding **(68)** zaps (66) adding **(46)**

Subpattern-4 = **(92),(11),(53),(87),(68),(46)**
G A D I F E

Subpatten-5 begins in **(93)** zaps (53) adding **(51)** and pending **(52)**
(51) zaps (11) adding **(12)**
(93) zaps (98) adding **(87)** zaps (47) adding **(68)** zaps (66) adding **(46)**

Subpatten-5 = **(93),(51),(12),(87),(68),(46)**
G A D I F E

4	015	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
D3	row1	7 ₂₄	7 ₁₃₅							
	row2									X
	row3				X					
	row4	P					7 ₃₄	7 ₁₂		
	row5	7 ₅	7 _P	7 ₁₂₃₄						
	row6						7 ₁₂		7 ₃₄₅	
	row7					X				
	row8	7 ₁	7 ₂					7 ₃₄₅		
	row9	7 ₃	7 ₄	7 ₅					7 ₁₂	

Pattern 4.015, continued.

A		
D	E	F
G		I

Box order: **G**→**A**→**D**→**I**→**F**→**E**

Due to the pending condition in **D**, subpattern-6 must
begin in the same square **(93)** as subpattern-5
include the pending square **(52)**

(52) zaps (12) adding **(11)**

(93) zaps (98) adding **(87)** zaps (47) adding **(68)** zaps (66) adding **(46)**

Subpattern-6 = **(93),(52),(11),(87),(68),(46)**

G A D I F E

Back at the starting box G, nothing is pending, and no squares are unclaimed,
so the pattern analysis is complete.

4	015	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
D3	row1	7 ₂₄₆	7 ₁₃₅							
	row2									X
	row3				X					
	row4	p					7 ₃₄₅₆	7 ₁₂		
	row5	7 ₅	7 ₆	7 ₁₂₃₄						
	row6						7 ₁₂		7 ₃₄₅₆	
	row7					X				
	row8	7 ₁	7 ₂					7 ₃₄₅₆		
	row9	7 ₃	7 ₄	7 ₅₆					7 ₁₂	

PATTERN FILE 1

1 001 B9

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		2 ₁						2 ₂	
row2	2 ₂						2 ₁		
row3				X					
row4		2 ₂			2 ₁				
row5	2 ₁					2 ₂			
row6									X
row7			X						
row8						2 ₁	2 ₂		
row9					2 ₂			2 ₁	

1 001 B9

	col 1	col 2	col 5	col 6	col 7	col 8
row1		2 ₁				2 ₂
row2	2 ₂				2 ₁	
row4		2 ₂	2 ₁			
row5	2 ₁			2 ₂		
row8				2 ₁	2 ₂	
row9			2 ₂			2 ₁

1002B1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2	4 ₁			4 ₂					
row3		4 ₂			4 ₁				
row4							X		
row5	4 ₂			4 ₁					
row6		4 ₁			4 ₂				
row7						X			
row8			X						
row9								X	

1002B1

	col 1	col 2	col 4	col 5
row2	4 ₁		4 ₂	
row3		4 ₂		4 ₁
row5	4 ₂		4 ₁	
row6		4 ₁		4 ₂

1 003 B9

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				2 ₁			2 ₂		
row2		X							
row3					2 ₂				2 ₁
row4	2 ₁								2 ₂
row5			2 ₂				2 ₁		
row6						X			
row7	2 ₂				2 ₁				
row8								X	
row9			2 ₁	2 ₂					

1 003 B9

	col 1	col 3	col 4	col 5	col 7	col 9
row1			2 ₁		2 ₂	
row3				2 ₂		2 ₁
row4	2 ₁					2 ₂
row5		2 ₂			2 ₁	
row7	2 ₂			2 ₁		
row9		2 ₁	2 ₂			

1 004 C2

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					3 ₁		3 ₂		
row2				3 ₂			3 _K		3 ₁
row3	X								
row4								X	
row5			3 ₂	3 ₁					
row6		3 ₁			3 ₂				
row7		3 ₂					3 ₁		
row8			3 ₁				3 _K		3 ₂
row9						X			

1 004 C2

	col 2	col 3	col 4	col 5	col 7	col 9
row1				3 ₁	3 ₂	
row2			3 ₂		3 _K	3 ₁
row5		3 ₂	3 ₁			
row6	3 ₁			3 ₂		
row7	3 ₂				3 ₁	
row8		3 ₁			3 _K	3 ₂

1 005 B1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		4 ₁						4 ₂	
row2	4 ₂								4 ₁
row3				X					
row4					X				
row5							X		
row6			X						
row7		4 ₂						4 ₁	
row8	4 ₁								4 ₂
row9						X			

1 005 B1

	col 1	col 2	col 8	col 9
row1		4 ₁	4 ₂	
row2	4 ₂			4 ₁
row7		4 ₂	4 ₁	
row8	4 ₁			4 ₂

1 006 A2

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2					X				
row3							X		
row4								3 ₁	3 ₂
row5		X							
row6						X			
row7	3 ₁							3 ₂	
row8	3 ₂								3 ₁
row9				X					

1 006 A2

	col 1	col 8	col 9
row4		3 ₁	3 ₂
row7	3 ₁	3 ₂	
row8	3 ₂		3 ₁

1 007 B9

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1								X	
row2			9 ₁		9 ₂				
row3	9 ₂			9 ₁					
row4		X							
row5				9 ₂					9 ₁
row6					9 ₁		9 ₂		
row7	9 ₁								9 ₂
row8						X			
row9			9 ₂				9 ₁		

1 007 B9

	col 1	col 3	col 4	col 5	col 7	col 9
row2		9 ₁		9 ₂		
row3	9 ₂		9 ₁			
row5			9 ₂			9 ₁
row6				9 ₁	9 ₂	
row7	9 ₁					9 ₂
row9		9 ₂			9 ₁	

1 008 B2

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					X				
row2		1 ₁					1 ₂		
row3	1 ₂								1 ₁
row4						1 ₁			1 ₂
row5		1 ₂					1 ₁		
row6	1 ₁					1 ₂			
row7			X						
row8				X					
row9								X	

1 008 B2

	col 1	col 2	col 6	col 7	col 9
row2		1 ₁		1 ₂	
row3	1 ₂				1 ₁
row4			1 ₁		1 ₂
row5		1 ₂		1 ₁	
row6	1 ₁		1 ₂		

1 009 A7

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			6 ₁	6 ₂					
row2	6 ₂			6 ₁					
row3							X		
row4						X			
row5		X							
row6								6 ₂	6 ₁
row7	6 ₁								6 ₂
row8					X				
row9			6 ₂					6 ₁	

1 009 A7

	col 1	col 3	col 4	col 8	col 9
row1		6 ₁	6 ₂		
row2	6 ₂		6 ₁		
row6				6 ₂	6 ₁
row7	6 ₁				6 ₂
row9		6 ₂		6 ₁	

1 010 B9

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		5 ₁			5 ₂				
row2			5 ₂	5 ₁					
row3							X		
row4	X								
row5				5 ₂					5 ₁
row6					5 ₁			5 ₂	
row7						X			
row8			5 ₁						5 ₂
row9		5 ₂						5 ₁	

1 010 B9

	col 2	col 3	col 4	col 5	col 8	col 9
row1	5 ₁			5 ₂		
row2		5 ₂	5 ₁			
row5			5 ₂			5 ₁
row6				5 ₁	5 ₂	
row8		5 ₁				5 ₂
row9	5 ₂				5 ₁	

1 011 B9

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	X								
row2					2 ₁				2 ₂
row3				2 ₂				2 ₁	
row4						X			
row5		2 ₁						2 ₂	
row6			2 ₂						2 ₁
row7							X		
row8			2 ₁		2 ₂				
row9		2 ₂		2 ₁					

1 011 B9

	col 2	col 3	col 4	col 5	col 8	col 9
row2				2 ₁		2 ₂
row3			2 ₂		2 ₁	
row5	2 ₁				2 ₂	
row6		2 ₂				2 ₁
row8		2 ₁		2 ₂		
row9	2 ₂		2 ₁			

1 012 B9

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	7 ₁						7 ₂		
row2					X				
row3		7 ₂							7 ₁
row4		7 ₁				7 ₂			
row5								X	
row6	7 ₂			7 ₁					
row7			X						
row8				7 ₂			7 ₁		
row9						7 ₁			7 ₂

1 012 B9

	col 1	col 2	col 4	col 6	col 7	col 9
row1	7 ₁				7 ₂	
row3		7 ₂				7 ₁
row4		7 ₁		7 ₂		
row6	7 ₂		7 ₁			
row8			7 ₂		7 ₁	
row9				7 ₁		7 ₂

1 013 B1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2							X		
row3					X				
row4				X					
row5	1 ₁								1 ₂
row6		1 ₂						1 ₁	
row7						X			
row8	1 ₂								1 ₁
row9		1 ₁						1 ₂	

1 013 B1

	col 1	col 2	col 8	col 9
row5	1 ₁			1 ₂
row6		1 ₂	1 ₁	
row8	1 ₂			1 ₁
row9		1 ₁	1 ₂	

1 014 C8

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2	5 ₁					5 ₂			
row3	5 _K	5 ₂			5 ₁				
row4		5 ₁					5 _K	5 ₂	
row5	5 ₂						5 ₁		
row6				X					
row7			X						
row8						5 ₁	5 ₂		
row9					5 ₂		5 _K	5 ₁	

1 014 C8

	col 1	col 2	col 5	col 6	col 7	col 8
row2	5 ₁			5 ₂		
row3	5 _K	5 ₂	5 ₁			
row4		5 ₁			5 _K	5 ₂
row5	5 ₂				5 ₁	
row8				5 ₁	5 ₂	
row9			5 ₂		5 _K	5 ₁

1 015 B1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				X					
row2	4 ₁						4 ₂		
row3		4 ₂						4 ₁	
row4			X						
row5						X			
row6									X
row7	4 ₂						4 ₁		
row8					X				
row9		4 ₁						4 ₂	

1 015 B1

	col 1	col 2	col 7	col 8
row2	4 ₁		4 ₂	
row3		4 ₂		4 ₁
row7	4 ₂		4 ₁	
row9		4 ₁		4 ₂

1 016 B9

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2						4 ₁	4 ₂		
row3				4 ₂					4 ₁
row4		4 ₁							4 ₂
row5					X				
row6	4 ₂						4 ₁		
row7	4 ₁					4 ₂			
row8								X	
row9		4 ₂		4 ₁					

1 016 B9

	col 1	col 2	col 4	col 6	col 7	col 9
row2				4 ₁	4 ₂	
row3			4 ₂			4 ₁
row4		4 ₁				4 ₂
row6	4 ₂				4 ₁	
row7	4 ₁			4 ₂		
row9		4 ₂	4 ₁			

1 017 A1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							X		
row2	X								
row3					X				
row4						X			
row5		X							
row6									X
row7			5 ₁	5 ₂					
row8			5 ₂					5 ₁	
row9				5 ₁				5 ₂	

1 017 A1

	col 3	col 4	col 8
row7	5 ₁	5 ₂	
row8	5 ₂		5 ₁
row9		5 ₁	5 ₂

1 018 C3

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					8 ₂		8 ₁		
row2				8 ₁			8 _K		8 ₂
row3		X							
row4						X			
row5			8 ₂				8 _K		8 ₁
row6	8 ₁						8 ₂		
row7	8 ₂				8 ₁				
row8								X	
row9			8 ₁	8 ₂	8 _K				

1 018 C3

	col 1	col 3	col 4	col 5	col 7	col 9
row1				8 ₂	8 ₁	
row2			8 ₁		8 _K	8 ₂
row5		8 ₂			8 _K	8 ₁
row6	8 ₁				8 ₂	
row7	8 ₂			8 ₁		
row9		8 ₁	8 ₂	8 _K		

1 019 B1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					6 ₁		6 ₂		
row2						6 ₂			6 ₁
row3		X							
row4	X								
row5						6 ₁			6 ₂
row6					6 ₂		6 ₁		
row7				X					
row8								X	
row9			X						

1 019 B1

	col 5	col 6	col 7	col 9
row1	6 ₁		6 ₂	
row2		6 ₂		6 ₁
row5		6 ₁		6 ₂
row6	6 ₂		6 ₁	

1 020 A4

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2			3 ₁			3 ₂			
row3			3 ₂	3 ₁					
row4	X								
row5					X				
row6							X		
row7		3 ₂				3 ₁			
row8								X	
row9		3 ₁		3 ₂					

1 020 A4

	col 2	col 3	col 4	col 6
row2		3 ₁		3 ₂
row3		3 ₂	3 ₁	
row7	3 ₂			3 ₁
row9	3 ₁		3 ₂	

1 021 B1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							X		
row2		X							
row3						X			
row4			2 ₁	2 ₂					
row5								X	
row6	2 ₂				2 ₁				
row7	2 ₁				2 ₂				
row8									X
row9			2 ₂	2 ₁					

1 021 B1

	col 1	col 3	col 4	col 5
row4		2 ₁	2 ₂	
row6	2 ₂			2 ₁
row7	2 ₁			2 ₂
row9		2 ₂	2 ₁	

1 022 B1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1								X	
row2		9 ₁			9 ₂				
row3	9 ₂			9 ₁					
row4									X
row5			X						
row6						X			
row7							X		
row8		9 ₂			9 ₁				
row9	9 ₁			9 ₂					

1 022 B1

	col 1	col 2	col 4	col 5
row2		9 ₁		9 ₂
row3	9 ₂		9 ₁	
row8		9 ₂		9 ₁
row9	9 ₁		9 ₂	

1 023 B2

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2							X		
row3					3 ₁	3 ₂			
row4						3 ₁			3 ₂
row5		X							
row6				3 ₂			3 ₁		
row7	X								
row8				3 ₁			3 ₂		
row9					3 ₂				3 ₁

1 023 B2

	col 4	col 5	col 6	col 7	col 9
row3		3 ₁	3 ₂		
row4			3 ₁		3 ₂
row6	3 ₂			3 ₁	
row8	3 ₁			3 ₂	
row9		3 ₂			3 ₁

1 024 A6

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		X							
row2						4 ₁	4 ₂		
row3					4 ₂			4 ₁	
row4				X					
row5			X						
row6							4 ₁	4 ₂	
row7	X								
row8					4 ₁	4 ₂			
row9									X

1 024 A6

	col 5	col 6	col 7	col 8
row2		4 ₁	4 ₂	
row3	4 ₂			4 ₁
row6			4 ₁	4 ₂
row8	4 ₁	4 ₂		

1 025 B9

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				2 ₁			2 ₂		
row2		X							
row3					2 ₂				2 ₁
row4	2 ₁								2 ₂
row5			2 ₂				2 ₁		
row6						X			
row7	2 ₂				2 ₁				
row8								X	
row9			2 ₁	2 ₂					

1 025 B9

	col 1	col 3	col 4	col 5	col 7	col 9
row1			2 ₁		2 ₂	
row3				2 ₂		2 ₁
row4	2 ₁					2 ₂
row5		2 ₂			2 ₁	
row7	2 ₂			2 ₁		
row9		2 ₁	2 ₂			

1 026 B9

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						X			
row2	6 ₁						6 ₂		
row3		6 ₂							6 ₁
row4					6 ₁				6 ₂
row5				6 ₂			6 ₁		
row6			X						
row7	6 ₂			6 ₁					
row8								X	
row9		6 ₁			6 ₂				

1 026 B9

	col 1	col 2	col 4	col 5	col 7	col 9
row2	6 ₁				6 ₂	
row3		6 ₂				6 ₁
row4				6 ₁		6 ₂
row5			6 ₂		6 ₁	
row7	6 ₂		6 ₁			
row9		6 ₁		6 ₂		

3 027

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				2 ₁			2 ₂		
row2					2 ₂			2 ₁	
row3			X						
row4		X							
row5					2 ₁			2 ₂	
row6				2 ₂			2 ₁		
row7	X								
row8						X			
row9									X

3 027

	col 4	col 5	col 7	col 8
row1	2 ₁		2 ₂	
row2		2 ₂		2 ₁
row5		2 ₁		2 ₂
row6	2 ₂		2 ₁	

1 028 B9

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				5 ₁			5 ₂		
row2						5 ₂			5 ₁
row3	X								
row4			5 ₁						5 ₂
row5					X				
row6		5 ₂					5 ₁		
row7		5 ₁		5 ₂					
row8								X	
row9			5 ₂			5 ₁			

1 028 B9

	col 2	col 3	col 4	col 6	col 7	col 9
row1			5 ₁		5 ₂	
row2				5 ₂		5 ₁
row4		5 ₁				5 ₂
row6	5 ₂				5 ₁	
row7	5 ₁		5 ₂			
row9		5 ₂		5 ₁		

1 029 B1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		2 ₁					2 ₂		
row2	2 ₂								2 ₁
row3					X				
row4						X			
row5	2 ₁								2 ₂
row6		2 ₂					2 ₁		
row7			X						
row8								X	
row9				X					

1 029 B1

	col 1	col 2	col 7	col 9
row1		2 ₁	2 ₂	
row2	2 ₂			2 ₁
row5	2 ₁			2 ₂
row6		2 ₂	2 ₁	

1 030 B2

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				X					
row2			8 ₂						8 ₁
row3		8 ₁						8 ₂	
row4	X								
row5							8 ₁		8 ₂
row6					X				
row7		8 ₂						8 ₁	
row8			8 ₁				8 ₂		
row9						X			

1 030 B2

	col 2	col 3	col 7	col 8	col 9
row2		8 ₂			8 ₁
row3	8 ₁			8 ₂	
row5			8 ₁		8 ₂
row7	8 ₂			8 ₁	
row8		8 ₁	8 ₂		

1 031 B9

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2						3 ₁			3 ₂
row3					3 ₂			3 ₁	
row4							X		
row5	3 ₁					3 ₂			
row6		3 ₂			3 ₁				
row7				X					
row8	3 ₂								3 ₁
row9		3 ₁						3 ₂	

1 031 B9

	col 1	col 2	col 5	col 6	col 8	col 9
row2				3 ₁		3 ₂
row3			3 ₂		3 ₁	
row5	3 ₁			3 ₂		
row6		3 ₂	3 ₁			
row8	3 ₂					3 ₁
row9		3 ₁			3 ₂	

1 032 A2

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	X								
row2				X					
row3							X		
row4		8 ₁							8 ₂
row5					X				
row6			8 ₂						8 ₁
row7								X	
row8		8 ₂	8 ₁						
row9				X					

1 032 A2

	col 2	col 3	col 9
row4	8 ₁		8 ₂
row6		8 ₂	8 ₁
row8	8 ₂	8 ₁	

1 033 A1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	3 ₁		3 ₂						
row2				X					
row3							X		
row4					X				
row5									X
row6		3 ₂	3 ₁						
row7						X			
row8	3 ₂	3 ₁							
row9								X	

1 033 A1

	col 1	col 2	col 3
row1	3 ₁		3 ₂
row6		3 ₂	3 ₁
row8	3 ₂	3 ₁	

1 034 A5

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1								X	
row2		X							
row3						X			
row4			7 ₂	7 ₁					
row5	7 ₁			7 ₂					
row6									X
row7			7 ₁				7 ₂		
row8					7 ₂		7 ₁		
row9	7 ₂				7 ₁				

1 034 A5

	col 1	col 3	col 4	col 5	col 7
row4		7 ₂	7 ₁		
row5	7 ₁		7 ₂		
row7		7 ₁			7 ₂
row8				7 ₂	7 ₁
row9	7 ₂			7 ₁	

1 035 A4

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					3 ₁			3 ₂	
row2				3 ₂				3 ₁	
row3		X							
row4									X
row5			3 ₁		3 ₂				
row6			3 ₂	3 ₁					
row7							X		
row8	X								
row9						X			

1 035 A4

	col 3	col 4	col 5	col 8
row1			3 ₁	3 ₂
row2		3 ₂		3 ₁
row5	3 ₁		3 ₂	
row6	3 ₂	3 ₁		

1 036 B1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		3 ₁					3 ₂		
row2	3 ₂								3 ₁
row3					X				
row4						X			
row5			X						
row6								X	
row7	3 ₁								3 ₂
row8				X					
row9		3 ₂					3 ₁		

1 036 B1

	col 1	col 2	col 7	col 9
row1		3 ₁	3 ₂	
row2	3 ₂			3 ₁
row7	3 ₁			3 ₂
row9		3 ₂	3 ₁	

1 037 C0

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				7 ₁	7 ₂		7 ₃		
row2		X							
row3				7 ₃			7 ₁₂		
row4				7 ₂					7 ₁₃
row5					7 ₁₃				7 ₂
row6			X						
row7						X			
row8	X								
row9								X	

1 037 C0

	col 4	col 5	col 7	col 9
row1	7 ₁	7 ₂	7 ₃	
row3	7 ₃		7 ₁₂	
row4	7 ₂			7 ₁₃
row5		7 ₁₃		7 ₂

*2

1 038 B3

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	X								
row2									X
row3					3 ₁	3 ₂			
row4		3 ₂						3 ₁	
row5			3 ₁				3 ₂		
row6				X					
row7		3 ₁						3 ₂	
row8			3 ₂			3 ₁			
row9					3 ₂		3 ₁		

1 038 B3

	col 2	col 3	col 5	col 6	col 7	col 8
row3			3 ₁	3 ₂		
row4	3 ₂					3 ₁
row5		3 ₁			3 ₂	
row7	3 ₁					3 ₂
row8		3 ₂		3 ₁		
row9			3 ₂		3 ₁	

1 039 B9

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						9 ₁	9 ₂		
row2		X							
row3				9 ₂					9 ₁
row4			9 ₂	9 ₁					
row5								X	
row6	9 ₁					9 ₂			
row7	9 ₂						9 ₁		
row8					X				
row9			9 ₁						9 ₂

1 039 B9

	col 1	col 3	col 4	col 6	col 7	col 9
row1				9 ₁	9 ₂	
row3			9 ₂			9 ₁
row4		9 ₂	9 ₁			
row6	9 ₁			9 ₂		
row7	9 ₂				9 ₁	
row9		9 ₁				9 ₂

1040

ne

w

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1			2 ₁			2 ₂			
row2			2 ₂		2 ₁				
row3							X		
row4		X							
row5					2 ₂	2 ₁			
row6									X
row7	X								
row8				X					
row9								X	

1040

ne

w

col 3

col 5

col 6

row1	2 ₁		2 ₂
row2	2 ₂	2 ₁	
row5		2 ₂	2 ₁

1 041 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			1 ₁				1 ₂		
row2						X			
row3	1 ₂								1 ₁
row4					X				
row5								X	
row6		X							
row7	1 ₁								1 ₂
row8				X					
row9			1 ₂				1 ₁		

1 041 ne
w

	col 1	col 3	col 7	col 9
row1		1 ₁	1 ₂	
row3	1 ₂			1 ₁
row7	1 ₁			1 ₂
row9		1 ₂	1 ₁	

1042

new

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2	2 ₁			2 ₂					
row3			2 ₂			2 ₁			
row4						2 ₂		2 ₁	
row5		X							
row6				2 ₁			2 ₂		
row7	2 ₂						2 ₁		
row8					X				
row9			2 ₁					2 ₂	

1042

new

	col 1	col 3	col 4	col 6	col 7	col 8
row2	2 ₁		2 ₂			
row3		2 ₂		2 ₁		
row4				2 ₂		2 ₁
row6			2 ₁		2 ₂	
row7	2 ₂				2 ₁	
row9		2 ₁				2 ₂

1043

new

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				5 ₂			5 _K	5 ₁	
row2						5 ₁		5 ₂	
row3		X							
row4	5 ₁						5 ₂	5 _K	
row5			5 ₂				5 ₁		
row6					X				
row7			5 ₁			5 ₂			
row8	5 ₂			5 ₁					
row9									X

1043

new

	col 1	col 3	col 4	col 6	col 7	col 8
row1			5 ₂		5 _K	5 ₁
row2				5 ₁		5 ₂
row4	5 ₁				5 ₂	5 _K
row5		5 ₂			5 ₁	
row7		5 ₁		5 ₂		
row8	5 ₂		5 ₁			

1044

new

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					1 ₁			1 ₂	
row2						1 ₂	1 ₁		
row3	X								
row4		1 ₁			1 ₂				
row5			1 ₂			1 ₁			
row6									X
row7		1 ₂						1 ₁	
row8			1 ₁				1 ₂		
row9				X					

1044

new

	col 2	col 3	col 5	col 6	col 7	col 8
row1			1 ₁			1 ₂
row2				1 ₂	1 ₁	
row4	1 ₁		1 ₂			
row5		1 ₂		1 ₁		
row7	1 ₂					1 ₁
row8		1 ₁			1 ₂	

1 045 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	8 ₂							8 ₁	8 _K
row2						X			
row3			8 ₁						8 ₂
row4		X							
row5				8 ₁				8 ₂	
row6				8 ₂			8 ₁		8 _K
row7					X				
row8			8 ₂						8 ₁
row9	8 ₁						8 ₂		

1 045 ne
w

	col 1	col 3	col 4	col 7	col 8	col 9
row1	8 ₂				8 ₁	8 _K
row3		8 ₁				8 ₂
row5			8 ₁		8 ₂	
row6			8 ₂	8 ₁		8 _K
row8		8 ₂				8 ₁
row9	8 ₁			8 ₂		

1 046 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		2 ₁						2 ₂	
row2	2 ₂						2 ₁		
row3						X			
row4		2 ₂			2 ₁				
row5	2 ₁			2 ₂					
row6									X
row7			X						
row8				2 ₁			2 ₂		
row9					2 ₂			2 ₁	

1 046 ne
w

	col 1	col 2	col 4	col 5	col 7	col 8
row1		2 ₁				2 ₂
row2	2 ₂				2 ₁	
row4		2 ₂		2 ₁		
row5	2 ₁		2 ₂			
row8			2 ₁		2 ₂	
row9				2 ₂		2 ₁

1 047 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2	3 ₁			3 ₂					
row3			3 ₂			3 ₁			
row4						3 ₂		3 ₁	
row5		X							
row6				3 ₁			3 ₂		
row7	3 ₂						3 ₁		
row8					X				
row9			3 ₁					3 ₂	

1 047 ne
w

	col 1	col 3	col 4	col 6	col 7	col 8
row2	3 ₁		3 ₂			
row3		3 ₂		3 ₁		
row4				3 ₂		3 ₁
row6			3 ₁		3 ₂	
row7	3 ₂				3 ₁	
row9		3 ₁				3 ₂

1 048 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						3 ₁	3 ₂		
row2					3 ₂				3 ₁
row3			X						
row4								X	
row5		3 ₁				3 ₂			
row6	3 ₂				3 ₁				
row7	3 ₁								3 ₂
row8				X					
row9		3 ₂					3 ₁		

1 048 ne
w

	col 1	col 2	col 3	col 5	col 6	col 7	col 9
row1					3 ₁	3 ₂	
row2				3 ₂			3 ₁
row5		3 ₁			3 ₂		
row6	3 ₂			3 ₁			
row7	3 ₁						3 ₂
row9		3 ₂				3 ₁	

1 049 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						X			
row2			7 ₁				7 ₂		
row3		7 ₂						7 ₁	
row4	X								
row5				7 ₂			7 ₁		
row6					7 ₁			7 ₂	
row7									X
row8			7 ₂	7 ₁					
row9		7 ₁			7 ₂				

1 049 ne
w

	col 2	col 3	col 4	col 5	col 7	col 8
row2		7 ₁			7 ₂	
row3	7 ₂					7 ₁
row5			7 ₂		7 ₁	
row6				7 ₁		7 ₂
row8		7 ₂	7 ₁			
row9	7 ₁			7 ₂		

1 050 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2				X					
row3									X
row4							X		
row5		3 ₁				3 ₂			
row6	3 ₂				3 ₁				
row7							X		
row8	3 ₁				3 ₂				
row9		3 ₂				3 ₁			

1 050 ne
w

	col 1	col 2	col 5	col 6
row5		3 ₁		3 ₂
row6	3 ₂		3 ₁	
row8	3 ₁		3 ₂	
row9		3 ₂		3 ₁

1051

new

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	X								
row2					4 ₁		4 ₂		
row3						4 ₂			4 ₁
row4			4 ₁		4 ₂				
row5		4 ₂				4 ₁			
row6								X	
row7		4 ₁							4 ₂
row8				X					
row9			4 ₂				4 ₁		

1051

new

	col 2	col 3	col 5	col 6	col 7	col 9
row2			4 ₁		4 ₂	
row3				4 ₂		4 ₁
row4		4 ₁	4 ₂			
row5	4 ₂			4 ₁		
row7	4 ₁					4 ₂
row9		4 ₂			4 ₁	

1 052 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2					X				
row3							X		
row4		1 ₁				1 ₂			
row5									X
row6	1 ₂			1 ₁					
row7	1 ₁			1 ₂					
row8								X	
row9		1 ₂				1 ₁			

1 052 ne
w

	col 1	col 2	col 4	col 6
row4		1 ₁		1 ₂
row6	1 ₂		1 ₁	
row7	1 ₁		1 ₂	
row9		1 ₂		1 ₁

1 053 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2						4 ₁	4 ₂		
row3				4 ₂					4 ₁
row4		4 ₁							4 ₂
row5					X				
row6	4 ₂						4 ₁		
row7	4 ₁					4 ₂			
row8								X	
row9		4 ₂		4 ₁					

1 053 ne
w

	col 1	col 2	col 4	col 6	col 7	col 9
row2				4 ₁	4 ₂	
row3			4 ₂			4 ₁
row4		4 ₁				4 ₂
row6	4 ₂				4 ₁	
row7	4 ₁			4 ₂		
row9		4 ₂	4 ₁			

1054

ne

w

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1	X							
row2						9 ₁	9 ₂	
row3				X				
row4					X			
row5			9 ₁			9 ₂		
row6			9 ₂				9 ₁	
row7			X					
row8		X						
row9								X

1054

ne

w

col 3

col 7

col 8

row2		9 ₁	9 ₂
row5	9 ₁	9 ₂	
row6	9 ₂		9 ₁

1055

ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				1 ₁	1 ₂				
row2	X								
row3								X	
row4									X
row5		X							
row6				1 ₂		1 ₁			
row7					1 ₁	1 ₂			
row8							X		
row9			X						

1055

ne
w

	col 4	col 5	col 6
row1	1 ₁	1 ₂	
row6	1 ₂		1 ₁
row7		1 ₁	1 ₂

1 056 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				X					
row2							7 ₁	7 ₂	
row3		X							
row4						X			
row5	X								
row6									X
row7			X						
row8					7 ₂			7 ₁	
row9					7 ₁		7 ₂		

1 056 ne
w

	col 5	col 7	col 8
row2		7 ₁	7 ₂
row8	7 ₂		7 ₁
row9	7 ₁	7 ₂	

1 057 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				7 ₁			7 ₂		
row2		X							
row3					7 ₂				7 ₁
row4	7 ₁								7 ₂
row5			7 ₂				7 ₁		
row6						X			
row7	7 ₂				7 ₁				
row8								X	
row9			7 ₁	7 ₂					

1 057 ne
w

	col 1	col 3	col 4	col 5	col 7	col 9
row1			7 ₁		7 ₂	
row3				7 ₂		7 ₁
row4	7 ₁					7 ₂
row5		7 ₂			7 ₁	
row7	7 ₂			7 ₁		
row9		7 ₁	7 ₂			

1 058 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				9 ₂			9 ₁		
row2					9 ₁		9 ₂		
row3	X								
row4						X			
row5								X	
row6			X						
row7		X							
row8					9 ₂				9 ₁
row9				9 ₁					9 ₂

1 058 ne
w

	col 4	col 5	col 7	col 9
row1	9 ₂		9 ₁	
row2		9 ₁	9 ₂	
row8		9 ₂		9 ₁
row9	9 ₁			9 ₂

1 059 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2			X						
row3					X				
row4		4 ₁		4 ₂					
row5							X		
row6		4 ₂				4 ₁			
row7	X								
row8				4 ₁		4 ₂			
row9								X	

1 059 ne
w

	col 2	col 4	col 6
row4	4 ₁	4 ₂	
row6	4 ₂		4 ₁
row8		4 ₁	4 ₂

1 060 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2						X			
row3		7 ₂	7 ₁						
row4	X								
row5				7 ₁			7 ₂		
row6				7 ₂				7 ₁	
row7					X				
row8			7 ₂				7 ₁		
row9		7 ₁						7 ₂	

1 060 ne
w

	col 2	col 3	col 4	col 7	col 8
row3	7 ₂	7 ₁			
row5			7 ₁	7 ₂	
row6			7 ₂		7 ₁
row8		7 ₂		7 ₁	
row9	7 ₁				7 ₂

1 061 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					X				
row2								X	
row3		9 ₁	9 ₂						
row4						X			
row5							X		
row6	X								
row7		9 ₂							9 ₁
row8			9 ₁						9 ₂
row9				X					

1 061 ne
w

	col 2	col 3	col 9
row3	9 ₁	9 ₂	
row7	9 ₂		9 ₁
row8		9 ₁	9 ₂

1 062 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					X				
row2		X							
row3									X
row4	4 ₁			4 ₂					
row5			4 ₂	4 ₁					
row6							X		
row7	4 ₂		4 ₁						
row8						X			
row9								X	

1 062 ne
w

	col 1	col 3	col 4
row4	4 ₁		4 ₂
row5		4 ₂	4 ₁
row7	4 ₂	4 ₁	

1 063 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		2 ₁						2 ₂	
row2			2 ₂						2 ₁
row3				X					
row4						X			
row5	X								
row6							X		
row7		2 ₂						2 ₁	
row8			2 ₁						2 ₂
row9									

1 063 ne
w

	col 2	col 3	col 8	col 9
row1	2 ₁		2 ₂	
row2		2 ₂		2 ₁
row7	2 ₂		2 ₁	
row8		2 ₁		2 ₂

1064

ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2				X					
row3									X
row4					9 ₁		9 ₂		
row5						9 ₂	9 ₁		
row6		X							
row7	X								
row8								X	
row9					9 ₂	9 ₁			

1064

ne
w

	col 5	col 6	col 7
row4	9 ₁		9 ₂
row5		9 ₂	9 ₁
row9	9 ₂	9 ₁	

1 065 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				X					
row2		1 ₁							1 ₂
row3			1 ₂				1 ₁		
row4						X			
row5		1 ₂							1 ₁
row6			1 ₁				1 ₂		
row7								X	
row8					X				
row9	X								

1 065 ne
w

	col 2	col 3	col 7	col 9
row2	1 ₁			1 ₂
row3		1 ₂	1 ₁	
row5	1 ₂			1 ₁
row6		1 ₁	1 ₂	

1 066 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			1 ₁				1 ₂		
row2					X				
row3	1 ₂		1 _K						1 ₁
row4		X							
row5						X			
row6								X	
row7	1 ₁		1 _K				1 _K		1 ₂
row8				X					
row9			1 ₂				1 ₁		

1 066 ne
w

	col 1	col 3	col 7	col 9
row1		1 ₁	1 ₂	
row3	1 ₂	1 _K		1 ₁
row7	1 ₁	1 _K	1 _K	1 ₂
row9		1 ₂	1 ₁	

1 067 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			2 ₁				2 ₂		
row2				X					
row3	2 ₂							2 ₁	
row4		X							
row5						2 ₁		2 ₂	
row6					2 ₂		2 ₁		
row7	2 ₁					2 ₂			
row8			2 ₂		2 ₁				
row9									X

1 067 ne
w

	col 1	col 3	col 5	col 6	col 7	col 8
row1		2 ₁			2 ₂	
row3	2 ₂					2 ₁
row5				2 ₁		2 ₂
row6			2 ₂		2 ₁	
row7	2 ₁			2 ₂		
row8		2 ₂	2 ₁			

1 068 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					1 ₁		1 ₂₃		
row2		X							
row3				1 ₂	1 ₃				1 ₁
row4						X			
row5							1 ₁		1 ₂₃
row6			X						
row7	X								
row8								X	
row9				1 ₁₃	1 ₂				

1 068 ne
w

	col 4	col 5	col 7	col 9
row1		1 ₁	1 ₂₃	
row3	1 ₂	1 ₃		1 ₁
row5			1 ₁	1 ₂₃
row9	1 ₁₃	1 ₂		

1 069 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	5 ₁							5 ₂	
row2						X			
row3			5 ₂				5 ₁		
row4					X				
row5									X
row6		X							
row7				X					
row8			5 ₁				5 ₂		
row9	5 ₂							5 ₁	

1 069 ne
w

	col 1	col 3	col 7	col 8
row1	5 ₁			5 ₂
row3		5 ₂	5 ₁	
row8		5 ₁	5 ₂	
row9	5 ₂			5 ₁

1 070 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				1 ₁					
row2									
row3				1 _K	1 ₂				1 ₁
row4	1 ₁		1 _K				1 _K		1 ₂
row5			1 ₂				1 ₁		
row6									
row7	1 ₂			1 _K	1 ₁				
row8									
row9			1 ₁	1 ₂					

1 070 ne
w

	col 1	col 3	col 4	col 5	col 7	col 9
row1			1 ₁			
row3			1 _K	1 ₂		1 ₁
row4	1 ₁	1 _K			1 _K	1 ₂
row5		1 ₂			1 ₁	
row7	1 ₂		1 _K	1 ₁		
row9		1 ₁	1 ₂			

1071

new

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					1 ₁			1 ₂	
row2						1 ₂			1 ₁
row3	X								
row4				X					
row5			1 ₁						1 ₂
row6		1 ₂						1 ₁	
row7		1 ₁			1 ₂				
row8			1 ₂			1 ₁			
row9							X		

1071

new

	col 2	col 3	col 5	col 6	col 8	col 9
row1			1 ₁		1 ₂	
row2				1 ₂		1 ₁
row5		1 ₁				1 ₂
row6	1 ₂				1 ₁	
row7	1 ₁		1 ₂			
row8		1 ₂		1 ₁		

1 072 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			3 ₁				3 ₂		
row2				X					
row3	3 ₂								3 ₁
row4								X	
row5					X				
row6		X							
row7	3 ₁								3 ₂
row8						X			
row9			3 ₂				3 ₁		

1 072 ne
w

	col 1	col 3	col 7	col 9
row1		3 ₁	3 ₂	
row3	3 ₂			3 ₁
row7	3 ₁			3 ₂
row9		3 ₂	3 ₁	

1 073 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		2 ₁					2 ₂		
row2					X				
row3			2 ₂						2 ₁
row4						X			
row5								X	
row6	X								
row7		2 ₂					2 ₁		
row8				2 ₁					2 ₂
row9			2 ₁	2 ₂					

1 073 ne
w

	col 2	col 3	col 4	col 7	col 9
row1	2 ₁			2 ₂	
row3		2 ₂			2 ₁
row7	2 ₂			2 ₁	
row8			2 ₁		2 ₂
row9		2 ₁	2 ₂		

1 074 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		1 ₁					1 ₂		
row2			1 ₂						1 ₁
row3				X					
row4	X								
row5						1 ₁			1 ₂
row6					1 ₂		1 ₁		
row7		1 ₂			1 ₁				
row8								X	
row9			1 ₁			1 ₂			

1 074 ne
w

	col 2	col 3	col 5	col 6	col 7	col 9
row1	1 ₁				1 ₂	
row2		1 ₂				1 ₁
row5				1 ₁		1 ₂
row6			1 ₂		1 ₁	
row7	1 ₂		1 ₁			
row9		1 ₁		1 ₂		

1 075

ne
w

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1		4 ₁			4 ₂			
row2						X		
row3	4 ₂					4 ₁		
row4	4 ₁							4 ₂
row5		4 ₂					4 ₁	
row6				X				
row7						4 ₂		4 ₁
row8			X					
row9					4 ₁		4 ₂	

1 075

ne
w

col 1

col 2

col 5

col 6

col 8

col 9

row1		4 ₁	4 ₂			
row3	4 ₂			4 ₁		
row4	4 ₁					4 ₂
row5		4 ₂			4 ₁	
row7				4 ₂		4 ₁
row9			4 ₁		4 ₂	

1076

ne

w

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1						3 ₁		3 ₂	
row2						3 ₂	3 ₁		
row3	X								
row4		X							
row5					X				
row6							3 ₂	3 ₁	
row7									X
row8			X						
row9				X					

1076

ne

w

col 6

col 7

col 8

row1	3 ₁		3 ₂
row2	3 ₂	3 ₁	
row6		3 ₂	3 ₁

1 077 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	X								
row2					3 ₁		3 ₂		
row3				3 ₂				3 ₁	
row4		X							
row5									X
row6						X			
row7			X						
row8					3 ₂		3 ₁		
row9				3 ₁				3 ₂	

1 077 ne
w

	col 4	col 5	col 7	col 8
row2		3 ₁	3 ₂	
row3	3 ₂			3 ₁
row8		3 ₂	3 ₁	
row9	3 ₁			3 ₂

1 078 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		1 ₁						1 ₂	
row2	1 ₂						1 ₁		
row3				X					
row4					1 ₂			1 ₁	
row5						1 ₁	1 ₂		
row6			X						
row7									X
row8	1 ₁					1 ₂			
row9		1 ₂			1 ₁				

1 078 ne
w

	col 1	col 2	col 5	col 6	col 7	col 8
row1		1 ₁				1 ₂
row2	1 ₂				1 ₁	
row4			1 ₂			1 ₁
row5				1 ₁	1 ₂	
row8	1 ₁			1 ₂		
row9		1 ₂	1 ₁			

1079

new

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2	2 ₂			2 ₁		2 _K			
row3		2 ₁				2 ₂			
row4		2 ₂						2 ₁	
row5					X				
row6	2 ₁						2 ₂	2 _K	
row7			X						
row8				2 ₂		2 _K	2 ₁		
row9						2 ₁		2 ₂	

1079

new

	col 1	col 2	col 4	col 6	col 7	col 8
row2	2 ₂		2 ₁	2 _K		
row3		2 ₁		2 ₂		
row4		2 ₂				2 ₁
row6	2 ₁				2 ₂	2 _K
row8			2 ₂	2 _K	2 ₁	
row9				2 ₁		2 ₂

1080

ne
w

col 1col 2col 3col 4col 5col 6col 7col 8col 9

row1

X

row2

X

row3

X

row4

X

row5

2₁

2₂

row6

2₂

2₁

row7

2₁

2₂

row8

2₂

2₁

row9

X

1080

ne
w

col 1col 3col 7col 9

row5

2₁

2₂

row6

2₂

2₁

row7

2₁

2₂

row8

2₂

2₁

539

1 081 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2		8 ₁	8 ₂						
row3						X			
row4					X				
row5							8 ₁	8 ₂	
row6	X								
row7				X					
row8			8 ₁				8 ₂		
row9		8 ₂						8 ₁	

1 081 ne
w

	col 2	col 3	col 7	col 8
row2	8 ₁	8 ₂		
row5			8 ₁	8 ₂
row8		8 ₁	8 ₂	
row9	8 ₂			8 ₁

1082

ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	X								
row2				4 ₁		4 ₂			4 ₃
row3				4 ₃					4 ₁₂
row4		X							
row5							X		
row6					X				
row7									
row8				4 ₂		4 ₁₃			
row9								X	

1082

ne
w

	col 4	col 6	col 9
row2	4 ₁	4 ₂	4 ₃
row3	4 ₃		4 ₁₂
row8	4 ₂	4 ₁₃	

1 083 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						X			
row2			X						
row3							X		
row4				X					
row5		2 ₁						2 ₂	
row6	2 ₂								2 ₁
row7		2 ₂						2 ₁	
row8	2 ₁								2 ₂
row9					X				

1 083 ne
w

	col 1	col 2	col 8	col 9
row5		2 ₁	2 ₂	
row6	2 ₂			2 ₁
row7		2 ₂	2 ₁	
row8	2 ₁			2 ₂

1084

new

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		7 ₁					7 ₂		
row2			7 ₂						7 ₁
row3				X					
row4			7 ₁			7 ₂			
row5								X	
row6		7 ₂			7 ₁				
row7					7 ₂		7 ₁		
row8						7 ₁			7 ₂
row9	X								

1084

new

	col 2	col 3	col 5	col 6	col 7	col 9
row1	7 ₁				7 ₂	
row2		7 ₂				7 ₁
row4		7 ₁		7 ₂		
row6	7 ₂		7 ₁			
row7			7 ₂		7 ₁	
row8				7 ₁		7 ₂

1085

new

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	X								
row2					6 ₁				6 ₂
row3				6 ₂				6 ₁	
row4					6 ₂				6 ₁
row5				6 ₁				6 ₂	
row6		X							
row7							X		
row8						X			
row9			X						

1085

new

	col 4	col 5	col 8	col 9
row2		6 ₁		6 ₂
row3	6 ₂		6 ₁	
row4		6 ₂		6 ₁
row5	6 ₁		6 ₂	

1086

ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					X				
row2								X	
row3	1 ₁	1 ₂							
row4									X
row5				X					
row6	1 ₂		1 ₁						
row7							X		
row8		1 ₁	1 ₂						
row9						X			

1086

ne
w

	col 1	col 2	col 3
row3	1 ₁	1 ₂	
row6	1 ₂		1 ₁
row8		1 ₁	1 ₂

1 087 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2									X
row3				7 ₁	7 ₂				
row4				7 ₂			7 ₁		
row5					7 ₁		7 ₂		
row6		X							
row7	X								
row8						X			
row9								X	

1 087 ne
w

	col 4	col 5	col 7
row3	7 ₁	7 ₂	
row4	7 ₂		7 ₁
row5		7 ₁	7 ₂

1088

new

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					3 ₁		3 ₂		
row2				3 ₂					3 ₁
row3	X								
row4				3 ₁					3 ₂
row5		X							
row6					3 ₂		3 ₁		
row7								X	
row8			X						
row9						X			

1088

new

	col 4	col 5	col 7	col 9
row1		3 ₁	3 ₂	
row2	3 ₂			3 ₁
row4	3 ₁			3 ₂
row6		3 ₂	3 ₁	

1089

new

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					X				
row2									X
row3	X								
row4							X		
row5			3 ₁	3 ₂					
row6		3 ₂				3 ₁			
row7		3 ₁				3 ₂			
row8								X	
row9			3 ₂	3 ₁					

1089

new

	col 2	col 3	col 4	col 6
row5		3 ₁	3 ₂	
row6	3 ₂			3 ₁
row7	3 ₁			3 ₂
row9		3 ₂	3 ₁	

1 090 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					7 ₁			7 ₂	
row2	7 ₁			7 ₂					
row3		7 ₂						7 ₁	
row4						X			
row5			X						
row6									X
row7							X		
row8	7 ₂			7 ₁					
row9		7 ₁			7 ₂				

1 090 ne
w

	col 1	col 2	col 4	col 5	col 8
row1				7 ₁	7 ₂
row2	7 ₁		7 ₂		
row3		7 ₂			7 ₁
row8	7 ₂		7 ₁		
row9		7 ₁		7 ₂	

1 091 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2						X			
row3							X		
row4					X				
row5	2 ₁								2 ₂
row6		2 ₂							2 ₁
row7				X					
row8								X	
row9	2 ₂	2 ₁							

1 091 ne
w

	col 1	col 2	col 9
row5	2 ₁		2 ₂
row6		2 ₂	2 ₁
row9	2 ₂	2 ₁	

1092

new

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	X								
row2						X			
row3								X	
row4				5 ₁			5 ₂		
row5					5 ₂				5 ₁
row6		X							
row7							5 ₁		5 ₂
row8			X						
row9				5 ₂	5 ₁				

1092

new

	col 4	col 5	col 7	col 8	col 9
row4	5 ₁		5 ₂		
row5		5 ₂			5 ₁
row7			5 ₁		5 ₂
row9	5 ₂	5 ₁			

1093

new

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			5 ₁				5 ₂		
row2						X			
row3	5 ₂							5 ₁	
row4		X							
row5									X
row6				X					
row7	5 ₁							5 ₂	
row8			5 ₂				5 ₁		
row9					X				

1093

new

	col 1	col 3	col 7	col 8
row1		5 ₁	5 ₂	
row3	5 ₂			5 ₁
row7	5 ₁			5 ₂
row8		5 ₂	5 ₁	

1094

new

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1								X	
row2					X				
row3	X								
row4									X
row5			4 ₁			4 ₂			
row6		4 ₂		4 ₁					
row7		4 ₁		4 ₂					
row8			4 ₂			4 ₁			
row9							X		

1094

new

	col 2	col 3	col 4	col 6
row5		4 ₁		4 ₂
row6	4 ₂		4 ₁	
row7	4 ₁		4 ₂	
row8		4 ₂		4 ₁

1095

new

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			2 ₁				2 ₂		
row2		2 ₂							2 ₁
row3					X				
row4						X			
row5		2 ₁							2 ₂
row6			2 ₂				2 ₁		
row7								X	
row8	X								
row9				X					

1095

new

	col 2	col 3	col 7	col 9
row1		2 ₁	2 ₂	
row2	2 ₂			2 ₁
row5	2 ₁			2 ₂
row6		2 ₂	2 ₁	

1096

ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2	X								
row3				X					
row4					1 ₁			1 ₂	
row5						1 ₂	1 ₁		
row6			X						
row7						1 ₁	1 ₂		
row8		X							
row9					1 ₂			1 ₁	

1096

ne
w

	col 5	col 6	col 7	col 8
row4	1 ₁			1 ₂
row5		1 ₂	1 ₁	
row7		1 ₁	1 ₂	
row9	1 ₂			1 ₁

1 097 ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		X							
row2				X					
row3									X
row4	X								
row5					1 ₁	1 ₂			
row6								X	
row7			1 ₂			1 ₁			
row8			1 ₁		1 ₂				
row9							X		

1 097 ne
w

	col 3	col 5	col 6
row5		1 ₁	1 ₂
row7	1 ₂		1 ₁
row8	1 ₁	1 ₂	

1098

new

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				X					
row2			4 ₂						4 ₁
row3		4 ₁						4 ₂	
row4	X								
row5							4 ₁		4 ₂
row6					X				
row7		4 ₂						4 ₁	
row8			4 ₁				4 ₂		
row9						X			

1098

new

	col 2	col 3	col 7	col 8	col 9
row2		4 ₂			4 ₁
row3	4 ₁			4 ₂	
row5			4 ₁		4 ₂
row7	4 ₂			4 ₁	
row8		4 ₁	4 ₂		

1099

new

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2			9 ₁			9 ₂			
row3			9 ₂	9 ₁					
row4	X								
row5					X				
row6							X		
row7		9 ₂				9 ₁			
row8								X	
row9		9 ₁		9 ₂					

1099

new

	col 2	col 3	col 4	col 6
row2		9 ₁		9 ₂
row3		9 ₂	9 ₁	
row7	9 ₂			9 ₁
row9	9 ₁		9 ₂	

1100

ne		col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
w										
row1			1 ₁						1 ₂	
row2		1 ₂								1 ₁
row3				X						
row4			X							
row5								X		
row6							X			
row7			1 ₂						1 ₁	
row8		1 ₁								1 ₂
row9					X					

1100

ne		col 1	col 2	col 8	col 9
w					
row1			1 ₁	1 ₂	
row2		1 ₂			1 ₁
row7			1 ₂	1 ₁	
row8		1 ₁			1 ₂

1101

ne
w

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			7 ₁					7 ₂	
row2						X			
row3	7 ₂								7 ₁
row4	7 ₁								7 ₂
row5			7 ₂					7 ₁	
row6				X					
row7							X		
row8		X							
row9					X				

1101

ne
w

	col 1	col 3	col 8	col 9
row1		7 ₁	7 ₂	
row3	7 ₂			7 ₁
row4	7 ₁			7 ₂
row5		7 ₂	7 ₁	

1102

		ne	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		w									
row1			1 ₁						1 ₂		
							X				
				1 ₂							1 ₁
				1 ₁				1 ₂			
										X	
			1 ₂			1 ₁					
					X						
						1 ₂			1 ₁		
								1 ₁			1 ₂

1102

		ne	col 1	col 2	col 4	col 6	col 7	col 9
		w						
row1			1 ₁				1 ₂	
				1 ₂				1 ₁
				1 ₁		1 ₂		
			1 ₂		1 ₁			
					1 ₂		1 ₁	
						1 ₁		1 ₂

1103

ne

w

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1								X
row2	5 ₁		5 ₂					
row3						X		
row4				X				
row5		5 ₂	5 ₁					
row6							X	
row7	5 ₂	5 ₁						
row8						X		
row9					X			

1103

ne

w

col 1

col 2

col 3

row2	5 ₁		5 ₂
row5		5 ₂	5 ₁
row7	5 ₂	5 ₁	

1104

		ne	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
		w									
	row1										X
	row2				X						
	row3	X									
	row4									X	
	row5		X								
	row6						X				
	row7					1 ₁		1 ₂			
	row8			1 ₂				1 ₁			
	row9			1 ₁		1 ₂					

1104

		ne	col 3	col 5	col 7
		w			
	row7		1 ₁	1 ₂	
	row8		1 ₂		1 ₁
	row9		1 ₁	1 ₂	

1105

new		col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							X			
row2								X		
row3	X									
row4										X
row5			2 ₁	2 ₂						
row6		2 ₂			2 ₁					
row7					2 ₂				2 ₁	
row8			2 ₂	2 ₁						
row9		2 ₁							2 ₂	

1105

col 2	col 3	col 4	col 5	col 8
	2 ₁	2 ₂		
2 ₂			2 ₁	
			2 ₂	2 ₁
	2 ₂	2 ₁		
2 ₁				2 ₂

PATTERN FILE 2

2 001 ML

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	X								
row2				6 ₁		6 ₂	6 ₃₄		
row3					6 ₃₄			6 ₁₂	
row4		X							
row5				6 ₂₃		6 ₁₄			
row6									X
row7					6 ₁₂			6 ₃₄	
row8				6 ₄		6 ₃	6 ₁₂		
row9			X						

2 001 ML

	col 4	col 5	col 6	col 7	col 8
row2	6 ₁		6 ₂	6 ₃₄	
row3		6 ₃₄			6 ₁₂
row5	6 ₂₃		6 ₁₄		
row7		6 ₁₂			6 ₃₄
row8	6 ₄		6 ₃	6 ₁₂	

2 002 D

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2				1 ₁			1 ₂₃		
row3				1 ₂	1 ₃			1 ₁	
row4									
row5									
row6							1 ₁	1 ₂₃	
row7									
row8									
row9				1 ₃	1 ₁₂				

2 002 D

	col 4	col 5	col 7	col 8
row2	1 ₁		1 ₂₃	
row3	1 ₂	1 ₃		1 ₁
row6			1 ₁	1 ₂₃
row9	1 ₃	1 ₁₂		

2 003 D

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2							5 ₃	5 ₁₂	
row3				5 ₂₃		5 ₁			
row4									
row5		X							
row6									X
row7				5 ₁		5 ₂		5 ₃	
row8	X								
row9						5 ₃	5 ₁₂		

2 003 D

	col 4	col 6	col 7	col 8
row2			5 ₃	5 ₁₂
row3	5 ₂₃	5 ₁		
row7	5 ₁	5 ₂		5 ₃
row9		5 ₃	5 ₁₂	

2 004 E

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							9 ₁	9 ₂₃	
row2				X					
row3			X						
row4					9 ₁		9 ₂₃		
row5					9 ₂	9 ₃		9 ₁	
row6		X							
row7	9 ₃					9 ₁₂			
row8	9 ₁₂				9 ₃				
row9									X

2 004 E

	col 1	col 5	col 6	col 7	col 8
row1				9 ₁	9 ₂₃
row4		9 ₁		9 ₂₃	
row5		9 ₂	9 ₃		9 ₁
row7	9 ₃		9 ₁₂		
row8	9 ₁₂	9 ₃			

2 005 ML

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	1 ₃₄								1 ₁₂
row2		1 ₁₂					1 ₃	1 ₄	
row3				X					
row4					X				
row5							1 ₂₄	1 ₁₃	
row6			X						
row7						X			
row8		1 ₃₄					1 ₁	1 ₂	
row9	1 ₁₂								1 ₃₄

2 005 ML

	col 1	col 2	col 7	col 8	col 9
row1	1 ₃₄				1 ₁₂
row2		1 ₁₂	1 ₃	1 ₄	
row5			1 ₂₄	1 ₁₃	
row8		1 ₃₄	1 ₁	1 ₂	
row9	1 ₁₂				1 ₃₄

2 006 D

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2							1 ₁₂		1 ₃
row3				X					
row4						X			
row5								X	
row6	1 ₂₃	1 ₁							
row7	1 ₁	1 ₂					1 ₃		
row8					X				
row9		1 ₃							1 ₁₂

2 006 D

	col 1	col 2	col 7	col 9
row2			1 ₁₂	1 ₃
row6	1 ₂₃	1 ₁		
row7	1 ₁	1 ₂	1 ₃	
row9		1 ₃		1 ₁₂

2007

G2

L

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1			X					
row2								X
row3				X				
row4	6 ₁₂						6 ₃	
row5		6 ₃						6 ₁₂
row6					X			
row7		6 ₁				6 ₂	6 ₃	
row8	6 ₃						6 ₁₂	
row9		6 ₂				6 ₁₃		

2007

G2

L

col 1

col 2

col 6

col 7

col 8

row4	6 ₁₂			6 ₃	
row5		6 ₃			6 ₁₂
row7		6 ₁	6 ₂		6 ₃
row8	6 ₃			6 ₁₂	
row9		6 ₂	6 ₁₃		

2 008 F

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	5 ₃				5 ₁	5 ₂			
row2	5 ₁₂					5 ₃			
row3								5 ₁	5 ₂₃
row4							X		
row5		X							
row6				X					
row7			X						
row8						5 ₁		5 ₂₃	
row9					5 ₂₃				5 ₁

2 008 F

	col 1	col 5	col 6	col 8	col 9
row1	5 ₃	5 ₁	5 ₂		
row2	5 ₁₂		5 ₃		
row3				5 ₁	5 ₂₃
row8			5 ₁	5 ₂₃	
row9		5 ₂₃			5 ₁

2 009 X9

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							X		
row2	8 ₁	8 ₂₃	8 ₄						
row3				X					
row4									X
row5	8 ₂	8 ₁₄	8 ₃						
row6					X				
row7			8 ₁₂					8 ₃₄	
row8	8 ₃₄							8 ₁₂	
row9						X			

2 009 X9

	col 1	col 2	col 3	col 8
row2	8 ₁	8 ₂₃	8 ₄	
row5	8 ₂	8 ₁₄	8 ₃	
row7			8 ₁₂	8 ₃₄
row8	8 ₃₄			8 ₁₂

2 010 D

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2							X		
row3					9 ₂₃	9 ₁			
row4				X					
row5							9 ₁₂		9 ₃
row6		X							
row7						9 ₂₃			9 ₁
row8					9 ₁		9 ₃		9 ₂
row9	X								

2 010 D

	col 5	col 6	col 7	col 9
row3	9 ₂₃	9 ₁		
row5			9 ₁₂	9 ₃
row7		9 ₂₃		9 ₁
row8	9 ₁		9 ₃	9 ₂

2 011 D

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2					X				
row3		6 ₃	6 ₁₂						
row4							X		
row5			6 ₃	6 ₁		6 ₂			
row6		6 ₁₂				6 ₃			
row7								X	
row8				6 ₂₃		6 ₁			
row9	X								

2 011 D

	col 2	col 3	col 4	col 6
row3	6 ₃	6 ₁₂		
row5		6 ₃	6 ₁	6 ₂
row6	6 ₁₂			6 ₃
row8			6 ₂₃	6 ₁

2 012 W6

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2				2 ₂₃			2 ₁		
row3					2 ₁				2 ₂₃
row4						X			
row5			2 ₁₃				2 ₂		
row6		2 ₂						2 ₁₃	
row7					2 ₂₃				2 ₁
row8		2 ₁₃						2 ₂	
row9			2 ₂	2 ₁			2 ₃		

2 012 W6

	col 2	col 3	col 4	col 5	col 7	col 8	col 9
row2			2 ₂₃		2 ₁		
row3				2 ₁			2 ₂₃
row5		2 ₁₃			2 ₂		
row6	2 ₂					2 ₁₃	
row7				2 ₂₃			2 ₁
row8	2 ₁₃					2 ₂	
row9		2 ₂	2 ₁		2 ₃		

2 013 P

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		X							
row2				X					
row3							3 ₂₄		3 ₁₃
row4	3 ₃₄						3 ₁		3 ₂
row5					X				
row6	3 ₁₂						3 ₃		3 ₄
row7						X			
row8			X						
row9								X	

2 013 P

	col 1	col 7	col 9
row3		3 ₂₄	3 ₁₃
row4	3 ₃₄	3 ₁	3 ₂
row6	3 ₁₂	3 ₃	3 ₄

2 014 U3

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							X		
row2	8 ₁		8 ₃	8 ₂₄		8 _K			
row3			8 ₂₄			8 ₁₃			
row4			8 ₁			8 ₂		8 ₃₄	
row5	8 ₂		8 _K	8 ₁₃		8 ₄			
row6	8 ₃₄							8 ₁₂	
row7									X
row8		X							
row9					X				

2 014 U3

	col 1	col 3	col 4	col 6	col 8
row2	8 ₁	8 ₃	8 ₂₄	8 _K	
row3		8 ₂₄		8 ₁₃	
row4		8 ₁		8 ₂	8 ₃₄
row5	8 ₂	8 _K	8 ₁₃	8 ₄	
row6	8 ₃₄				8 ₁₂

2015

G2

L

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1								X
row2				X				
row3	2 ₁₃		2 ₂					
row4		2 ₁					2 ₂₃	
row5	2 ₂		2 ₃				2 ₁	
row6			X					
row7		2 ₂₃			2 ₁			
row8			2 ₁			2 ₂₃		
row9					2 ₂₃		2 ₁	

2015

G2

L

col 1

col 2

col 3

col 6

col 7

col 8

row3	2 ₁₃		2 ₂		
row4		2 ₁			2 ₂₃
row5	2 ₂		2 ₃		2 ₁
row7		2 ₂₃		2 ₁	
row8			2 ₁	2 ₂₃	
row9			2 ₂₃		2 ₁

2 016 ML

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2					X				
row3		X							
row4			5 ₁₂					5 ₃₄	
row5	5 ₃			5 ₂₄			5 ₁		
row6	5 ₄			5 ₁₃			5 ₂		
row7						X			
row8	5 ₁₂						5 ₃₄		
row9			5 ₃₄					5 ₁₂	

2 016 ML

	col 1	col 3	col 4	col 7	col 8
row4		5 ₁₂			5 ₃₄
row5	5 ₃		5 ₂₄	5 ₁	
row6	5 ₄		5 ₁₃	5 ₂	
row8	5 ₁₂			5 ₃₄	
row9		5 ₃₄			5 ₁₂

2017

G2

L

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					5 ₁			5 ₂₃	
row2				5 ₂		5 ₃	5 ₁		
row3	X								
row4				5 ₃		5 ₁₂			
row5		X							
row6									X
row7			X						
row8				5 ₁			5 ₂₃		
row9					5 ₂₃			5 ₁	

2017

G2

L

	col 4	col 5	col 6	col 7	col 8
row1		5 ₁			5 ₂₃
row2	5 ₂		5 ₃	5 ₁	
row4	5 ₃		5 ₁₂		
row8	5 ₁			5 ₂₃	
row9		5 ₂₃			5 ₁

2 018 Q

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						X			
row2								X	
row3			X						
row4	6 ₃₄						6 ₁		6 ₂
row5					X				
row6	6 ₁₂						6 ₃		6 ₄
row7		6 ₂₄							6 ₁₃
row8				X					
row9		6 ₁₃					6 ₂₄		

2 018 Q

	col 1	col 2	col 7	col 9
row4	6 ₃₄		6 ₁	6 ₂
row6	6 ₁₂		6 ₃	6 ₄
row7		6 ₂₄		6 ₁₃
row9		6 ₁₃	6 ₂₄	

2019

G2

L

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						X			
row2	6 ₁₂								6 ₃
row3		6 ₃						6 ₁₂	
row4		6 ₁		6 ₂₃					
row5	6 ₃								6 ₁₂
row6		6 ₂		6 ₁				6 ₃	
row7			X						
row8					X				
row9							X		

2019

G2

L

	col 1	col 2	col 4	col 8	col 9
row2	6 ₁₂				6 ₃
row3		6 ₃		6 ₁₂	
row4		6 ₁	6 ₂₃		
row5	6 ₃				6 ₁₂
row6		6 ₂	6 ₁	6 ₃	

2020

A4L

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	1 ₃			1 ₁	1 ₂				
row2	1 ₁₂					1 ₃			
row3									X
row4							X		
row5		X							
row6				1 ₂₃	1 ₁				
row7			X						
row8								X	
row9					1 ₃	1 ₁₂			

2020

D

	col 1	col 4	col 5	col 6
row1	1 ₃	1 ₁	1 ₂	
row2	1 ₁₂			1 ₃
row6		1 ₂₃	1 ₁	
row9			1 ₃	1 ₁₂

2021

G2

L

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1								X
row2				2 ₃		2 ₁₂		
row3	X							
row4					2 ₁		2 ₂₃	
row5				2 ₂		2 ₃	2 ₁	
row6			X					
row7		X						
row8				2 ₁			2 ₂₃	
row9					2 ₂₃		2 ₁	

2021

G2

L

col 4

col 5

col 6

col 7

col 8

row2	2 ₃		2 ₁₂		
row4		2 ₁			2 ₂₃
row5	2 ₂		2 ₃	2 ₁	
row8	2 ₁			2 ₂₃	
row9		2 ₂₃			2 ₁

2 022 ML

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	1 ₁			1 ₂₃			1 ₄		
row2	1 ₂			1 ₁₄			1 ₃		
row3			1 ₃₄					1 ₁₂	
row4						X			
row5		X							
row6									X
row7	1 ₃₄						1 ₁₂		
row8					X				
row9			1 ₁₂					1 ₃₄	

2 022 ML

	col 1	col 3	col 4	col 7	col 8
row1	1 ₁		1 ₂₃	1 ₄	
row2	1 ₂		1 ₁₄	1 ₃	
row3		1 ₃₄			1 ₁₂
row7	1 ₃₄			1 ₁₂	
row9		1 ₁₂			1 ₃₄

2 023 A1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	X								
row2								X	
row3						X			
row4			3 ₃	3 ₁	3 ₂				
row5			3 ₁₂	3 ₃					
row6									X
row7							X		
row8		X							
row9				3 ₂	3 ₁₃				

2 023 A1

	col 3	col 4	col 5
row4	3 ₃	3 ₁	3 ₂
row5	3 ₁₂	3 ₃	
row9		3 ₂	3 ₁₃

2 024 ML

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		9 ₃₄			9 ₁			9 ₂	
row2				9 ₂₃					9 ₁₄
row3		9 ₁₂			9 ₄			9 ₃	
row4					9 ₂₃			9 ₁₄	
row5				9 ₁₄					9 ₂₃
row6	X								
row7						X			
row8			X						
row9							X		

2 024 ML

	col 2	col 4	col 5	col 8	col 9
row1	9 ₃₄		9 ₁	9 ₂	
row2		9 ₂₃			9 ₁₄
row3	9 ₁₂		9 ₄	9 ₃	
row4			9 ₂₃	9 ₁₄	
row5		9 ₁₄			9 ₂₃

2 025 U2

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					8 ₂₄	8 ₁₃			
row2		8 ₁	8 ₂				8 ₃₄		
row3		8 ₃	8 ₄			8 _K	8 ₁₂		
row4			8 ₁₃			8 ₂₄			
row5		8 ₂₄			8 ₁₃				
row6								X	
row7	X								
row8				X					
row9									X

2 025 U2

	col 2	col 3	col 5	col 6	col 7
row1			8 ₂₄	8 ₁₃	
row2	8 ₁	8 ₂			8 ₃₄
row3	8 ₃	8 ₄		8 _K	8 ₁₂
row4		8 ₁₃		8 ₂₄	
row5	8 ₂₄		8 ₁₃		

2 026 E

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1								1 ₁₂	1 ₃
row2			1 ₁₃			1 ₂			
row3		1 ₂				1 ₁₃			
row4	X								
row5				X					
row6							X		
row7					X				
row8		1 ₁	1 ₂					1 ₃	
row9		1 ₃							1 ₁₂

2 026 E

	col 2	col 3	col 6	col 8	col 9
row1				1 ₁₂	1 ₃
row2		1 ₁₃	1 ₂		
row3	1 ₂		1 ₁₃		
row8	1 ₁	1 ₂		1 ₃	
row9	1 ₃				1 ₁₂

2027

G2

L

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1					X			
row2		9 ₁₃					9 ₂	
row3	9 ₂							9 ₁₃
row4							X	
row5			X					
row6						X		
row7	9 ₁			9 ₃				9 ₂
row8		9 ₂					9 ₁₃	
row9	9 ₃			9 ₁₂				

2027

G2

L

col 1

col 2

col 4

col 7

col 9

row2		9 ₁₃		9 ₂	
row3	9 ₂				9 ₁₃
row7	9 ₁		9 ₃		9 ₂
row8		9 ₂		9 ₁₃	
row9	9 ₃		9 ₁₂		

2 028 P

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		1 ₁	1 ₂					1 ₃₄	
row2		1 ₃	1 ₄					1 ₁₂	
row3					X				
row4				X					
row5	X								
row6									X
row7							X		
row8		1 ₂₄	1 ₁₃						
row9						X			

2 028 P

	col 2	col 3	col 8
row1	1 ₁	1 ₂	1 ₃₄
row2	1 ₃	1 ₄	1 ₁₂
row8	1 ₂₄	1 ₁₃	

2029

G2

L

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1			1 ₂		1 ₃		1 ₁		
row2			1 ₁₃				1 ₂		
row3						1 ₁₂			1 ₃
row4	X								
row5						1 ₃			1 ₁₂
row6					1 ₁₂		1 ₃		
row7								X	
row8		X							
row9				X					

2029

G2

L

col 3

col 5

col 6

col 7

col 9

row1	1 ₂	1 ₃		1 ₁	
row2	1 ₁₃			1 ₂	
row3			1 ₁₂		1 ₃
row5			1 ₃		1 ₁₂
row6		1 ₁₂		1 ₃	

2 030 A3

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				X					
row2							X		
row3	3 ₁	3 ₂	3 ₃						
row4	3 ₂	3 ₁₃							
row5								X	
row6					X				
row7						X			
row8	3 ₃		3 ₁₂						
row9									X

2 030 A3

	col 1	col 2	col 3
row3	3 ₁	3 ₂	3 ₃
row4	3 ₂	3 ₁₃	
row8	3 ₃		3 ₁₂

2 031 H

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2				2 ₃		2 ₁₂			
row3	X								
row4					2 ₁			2 ₂₃	
row5				2 ₂		2 ₃	2 ₁		
row6			X						
row7		X							
row8				2 ₁			2 ₂₃		
row9					2 ₂₃			2 ₁	

2 031 H

	col 4	col 5	col 6	col 7	col 8
row2	2 ₃		2 ₁₂		
row4		2 ₁			2 ₂₃
row5	2 ₂		2 ₃	2 ₁	
row8	2 ₁			2 ₂₃	
row9		2 ₂₃			2 ₁

2 032 W6

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	X								
row2				5 ₂₃			5 ₁		
row3					5 ₁			5 _K	5 ₂₃
row4						X			
row5			5 ₁₃				5 ₂		
row6		5 ₂						5 ₁₃	
row7		5 _K			5 ₂₃				5 ₁
row8		5 ₁₃						5 ₂	
row9			5 ₂	5 ₁			5 ₃		

2 032 W6

	col 2	col 3	col 4	col 5	col 7	col 8	col 9
row2			5 ₂₃		5 ₁		
row3				5 ₁		5 _K	5 ₂₃
row5		5 ₁₃			5 ₂		
row6	5 ₂					5 ₁₃	
row7	5 _K			5 ₂₃			5 ₁
row8	5 ₁₃					5 ₂	
row9		5 ₂	5 ₁		5 ₃		

2 033 W8

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		1 ₁			1 ₂₃				
row2	1 ₂		1 _K	1 ₁			1 ₃		
row3			1 ₃					1 ₁₂	
row4			1 ₁₂					1 ₃	
row5	1 ₃		1 _K				1 ₁₂		
row6						X			
row7									X
row8	1 ₁			1 ₂₃					
row9		1 ₂₃			1 ₁				

2 033 W8

	col 1	col 2	col 3	col 4	col 5	col 7	col 8
row1		1 ₁			1 ₂₃		
row2	1 ₂		1 _K	1 ₁		1 ₃	
row3			1 ₃				1 ₁₂
row4			1 ₁₂				1 ₃
row5	1 ₃		1 _K			1 ₁₂	
row8	1 ₁			1 ₂₃			
row9		1 ₂₃			1 ₁		

2 034 ML

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				X					
row2									X
row3	X								
row4							X		
row5			1 ₁₄			1 ₂₃			
row6		1 ₂₃			1 ₁₄				
row7		1 ₁			1 ₂			1 ₃₄	
row8			1 ₂₃			1 ₁₄			
row9		1 ₄			1 ₃			1 ₁₂	

2 034 ML

	col 2	col 3	col 5	col 6	col 8
row5		1 ₁₄		1 ₂₃	
row6	1 ₂₃		1 ₁₄		
row7	1 ₁		1 ₂		1 ₃₄
row8		1 ₂₃		1 ₁₄	
row9	1 ₄		1 ₃		1 ₁₂

2 035 ML

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					3 ₃₄			3 ₁₂	
row2						3 ₁₂	3 ₃		3 ₄
row3	X								
row4		X							
row5							3 ₂₄		3 ₁₃
row6				X					
row7			X						
row8						3 ₃₄	3 ₁		3 ₂
row9					3 ₁₂			3 ₃₄	

2 035 ML

	col 5	col 6	col 7	col 8	col 9
row1	3 ₃₄			3 ₁₂	
row2		3 ₁₂	3 ₃		3 ₄
row5			3 ₂₄		3 ₁₃
row8		3 ₃₄	3 ₁		3 ₂
row9	3 ₁₂			3 ₃₄	

2036

G4

L

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1		9 ₃	9 ₁₂					
row2						X		
row3							X	
row4							X	
row5		9 ₁₂		9 ₃				
row6	9 ₃				9 ₁₂			
row7	9 ₁							9 ₂₃
row8	9 ₂				9 ₃			9 ₁
row9			9 ₃	9 ₁₂				

2036

G4

L

col 1

col 2

col 3

col 4

col 5

col 9

row1		9 ₃	9 ₁₂			
row5		9 ₁₂		9 ₃		
row6	9 ₃				9 ₁₂	
row7	9 ₁					9 ₂₃
row8	9 ₂				9 ₃	9 ₁
row9			9 ₃	9 ₁₂		

2 037 U3

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				2 ₃₄			2 ₁	2 ₂	
row2		X							
row3						2 ₁₂		2 ₃₄	
row4			2 ₂₄			2 ₃		2 ₁	
row5			2 ₁₃			2 ₄	2 ₂		
row6				2 ₁₂			2 ₃₄	2 _K	
row7									X
row8					X				
row9	X								

2 037 U3

	col 3	col 4	col 6	col 7	col 8
row1		2 ₃₄		2 ₁	2 ₂
row3			2 ₁₂		2 ₃₄
row4	2 ₂₄		2 ₃		2 ₁
row5	2 ₁₃		2 ₄	2 ₂	
row6		2 ₁₂		2 ₃₄	2 _K

2 038 A1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2							X		
row3					δ_{13}	δ_2			
row4	X								
row5						δ_1	δ_{23}		
row6					δ_2	δ_3	δ_1		
row7									X
row8		X							
row9				X					

2 038 A1

	col 5	col 6	col 7
row3	δ_{13}	δ_2	
row5		δ_1	δ_{23}
row6	δ_2	δ_3	δ_1

2 039 A4

L col 1 col 2 col 3 col 4 col 5 col 6 col 7 col 8 col 9

row1	7 ₁		7 ₂						7 ₃
row2					X				
row3		7 ₃							7 ₁₂
row4							X		
row5		7 ₁₂	7 ₃						
row6				X					
row7						X			
row8							X		
row9	7 ₂₃		7 ₁						

2 039 A4

L col 1 col 2 col 3 col 9

row1	7 ₁		7 ₂	7 ₃
row3		7 ₃		7 ₁₂
row5		7 ₁₂	7 ₃	
row9	7 ₂₃		7 ₁	

2 040 ML

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				X					
row2	X								
row3							X		
row4					5 ₁₄			5 ₂₃	
row5						5 ₂₃			5 ₁₄
row6			X						
row7		5 ₃₄			5 ₂			5 ₁	
row8						5 ₁₄			5 ₂₃
row9		5 ₁₂			5 ₃			5 ₄	

2 040 ML

	col 2	col 5	col 6	col 8	col 9
row4		5 ₁₄		5 ₂₃	
row5			5 ₂₃		5 ₁₄
row7	5 ₃₄	5 ₂		5 ₁	
row8			5 ₁₄		5 ₂₃
row9	5 ₁₂	5 ₃		5 ₄	

2 041 Q

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	X								
row2								X	
row3				X					
row4			7 ₃₄				7 ₁		7 ₂
row5						X			
row6			7 ₁₂				7 ₃		7 ₄
row7		X							
row8					7 ₂₄				7 ₁₃
row9					7 ₁₃		7 ₂₄		

2 041 Q

	col 3	col 5	col 7	col 9
row4	7 ₃₄		7 ₁	7 ₂
row6	7 ₁₂		7 ₃	7 ₄
row8		7 ₂₄		7 ₁₃
row9		7 ₁₃	7 ₂₄	

2 042 ML

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		9 ₃₄			9 ₁			9 ₂	
row2				9 ₂₃					9 ₁₄
row3		9 ₁₂			9 ₄			9 ₃	
row4					9 ₂₃			9 ₁₄	
row5				9 ₁₄					9 ₂₃
row6	X								
row7						X			
row8			X						
row9							X		

2 042 ML

	col 2	col 4	col 5	col 8	col 9
row1	9 ₃₄		9 ₁	9 ₂	
row2		9 ₂₃			9 ₁₄
row3	9 ₁₂		9 ₄	9 ₃	
row4			9 ₂₃	9 ₁₄	
row5		9 ₁₄			9 ₂₃

2 043 ML

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	4 ₁					4 ₂₃	4 ₄		
row2	4 ₂					4 ₁₄	4 ₃		
row3			4 ₃₄					4 ₁₂	
row4				X					
row5		X							
row6									X
row7	4 ₃₄						4 ₁₂		
row8					X				
row9			4 ₁₂					4 ₃₄	

2 043 ML

	col 1	col 3	col 6	col 7	col 8
row1	4 ₁		4 ₂₃	4 ₄	
row2	4 ₂		4 ₁₄	4 ₃	
row3		4 ₃₄			4 ₁₂
row7	4 ₃₄			4 ₁₂	
row9		4 ₁₂			4 ₃₄

2 044 F

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					3 ₃			3 ₁₂	
row2						3 ₁₂	3 ₃		
row3	X								
row4		3 ₂₃			3 ₁				
row5		3 ₁			3 ₂	3 ₃			
row6									X
row7			X						
row8							3 ₁₂	3 ₃	
row9				X					

2 044 F

	col 2	col 5	col 6	col 7	col 8
row1		3 ₃			3 ₁₂
row2			3 ₁₂	3 ₃	
row4	3 ₂₃	3 ₁			
row5	3 ₁	3 ₂	3 ₃		
row8				3 ₁₂	3 ₃

2045

G5

L

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1		1 ₂₃					1 ₁	
row2				1 ₁₃				1 ₂
row3		1 ₁			1 ₂		1 ₃	
row4				1 ₂		1 ₁₃		
row5			X					
row6							X	
row7					1 ₁₃		1 ₂	
row8						1 ₂		1 ₁₃
row9	X							

2045

G5

L

col 2

col 4

col 5

col 6

col 8

col 9

row1	1 ₂₃				1 ₁	
row2		1 ₁₃				1 ₂
row3	1 ₁		1 ₂		1 ₃	
row4		1 ₂		1 ₁₃		
row7			1 ₁₃		1 ₂	
row8				1 ₂		1 ₁₃

2046

G2

L

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	X								
row2				6 ₂					6 ₁₃
row3					6 ₁₃			6 ₂	
row4		6 ₃			6 ₂			6 ₁	
row5				6 ₁₃					6 ₂
row6		6 ₁₂						6 ₃	
row7							X		
row8			X						
row9						X			

2046

G2

L

	col 2	col 4	col 5	col 8	col 9
row2	6 ₂				6 ₁₃
row3			6 ₁₃	6 ₂	
row4	6 ₃		6 ₂	6 ₁	
row5		6 ₁₃			6 ₂
row6	6 ₁₂			6 ₃	

2 047 A1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					1 ₁	1 ₂			1 ₃
row2	X								
row3					1 ₃				1 ₁₂
row4								X	
row5					1 ₂	1 ₁₃			
row6		X							
row7				X					
row8							X		
row9			X						

2 047 A1

	col 5	col 6	col 9
row1	1 ₁	1 ₂	1 ₃
row3	1 ₃		1 ₁₂
row5	1 ₂	1 ₁₃	

2 048 A1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				2 ₁	2 ₂		2 ₃		
row2					2 ₃		2 ₁₂		
row3			X						
row4									X
row5						X			
row6		X							
row7				2 ₂₃	2 ₁				
row8								X	
row9	X								

2 048 A1

	col 4	col 5	col 7
row1	2 ₁	2 ₂	2 ₃
row2		2 ₃	2 ₁₂
row7	2 ₂₃	2 ₁	

2049

G2

L

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1		X						
row2						X		
row3								X
row4	1 ₁				1 ₂		1 ₃	
row5				1 ₁₃			1 ₂	
row6	1 ₂₃						1 ₁	
row7				1 ₂			1 ₁₃	
row8					1 ₁₃		1 ₂	
row9			X					

2049

G2

L

col 1

col 4

col 5

col 7

col 8

row4	1 ₁		1 ₂	1 ₃	
row5		1 ₁₃			1 ₂
row6	1 ₂₃			1 ₁	
row7		1 ₂			1 ₁₃
row8			1 ₁₃	1 ₂	

2 050 D

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		2 ₁				2 ₂₃			
row2							X		
row3	2 ₂₃					2 ₁			
row4									X
row5			X						
row6				X					
row7					X				
row8	2 ₁	2 ₂						2 ₃	
row9		2 ₃						2 ₁₂	

2 050 D

	col 1	col 2	col 6	col 8
row1		2 ₁	2 ₂₃	
row3	2 ₂₃		2 ₁	
row8	2 ₁	2 ₂		2 ₃
row9		2 ₃		2 ₁₂

2051

A4

L

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	1 ₃			1 ₁	1 ₂				
row2	1 ₁₂					1 ₃			
row3									X
row4							X		
row5		X							
row6				1 ₂₃	1 ₁				
row7			X						
row8								X	
row9					1 ₃	1 ₁₂			

2051

A4

L

	col 1	col 4	col 5	col 6
row1	1 ₃	1 ₁	1 ₂	
row2	1 ₁₂			1 ₃
row6		1 ₂₃	1 ₁	
row9			1 ₃	1 ₁₂

2 052 P

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1								X	
row2	7 ₃₄			7 ₁		7 ₂			
row3	7 ₁₂			7 ₃		7 ₄			
row4			X						
row5					X				
row6							X		
row7				7 ₂₄		7 ₁₃			
row8		X							
row9									X

2 052 P

	col 1	col 4	col 6
row2	7 ₃₄	7 ₁	7 ₂
row3	7 ₁₂	7 ₃	7 ₄
row7		7 ₂₄	7 ₁₃

2 053 L2

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		X							
row2					3 ₁			3 ₂₃	
row3				3 ₂	3 ₃				3 ₁
row4			X						
row5						X			
row6							X		
row7				3 ₃	3 ₂			3 ₁	
row8	X								
row9				3 ₁					3 ₂₃

2 053 L2

	col 4	col 5	col 8	col 9
row2		3 ₁	3 ₂₃	
row3	3 ₂	3 ₃		3 ₁
row7	3 ₃	3 ₂	3 ₁	
row9	3 ₁			3 ₂₃

2 054 ML

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		5 ₁₂			5 ₃			5 ₄	
row2				5 ₁₄					5 ₂₃
row3		5 ₃₄			5 ₂			5 ₁	
row4	X								
row5				5 ₂₃					5 ₁₄
row6					5 ₁₄			5 ₂₃	
row7						X			
row8			X						
row9							X		

2 054 ML

	col 2	col 4	col 5	col 8	col 9
row1	5 ₁₂		5 ₃	5 ₄	
row2		5 ₁₄			5 ₂₃
row3	5 ₃₄		5 ₂	5 ₁	
row5		5 ₂₃			5 ₁₄
row6			5 ₁₄	5 ₂₃	

2 055 ML

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		5 ₂₃			5 ₄			5 ₁	
row2		5 ₁₄			5 ₃			5 ₂	
row3						5 ₁₂			5 ₃₄
row4	X								
row5							X		
row6				X					
row7						5 ₃₄			5 ₁₂
row8			X						
row9					5 ₁₂			5 ₃₄	

2 055 ML

	col 2	col 5	col 6	col 8	col 9
row1	5 ₂₃	5 ₄		5 ₁	
row2	5 ₁₄	5 ₃		5 ₂	
row3			5 ₁₂		5 ₃₄
row7			5 ₃₄		5 ₁₂
row9		5 ₁₂		5 ₃₄	

2 056 A1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	3 ₁	3 ₂			3 ₃				
row2		3 ₃			3 ₁₂				
row3							X		
row4	3 ₂₃	3 ₁							
row5				X					
row6								X	
row7						X			
row8									
row9			X						X

2 056 A1

	col 1	col 2	col 5
row1	3 ₁	3 ₂	3 ₃
row2		3 ₃	3 ₁₂
row4	3 ₂₃	3 ₁	

2 057 Q

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2				1 ₃₄			1 ₁		1 ₂
row3					1 ₁₂		1 ₃		1 ₄
row4	X								
row5								X	
row6				1 ₁₂	1 ₃₄				
row7						X			
row8							1 ₂₄		1 ₁₃
row9		X							

2 057 Q

	col 4	col 5	col 7	col 9
row2	1 ₃₄		1 ₁	1 ₂
row3		1 ₁₂	1 ₃	1 ₄
row6	1 ₁₂	1 ₃₄		
row8			1 ₂₄	1 ₁₃

2 058 R

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2				X					
row3	2 ₂₄	2 ₁₃							
row4	2 ₁		2 ₂		2 ₃₄				
row5							X		
row6	2 ₃		2 ₄		2 ₁₂				
row7								X	
row8						X			
row9		2 ₂₄	2 ₁₃						

2 058 R

	col 1	col 2	col 3	col 5
row3	2 ₂₄	2 ₁₃		
row4	2 ₁		2 ₂	2 ₃₄
row6	2 ₃		2 ₄	2 ₁₂
row9		2 ₂₄	2 ₁₃	

2059

G2

L

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1								X
row2				2 ₃		2 ₁₂		
row3	X							
row4					2 ₁		2 ₂₃	
row5				2 ₂		2 ₃	2 ₁	
row6			X					
row7		X						
row8				2 ₁			2 ₂₃	
row9					2 ₂₃		2 ₁	

2059

G2

L

col 4

col 5

col 6

col 7

col 8

row2	2 ₃		2 ₁₂		
row4		2 ₁			2 ₂₃
row5	2 ₂		2 ₃	2 ₁	
row8	2 ₁			2 ₂₃	
row9		2 ₂₃			2 ₁

2 060 ML

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	6 ₁₂						6 ₃₄		
row2					X				
row3		6 ₃₄							6 ₁₂
row4						X			
row5								X	
row6			X						
row7	6 ₃			6 ₂₄			6 ₁		
row8	6 ₄			6 ₁₃			6 ₂		
row9		6 ₁₂							6 ₃₄

2 060 ML

	col 1	col 2	col 4	col 7	col 9
row1	6 ₁₂			6 ₃₄	
row3		6 ₃₄			6 ₁₂
row7	6 ₃		6 ₂₄	6 ₁	
row8	6 ₄		6 ₁₃	6 ₂	
row9		6 ₁₂			6 ₃₄

2 061 W4

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						6 ₂		6 ₁₃	
row2		X							
row3					6 ₁₃			6 ₂	
row4				6 ₁	6 ₂	6 ₃			
row5	X								
row6							X		
row7									X
row8			X						
row9				6 ₂₃		6 ₁			

2 061 W4

	col 4	col 5	col 6	col 8
row1			6 ₂	6 ₁₃
row3		6 ₁₃		6 ₂
row4	6 ₁	6 ₂	6 ₃	
row9	6 ₂₃		6 ₁	

2062

G2

L

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1		6 ₃		6 ₁		6 ₂			
row2			6 ₁₂		6 ₃				
row3							X		
row4								X	
row5		6 ₁₂		6 ₃					
row6			6 ₃		6 ₁₂				
row7				6 ₂		6 ₁₃			
row8									X
row9	X								

2062

G2

L

col 2

col 3

col 4

col 5

col 6

row1	6 ₃		6 ₁		6 ₂
row2		6 ₁₂		6 ₃	
row5	6 ₁₂		6 ₃		
row6		6 ₃		6 ₁₂	
row7			6 ₂		6 ₁₃

2063

G2

L

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1		X						
row2				X				
row3						X		
row4							X	
row5			1 ₁₂		1 ₃			
row6	1 ₃					1 ₁₂		
row7	1 ₁							1 ₂₃
row8			1 ₃		1 ₁₂			
row9	1 ₂				1 ₃			1 ₁

2063

G2

L

col 1

col 3

col 5

col 6

col 9

row5		1 ₁₂	1 ₃		
row6	1 ₃			1 ₁₂	
row7	1 ₁				1 ₂₃
row8		1 ₃	1 ₁₂		
row9	1 ₂			1 ₃	1 ₁

2 064 Q

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1								X	
row2		X							
row3						X			
row4									X
row5				2 ₃₄	2 ₁₂				
row6	2 ₂₄		2 ₁₃						
row7							X		
row8	2 ₁		2 ₂		2 ₃₄				
row9	2 ₃		2 ₄	2 ₁₂					

2 064 Q

	col 1	col 3	col 4	col 5
row5			2 ₃₄	2 ₁₂
row6	2 ₂₄	2 ₁₃		
row8	2 ₁	2 ₂		2 ₃₄
row9	2 ₃	2 ₄	2 ₁₂	

2
U

065

col 1col 2col 3col 4col 5col 6col 7col 8col 9

row1		2 ₃₄		2 ₁		2 ₂			
row2							X		
row3	2 ₂	2 ₁		2 ₃	2 ₄				
row4			X						
row5				2 ₄	2 ₁₂₃				
row6							X		
row7		2 ₂				2 ₁₃₄			
row8								X	
row9	2 ₁₃₄			2 ₂					

2

U

065

col 1col 2col 4col 5col 6

row1		2 ₃₄	2 ₁		2 ₂
row3	2 ₂	2 ₁	2 ₃	2 ₄	
row5			2 ₄	2 ₁₂₃	
row7		2 ₂			2 ₁₃₄
row9	2 ₁₃₄		2 ₂		

2 066 A1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	4 ₂₃				4 ₁				
row2	4 ₁				4 ₂	4 ₃			
row3									X
row4		X							
row5							X		
row6				X					
row7					4 ₃	4 ₁₂			
row8								X	
row9			X						

2 066 A1

	col 1	col 5	col 6
row1	4 ₂₃	4 ₁	
row2	4 ₁	4 ₂	4 ₃
row7		4 ₃	4 ₁₂

2067

G2

L

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1	6 ₁	6 ₂						6 ₃
row2			6 ₃				6 ₁₂	
row3				X				
row4					X			
row5			6 ₁₂				6 ₃	
row6	6 ₃							6 ₁₂
row7						X		
row8							X	
row9	6 ₂	6 ₁₃						

2067

G2

L

col 1

col 2

col 3

col 7

col 9

row1	6 ₁	6 ₂			6 ₃
row2			6 ₃	6 ₁₂	
row5			6 ₁₂	6 ₃	
row6	6 ₃				6 ₁₂
row9	6 ₂	6 ₁₃			

2 068 A1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2	4 ₁		4 ₂		4 ₃				
row3			4 ₃		4 ₁₂				
row4						X			
row5	4 ₂₃		4 ₁						
row6								X	
row7							X		
row8		X							
row9				X					

2 068 A1

	col 1	col 3	col 5
row2	4 ₁	4 ₂	4 ₃
row3		4 ₃	4 ₁₂
row5	4 ₂₃	4 ₁	

2 069 ML

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	1 ₁		1 ₂				1 ₃₄		
row2				X					
row3		1 ₃₄						1 ₁₂	
row4	1 ₂₄		1 ₁₃						
row5									X
row6					X				
row7		1 ₁₂						1 ₃₄	
row8						X			
row9	1 ₃		1 ₄				1 ₁₂		

2 069 ML

	col 1	col 2	col 3	col 7	col 8
row1	1 ₁		1 ₂	1 ₃₄	
row3		1 ₃₄			1 ₁₂
row4	1 ₂₄		1 ₁₃		
row7		1 ₁₂			1 ₃₄
row9	1 ₃		1 ₄	1 ₁₂	

2070

A4L

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							X		
row2						X			
row3		X							
row4				4 ₂	4 ₁₃				
row5	X								
row6								X	
row7				4 ₁					4 ₂₃
row8			4 ₃		4 ₂				4 ₁
row9			4 ₁₂	4 ₃					

2070

A4L

	col 3	col 4	col 5	col 9
row4		4 ₂	4 ₁₃	
row7		4 ₁		4 ₂₃
row8	4 ₃		4 ₂	4 ₁
row9	4 ₁₂	4 ₃		

2 071 F

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					2 ₂₃		2 ₁		
row2						2 ₁	2 ₂		2 ₃
row3	X								
row4		2 ₁				2 ₂₃			
row5								X	
row6		2 ₂₃			2 ₁				
row7			X						
row8							2 ₃		2 ₁₂
row9				X					

2 071 F

	col 2	col 5	col 6	col 7	col 9
row1		2 ₂₃		2 ₁	
row2			2 ₁	2 ₂	2 ₃
row4	2 ₁		2 ₂₃		
row6	2 ₂₃	2 ₁			
row8				2 ₃	2 ₁₂

2 072 A4
L

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2				3 ₂		3 ₁₃			
row3							X		
row4		3 ₃			3 ₁	3 ₂			
row5								X	
row6		3 ₁₂		3 ₃					
row7				3 ₁	3 ₂₃				
row8									X
row9	X								

2 072 A4
L

	col 2	col 4	col 5	col 6
row2		3 ₂		3 ₁₃
row4	3 ₃		3 ₁	3 ₂
row6	3 ₁₂	3 ₃		
row7		3 ₁	3 ₂₃	

2 073 E

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				2 ₃		2 ₁₂			
row2									X
row3			X						
row4	2 ₁	2 ₂				2 ₃			
row5							X		
row6	2 ₃			2 ₁₂					
row7					X				
row8	2 ₂							2 ₁₃	
row9		2 ₁₃						2 ₂	

2 073 E

	col 1	col 2	col 4	col 6	col 8
row1			2 ₃	2 ₁₂	
row4	2 ₁	2 ₂		2 ₃	
row6	2 ₃		2 ₁₂		
row8	2 ₂				2 ₁₃
row9		2 ₁₃			2 ₂

2074

G2

L

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1			1 ₃			1 ₁	1 ₂		
row2					1 ₂				1 ₁₃
row3			1 ₁₂			1 ₃			
row4		X							
row5				X					
row6								X	
row7						1 ₂	1 ₁₃		
row8					1 ₁₃				1 ₂
row9	X								

2074

G2

L

col 3

col 5

col 6

col 7

col 9

row1	1 ₃		1 ₁	1 ₂	
row2		1 ₂			1 ₁₃
row3	1 ₁₂		1 ₃		
row7			1 ₂	1 ₁₃	
row8		1 ₁₃			1 ₂

2075

G2

L

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1					1 ₁₃			1 ₂	
row2				1 ₂					1 ₁₃
row3			X						
row4		1 ₂₃						1 ₁	
row5				1 ₁₃					1 ₂
row6		1 ₁			1 ₂			1 ₃	
row7							X		
row8	X								
row9						X			

2075

G2

L

col 2

col 4

col 5

col 8

col 9

row1			1 ₁₃	1 ₂	
row2		1 ₂			1 ₁₃
row4	1 ₂₃			1 ₁	
row5		1 ₁₃			1 ₂
row6	1 ₁		1 ₂	1 ₃	

2076

G3

L

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		X							
row2							X		
row3						X			
row4					3 ₂₃		3 ₁		
row5	3 ₁₃								3 ₂
row6			3 ₂		3 ₁		3 ₃		
row7	3 ₂								3 ₁₃
row8			3 ₁₃				3 ₂		
row9				X					

2077

G2

L

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		3 ₃						3 ₁₂	
row2					X				
row3	3 ₁₂								3 ₃
row4							X		
row5				X					
row6			X						
row7	3 ₃					3 ₂			3 ₁
row8						3 ₁₃			3 ₂
row9		3 ₁₂						3 ₃	

2 078 D

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		2 ₁				2 ₂₃			
row2							X		
row3	2 ₂₃					2 ₁			
row4									X
row5			X						
row6				X					
row7					X				
row8	2 ₁	2 ₂						2 ₃	
row9		2 ₃						2 ₁₂	

2 078 D

	col 1	col 2	col 6	col 8
row1		2 ₁	2 ₂₃	
row3	2 ₂₃		2 ₁	
row8	2 ₁	2 ₂		2 ₃
row9		2 ₃		2 ₁₂

2

079

A4
L

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2					X				
row3									X
row4		3 ₁				3 ₂₃			
row5	3 ₂					3 ₁	3 ₃		
row6		3 ₃					3 ₁₂		
row7	3 ₁₃	3 ₂							
row8							X		
row9				X					

2 080 D

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		2 ₁	2 ₂	2 ₃					
row2			2 ₃	2 ₁₂					
row3							X		
row4	X								
row5					X				
row6								X	
row7						X			
row8			2 ₁				2 ₂₃		
row9		2 ₂₃					2 ₁		

2 080 D

	col 2	col 3	col 4	col 7
row1	2 ₁	2 ₂	2 ₃	
row2		2 ₃	2 ₁₂	
row8		2 ₁		2 ₂₃
row9	2 ₂₃			2 ₁

2 081 X1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							X		
row2			X						
row3						X			
row4	2 ₁				2 ₂				2 ₃₄
row5	2 ₂₃				2 ₁₄				
row6	2 ₄				2 ₃				2 ₁₂
row7				X					
row8		X							
row9								X	

2 081 X1

	col 1	col 5	col 9
row4	2 ₁	2 ₂	2 ₃₄
row5	2 ₂₃	2 ₁₄	
row6	2 ₄	2 ₃	2 ₁₂

2 082 G2
L

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		X							
row2						X			
row3									X
row4	2 ₃				2 ₂		2 ₁		
row5				2 ₁₃				2 ₂	
row6	2 ₁₂						2 ₃		
row7				2 ₂				2 ₁₃	
row8					2 ₁₃		2 ₂		
row9			X						

2 082 G2
L

	col 1	col 4	col 5	col 7	col 8
row4	2 ₃		2 ₂	2 ₁	
row5		2 ₁₃			2 ₂
row6	2 ₁₂			2 ₃	
row7		2 ₂			2 ₁₃
row8			2 ₁₃	2 ₂	

2083

G2

L

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1		8 ₁			8 ₂₃			
row2			8 ₂				8 ₁₃	
row3		8 ₃			8 ₁		8 ₂	
row4	X							
row5						X		
row6								X
row7				X				
row8			8 ₁₃				8 ₂	
row9		8 ₂					8 ₁₃	

2083

G2

L

col 2

col 3

col 5

col 7

col 8

row1	8 ₁		8 ₂₃		
row2		8 ₂		8 ₁₃	
row3	8 ₃		8 ₁		8 ₂
row8		8 ₁₃		8 ₂	
row9	8 ₂				8 ₁₃

2 084 ML

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2				X					
row3			X						
row4		5 ₁			5 ₃₄			5 ₂	
row5	5 ₂₃						5 ₁₄		
row6		5 ₄			5 ₁₂			5 ₃	
row7						X			
row8	5 ₁₄						5 ₂₃		
row9		5 ₂₃						5 ₁₄	

2 084 ML

	col 1	col 2	col 5	col 7	col 8
row4		5 ₁	5 ₃₄		5 ₂
row5	5 ₂₃			5 ₁₄	
row6		5 ₄	5 ₁₂		5 ₃
row8	5 ₁₄			5 ₂₃	
row9		5 ₂₃			5 ₁₄

2 085 N

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	X								
row2					X				
row3							X		
row4				8 ₃				8 ₄	8 ₁₂
row5		X							
row6						8 ₁₂₄		8 ₃	
row7				8 ₂₄		8 ₃		8 ₁	
row8			X						
row9				8 ₁				8 ₂	8 ₃₄

equivalent to 3.006

2 085 N

	col 4	col 6	col 8	col 9
row4	8 ₃		8 ₄	8 ₁₂
row6		8 ₁₂₄	8 ₃	
row7	8 ₂₄	8 ₃	8 ₁	
row9	8 ₁		8 ₂	8 ₃₄

2 086 ML

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		3 ₁			3 ₃₄			3 ₂	
row2	3 ₂₃								3 ₁₄
row3		3 ₄			3 ₁₂			3 ₃	
row4							X		
row5						X			
row6			X						
row7				X					
row8	3 ₁₄								3 ₂₃
row9		3 ₂₃						3 ₁₄	

2 086 ML

	col 1	col 2	col 5	col 8	col 9
row1		3 ₁	3 ₃₄	3 ₂	
row2	3 ₂₃				3 ₁₄
row3		3 ₄	3 ₁₂	3 ₃	
row8	3 ₁₄				3 ₂₃
row9		3 ₂₃		3 ₁₄	

2 087 N

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2						3 ₂₃			3 ₁
row3					3 ₁			3 ₂	3 ₃
row4					3 ₃			3 ₁	3 ₂
row5		X							
row6					3 ₂	3 ₁		3 ₃	
row7				X					
row8	X								
row9							X		

2 087 N

	col 5	col 6	col 8	col 9
row2		3 ₂₃		3 ₁
row3	3 ₁		3 ₂	3 ₃
row4	3 ₃		3 ₁	3 ₂
row6	3 ₂	3 ₁	3 ₃	

2088

G2

L

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1		5 ₃				5 ₂	5 ₁		
row2						5 ₁₃	5 ₂		
row3	5 ₁₂								5 ₃
row4							X		
row5					X				
row6			X						
row7				X					
row8	5 ₃								5 ₁₂
row9		5 ₁₂					5 ₃		

2088

G2

L

col 1

col 2

col 6

col 7

col 9

row1		5 ₃	5 ₂	5 ₁	
row2			5 ₁₃	5 ₂	
row3	5 ₁₂				5 ₃
row8	5 ₃				5 ₁₂
row9		5 ₁₂		5 ₃	

2 089 D

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				8 ₁				8 ₂₃	
row2			X						
row3				8 ₂		8 ₃	8 ₁		
row4				8 ₃		8 ₁₂			
row5									X
row6		X							
row7							8 ₂₃	8 ₁	
row8	X								
row9					X				

2 089 D

	col 4	col 6	col 7	col 8
row1	8 ₁			8 ₂₃
row3	8 ₂	8 ₃	8 ₁	
row4	8 ₃	8 ₁₂		
row7			8 ₂₃	8 ₁

2 090 W5

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						2 ₂₃			2 ₁
row2	2 ₁₂								2 ₃
row3	2 ₃				2 ₁				2 ₂
row4		X							
row5								X	
row6				X					
row7			2 ₁		2 ₂₃				
row8							X		
row9			2 ₂₃			2 ₁			

2 090 W5

	col 1	col 3	col 5	col 6	col 9
row1				2 ₂₃	2 ₁
row2	2 ₁₂				2 ₃
row3	2 ₃		2 ₁		2 ₂
row7		2 ₁	2 ₂₃		
row9		2 ₂₃		2 ₁	

2 091 A1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	X								
row2						2 ₁	2 ₂		2 ₃
row3						2 ₂₃			2 ₁
row4							2 ₁₃		2 ₂
row5		X							
row6					X				
row7			X						
row8				X					
row9								X	

2 091 A1

	col 6	col 7	col 9
row2	2 ₁	2 ₂	2 ₃
row3	2 ₂₃		2 ₁
row4		2 ₁₃	2 ₂

2 092 A1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2					X				
row3							X		
row4								X	
row5				6 ₂		6 ₁₃			
row6	X								
row7				6 ₁		6 ₂			6 ₃
row8		X							
row9				6 ₃					6 ₁₂

2 092 A1

	col 4	col 6	col 9
row5	6 ₂	6 ₁₃	
row7	6 ₁	6 ₂	6 ₃
row9	6 ₃		6 ₁₂

2 093 A1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2				X					
row3							X		
row4					8 ₁	8 ₂₃			
row5								X	
row6		X							
row7									X
row8	8 ₃				8 ₂	8 ₁			
row9	8 ₁₂				8 ₃				

2 093 A1

	col 1	col 5	col 6
row4		8 ₁	8 ₂₃
row8	8 ₃	8 ₂	8 ₁
row9	8 ₁₂	8 ₃	

2 094 A1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					X				
row2	X								
row3							X		
row4								X	
row5		5 ₁		5 ₂		5 ₃			
row6		5 ₂₃		5 ₁					
row7									X
row8			X						
row9				5 ₃		5 ₁₂			

2 094 A1

	col 2	col 4	col 6
row5	5 ₁	5 ₂	5 ₃
row6	5 ₂₃	5 ₁	
row9		5 ₃	5 ₁₂

2095

A4

L

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1	X							
row2				7 ₁		7 ₂	7 ₃	
row3					7 ₃		7 ₁₂	
row4			X					
row5								X
row6					7 ₁₂	7 ₃		
row7		X						
row8							X	
row9				7 ₂₃		7 ₁		

2095

A4

L

col 4

col 5

col 6

col 7

row2	7 ₁		7 ₂	7 ₃
row3		7 ₃		7 ₁₂
row6		7 ₁₂	7 ₃	
row9	7 ₂₃		7 ₁	

2 096 A1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					2 ₂₃				2 ₁
row2					2 ₁			2 ₂	2 ₃
row3			X						
row4							X		
row5						X			
row6	X								
row7				X					
row8								2 ₁₃	2 ₂
row9		X							

2 096 A1

	col 5	col 8	col 9
row1	2 ₂₃		2 ₁
row2	2 ₁	2 ₂	2 ₃
row8		2 ₁₃	2 ₂

2097

A5
L

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2					X				
row3		X							
row4			2 ₁	2 ₂			2 ₃		
row5				2 ₁₃				2 ₂	
row6			2 ₂₃				2 ₁		
row7						2 ₁₃	2 ₂		
row8	X								
row9						2 ₂		2 ₁₃	

2097

A5
L

	col 3	col 4	col 6	col 7	col 8
row4	2 ₁	2 ₂		2 ₃	
row5		2 ₁₃			2 ₂
row6	2 ₂₃			2 ₁	
row7			2 ₁₃	2 ₂	
row9			2 ₂		2 ₁₃

2 098 G1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		X							
row2				X					
row3							X		
row4			1 ₁			1 ₂₃			
row5								X	
row6	1 ₂₃					1 ₁			
row7	1 ₁		1 ₂		1 ₃				
row8			1 ₃		1 ₁₂				
row9									X

2 098 G1

	col 1	col 3	col 5	col 6
row4		1 ₁		1 ₂₃
row6	1 ₂₃			1 ₁
row7	1 ₁	1 ₂	1 ₃	
row8		1 ₃	1 ₁₂	

2 099 D

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		X							
row2								X	
row3					X				
row4			1 ₁			1 ₂₃			
row5			1 ₂₃	1 ₁					
row6							X		
row7	X								
row8				1 ₂		1 ₁			1 ₃
row9				1 ₃					1 ₁₂

2 099 D

	col 3	col 4	col 6	col 9
row4	1 ₁		1 ₂₃	
row5	1 ₂₃	1 ₁		
row8		1 ₂	1 ₁	1 ₃
row9		1 ₃		1 ₁₂

2 100 W1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						X			
row2								X	
row3	X								
row4		X							
row5							X		
row6					X				
row7			3 ₂₃						3 ₁
row8				3 ₁₃					3 ₂
row9			3 ₁	3 ₂					3 ₃

2 100 W1

	col 3	col 4	col 9
row7	3 ₂₃		3 ₁
row8		3 ₁₃	3 ₂
row9	3 ₁	3 ₂	3 ₃

2 101 P

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									
row2			X						
row3					X				
row4							2 ₁₂		2 ₃₄
row5	X								
row6						X			
row7		X							
row8				2 ₂₄			2 ₃		2 ₁
row9				2 ₁₃			2 ₄		2 ₂

2 101 P

	col 4	col 7	col 9
row4		2 ₁₂	2 ₃₄
row8	2 ₂₄	2 ₃	2 ₁
row9	2 ₁₃	2 ₄	2 ₂

2 102 A3

	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						X		
row2				7 ₁₃	7 ₂			
row3			X					
row4	X							
row5				7 ₂₃	7 ₁			
row6								X
row7		X						
row8							X	
row9				7 ₁	7 ₂	7 ₃		

2 102 A3

	col 4	col 5	col 6
row2		7 ₁₃	7 ₂
row5	7 ₂₃		7 ₁
row9	7 ₁	7 ₂	7 ₃

2 103 D

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					2 ₁₃				2 ₂
row2					2 ₂		2 ₁₃		
row3	X								
row4				X					
row5		2 ₂₃							2 ₁
row6		2 ₁					2 ₂		2 ₃
row7			X						
row8								X	
row9						X			

2 103 D

	col 2	col 5	col 7	col 9
row1		2 ₁₃		2 ₂
row2		2 ₂	2 ₁₃	
row5	2 ₂₃			2 ₁
row6	2 ₁		2 ₂	2 ₃

2104

A6X

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			9 ₁₂						9 ₃
row2		9 ₃							9 ₁₂
row3						X			
row4				X					
row5	9 ₂	9 ₁	9 ₃						
row6								X	
row7					X				
row8	9 ₁₃	9 ₂							
row9							X		

2104

A6X

	col 1	col 2	col 3	col 9
row1			9 ₁₂	9 ₃
row2		9 ₃		9 ₁₂
row5	9 ₂	9 ₁	9 ₃	
row8	9 ₁₃	9 ₂		

2 105 A1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2					2 ₃			2 ₁	2 ₂
row3					2 ₁₂			2 ₃	
row4							X		
row5						X			
row6	X								
row7				X					
row8								2 ₂	2 ₁₃
row9		X							

2 105 A1

	col 5	col 8	col 9
row2	2 ₃	2 ₁	2 ₂
row3	2 ₁₂	2 ₃	
row8		2 ₂	2 ₁₃

2 106 D

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			9 ₁₂			9 ₃			
row2			9 ₃		9 ₁₂				
row3									X
row4	X								
row5				X					
row6							X		
row7						9 ₁		9 ₂₃	
row8		X							
row9					9 ₃	9 ₂		9 ₁	

2 106 D

	col 3	col 5	col 6	col 8
row1	9 ₁₂		9 ₃	
row2	9 ₃	9 ₁₂		
row7			9 ₁	9 ₂₃
row9		9 ₃	9 ₂	9 ₁

2107A4

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						X			
row2			X						
row3									X
row4		9 ₁			9 ₂			9 ₃	
row5					9 ₁₃		9 ₂		
row6		9 ₂₃						9 ₁	
row7							9 ₁₃	9 ₂	
row8	X								
row9				X					

2107A4

	col 2	col 5	col 7	col 8
row4	9 ₁	9 ₂		9 ₃
row5		9 ₁₃	9 ₂	
row6	9 ₂₃			9 ₁
row7			9 ₁₃	9 ₂

2108

G2

L

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1	X							
row2				6 ₁₃				6 ₂
row3					6 ₂		6 ₁₃	
row4			6 ₁	6 ₂				6 ₃
row5			6 ₂₃					6 ₁
row6					6 ₁₃		6 ₂	
row7						X		
row8		X						
row9							X	

2108

G2

L

col 3

col 4

col 5

col 8

col 9

row2		6 ₁₃			6 ₂
row3			6 ₂	6 ₁₃	
row4	6 ₁	6 ₂			6 ₃
row5	6 ₂₃				6 ₁
row6			6 ₁₃	6 ₂	

2 109 L2

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		X							
row2						9 ₁₂			9 ₃
row3					9 ₃			9 ₁	9 ₂
row4	X								
row5					9 ₁₂			9 ₃	
row6						9 ₃		9 ₂	9 ₁
row7			X						
row8							X		
row9				X					

2 109 L2

	col 5	col 6	col 8	col 9
row2		9 ₁₂		9 ₃
row3	9 ₃		9 ₁	9 ₂
row5	9 ₁₂		9 ₃	
row6		9 ₃	9 ₂	9 ₁

2 110 A4s

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							X		
row2	X								
row3						X			
row4									X
row5			X						
row6				4 ₂₃	4 ₁				
row7					4 ₂			4 ₁₃	
row8		4 ₂		4 ₁	4 ₃				
row9		4 ₁₃						4 ₂	

2 110 A4s

	col 2	col 4	col 5	col 8
row6		4 ₂₃	4 ₁	
row7			4 ₂	4 ₁₃
row8	4 ₂	4 ₁	4 ₃	
row9	4 ₁₃			4 ₂

2 111 A5

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						X			
row2							X		
row3			X						
row4		7 ₃							7 ₁₂
row5		7 ₁₂						7 ₃	
row6				X					
row7					7 ₁			7 ₂	7 ₃
row8	7 ₁				7 ₂₃				
row9	7 ₂₃							7 ₁	

2 111 E

	col 1	col 2	col 5	col 8	col 9
row4		7 ₃			7 ₁₂
row5		7 ₁₂		7 ₃	
row7			7 ₁	7 ₂	7 ₃
row8	7 ₁		7 ₂₃		
row9	7 ₂₃			7 ₁	

2 112 Q

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	X								
row2							X		
row3				X					
row4		9 ₁	9 ₂					9 ₃₄	
row5						X			
row6		9 ₃	9 ₄					9 ₁₂	
row7									X
row8		9 ₂₄			9 ₁₃				
row9			9 ₁₃		9 ₂₄				

2 112 Q

	col 2	col 3	col 5	col 8
row4	9 ₁	9 ₂		9 ₃₄
row6	9 ₃	9 ₄		9 ₁₂
row8	9 ₂₄		9 ₁₃	
row9		9 ₁₃	9 ₂₄	

2 113 D

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2	2 ₁	2 ₂₃							
row3					X				
row4	2 ₂	2 ₁		2 ₃					
row5				2 ₁₂			2 ₃		
row6	2 ₃						2 ₁₂		
row7								X	
row8						X			
row9									

2 113 D

	col 1	col 2	col 4	col 7
row2	2 ₁	2 ₂₃		
row4	2 ₂	2 ₁	2 ₃	
row5			2 ₁₂	2 ₃
row6	2 ₃			2 ₁₂

2 114 D

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		X							
row2							1 ₁₃		1 ₂
row3					X				
row4				1 ₂₃				1 ₁	
row5			X						
row6				1 ₁			1 ₂	1 ₃	
row7	X								
row8								1 ₂	1 ₁₃
row9						X			

2 114 D

	col 4	col 7	col 8	col 9
row2		1 ₁₃		1 ₂
row4	1 ₂₃		1 ₁	
row6	1 ₁	1 ₂	1 ₃	
row8			1 ₂	1 ₁₃

2 115 D

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		1 ₁	1 ₂		1 ₃				
row2			1 ₃		1 ₁₂				
row3							X		
row4				X					
row5			1 ₁						1 ₂₃
row6		1 ₂₃							1 ₁
row7						X			
row8	X								
row9								X	

2 115 D

	col 2	col 3	col 5	col 9
row1	1 ₁	1 ₂	1 ₃	
row2		1 ₃	1 ₁₂	
row5		1 ₁		1 ₂₃
row6	1 ₂₃			1 ₁

2 116 W2

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				2 ₁₂		2 ₃			
row2	X								
row3								X	
row4				2 ₃	2 ₁	2 ₂			
row5		X							
row6							X		
row7					2 ₂₃				2 ₁
row8						2 ₁			2 ₂₃
row9			X						

2 116 W2

	col 4	col 5	col 6	col 9
row1	2 ₁₂		2 ₃	
row4	2 ₃	2 ₁	2 ₂	
row7		2 ₂₃		2 ₁
row8			2 ₁	2 ₂₃

2 117 G2

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							X		
row2	X								
row3						X			
row4					1 ₁₂			1 ₃	
row5				1 ₃					1 ₁₂
row6			X						
row7		1 ₂₃		1 ₁					
row8								1 ₁₂	1 ₃
row9		1 ₁		1 ₂	1 ₃				

2 117 G2

	col 2	col 4	col 5	col 8	col 9
row4			1 ₁₂	1 ₃	
row5		1 ₃			1 ₁₂
row7	1 ₂₃	1 ₁			
row8				1 ₁₂	1 ₃
row9	1 ₁	1 ₂	1 ₃		

2 118 D

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				X					
row2								X	
row3			X						
row4					4 ₁₂	4 ₃			
row5							4 ₂		4 ₁₃
row6		X							
row7					4 ₃	4 ₁			4 ₂
row8						4 ₂	4 ₁₃		
row9	X								

2 118 D

	col 5	col 6	col 7	col 9
row4	4 ₁₂	4 ₃		
row5			4 ₂	4 ₁₃
row7	4 ₃	4 ₁		4 ₂
row8		4 ₂	4 ₁₃	

2 119 E

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	9 ₁			9 ₂₃					
row2			9 ₂₃	9 ₁					
row3								X	
row4						X			
row5									X
row6		X							
row7					9 ₃		9 ₁₂		
row8	9 ₂		9 ₁				9 ₃		
row9	9 ₃				9 ₁₂				

2 119 E

	col 1	col 3	col 4	col 5	col 7
row1	9 ₁		9 ₂₃		
row2		9 ₂₃	9 ₁		
row7				9 ₃	9 ₁₂
row8	9 ₂	9 ₁			9 ₃
row9	9 ₃			9 ₁₂	

2120A4S

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					X				
row2	5 ₁	5 ₂₃							
row3							X		
row4	5 ₂₃		5 ₁						
row5				X					
row6								X	
row7		5 ₁	5 ₂						5 ₃
row8			5 ₃						5 ₁₂
row9						X			

2120A4S

	col 1	col 2	col 3	col 9
row2	5 ₁	5 ₂₃		
row4	5 ₂₃		5 ₁	
row7		5 ₁	5 ₂	5 ₃
row8			5 ₃	5 ₁₂

2 121 W2

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									
row2				9 ₁	9 ₂	9 ₃			
row3									
row4						9 ₁₂	9 ₃		
row5									
row6				9 ₃			9 ₁₂		
row7									
row8									
row9				9 ₂	9 ₁₃				

2 121 W2

	col 4	col 5	col 6	col 7
row2	9 ₁	9 ₂	9 ₃	
row4			9 ₁₂	9 ₃
row6	9 ₃			9 ₁₂
row9	9 ₂	9 ₁₃		

2 122 D

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		1 ₁₂			1 ₃				
row2		1 ₃		1 ₁	1 ₂				
row3									
row4	1 ₁			1 ₂₃					
row5	1 ₂₃				1 ₁				
row6									
row7									
row8									
row9									

2 122 D

	col 1	col 2	col 4	col 5
row1		1 ₁₂		1 ₃
row2		1 ₃	1 ₁	1 ₂
row4	1 ₁		1 ₂₃	
row5	1 ₂₃			1 ₁

2123A4L

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2					2 ₁	2 ₂₃			
row3									X
row4	X								
row5				2 ₁₂	2 ₃				
row6							X		
row7				2 ₃		2 ₁		2 ₂	
row8					2 ₂			2 ₁₃	
row9		X							

2123A4L

	col 4	col 5	col 6	col 8
row2		2 ₁	2 ₂₃	
row5	2 ₁₂	2 ₃		
row7	2 ₃		2 ₁	2 ₂
row8		2 ₂		2 ₁₃

2 124 D

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1								X	
row2			4 ₂₃		4 ₁				
row3	4 ₁				4 ₂₃				
row4	4 ₂		4 ₁			4 ₃			
row5	4 ₃					4 ₁₂			
row6									X
row7				X					
row8							X		
row9		X							

2 124 D

	col 1	col 3	col 5	col 6
row2		4 ₂₃	4 ₁	
row3	4 ₁		4 ₂₃	
row4	4 ₂	4 ₁		4 ₃
row5	4 ₃			4 ₁₂

2 125 R

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	X								
row2						9 ₁₂			9 ₃₄
row3						9 ₃₄	9 ₁₂		
row4					9 ₂₄		9 ₃		9 ₁
row5			X						
row6					9 ₁₃		9 ₄		9 ₂
row7				X					
row8								X	
row9		X							

2 125 R

	col 5	col 6	col 7	col 9
row2		9 ₁₂		9 ₃₄
row3		9 ₃₄	9 ₁₂	
row4	9 ₂₄		9 ₃	9 ₁
row6	9 ₁₃		9 ₄	9 ₂

2 126 A1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	X								
row2							X		
row3					X				
row4									X
row5				1 ₁₂		1 ₃₄			
row6			X						
row7								X	
row8		1 ₂₄		1 ₃		1 ₁			
row9		1 ₁₃		1 ₄		1 ₂			

2 126 A1

	col 2	col 4	col 6
row5		1 ₁₂	1 ₃₄
row8	1 ₂₄	1 ₃	1 ₁
row9	1 ₁₃	1 ₄	1 ₂

2 127 D

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		X							
row2							1 ₁₃		1 ₂
row3					X				
row4				1 ₂₃				1 ₁	
row5			X						
row6				1 ₁			1 ₂	1 ₃	
row7	X								
row8								1 ₂	1 ₁₃
row9						X			

2 127 D

	col 4	col 7	col 8	col 9
row2		1 ₁₃		1 ₂
row4	1 ₂₃		1 ₁	
row6	1 ₁	1 ₂	1 ₃	
row8			1 ₂	1 ₁₃

2 128 Y1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				5 ₁₂	5 ₃₄	5 ₅₆			
row2		X							
row3									X
row4	X								
row5								X	
row6				5 ₃₅	5 ₁₆	5 ₂₄			
row7							X		
row8			X						
row9				5 ₄₆	5 ₂₅	5 ₁₃			

2 128 Y1

	col 4	col 5	col 6
row1	5 ₁₂	5 ₃₄	5 ₅₆
row6	5 ₃₅	5 ₁₆	5 ₂₄
row9	5 ₄₆	5 ₂₅	5 ₁₃

2 129 W3

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						8 ₂			8 ₁₃
row2			8 ₂			8 ₁₃			
row3		8 ₁₃							8 ₂
row4					X				
row5	8 ₂₃		8 ₁						
row6							X		
row7				X					
row8	8 ₁	8 ₂	8 ₃						
row9								X	

2 129 W3

	col 1	col 2	col 3	col 6	col 9
row1				8 ₂	8 ₁₃
row2			8 ₂	8 ₁₃	
row3		8 ₁₃			8 ₂
row5	8 ₂₃		8 ₁		
row8	8 ₁	8 ₂	8 ₃		

2 130 P

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						X			
row2							X		
row3			X						
row4								X	
row5				8 ₂₄	8 ₁₃				
row6	X								
row7									X
row8		8 ₃₄		8 ₁	8 ₂				
row9		8 ₁₂		8 ₃	8 ₄				

2 130 P

	col 2	col 4	col 5
row5		8 ₂₄	8 ₁₃
row8	8 ₃₄	8 ₁	8 ₂
row9	8 ₁₂	8 ₃	8 ₄

2 131 X3

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		1 ₁				1 ₂₃	1 ₄		
row2		1 ₂				1 ₁₄	1 ₃		
row3			1 ₃₄				1 ₁₂		
row4		1 ₃₄	1 ₁₂						
row5				X					
row6									X
row7					X				
row8								X	
row9	X								

2 131 X3

	col 2	col 3	col 6	col 7
row1	1 ₁		1 ₂₃	1 ₄
row2	1 ₂		1 ₁₄	1 ₃
row3		1 ₃₄		1 ₁₂
row4	1 ₃₄	1 ₁₂		

2 132 P

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		7 ₁₂	7 ₃₄						
row2					X				
row3									X
row4	X								
row5								X	
row6						X			
row7		7 ₃	7 ₁				7 ₂₄		
row8		7 ₄	7 ₂				7 ₁₃		
row9				X					

2 132 P

	col 2	col 3	col 7
row1	7 ₁₂	7 ₃₄	
row7	7 ₃	7 ₁	7 ₂₄
row8	7 ₄	7 ₂	7 ₁₃

2 133 Q1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		1 ₁₂	1 ₃₄						
row2						X			
row3								1 ₁₃	1 ₂₄
row4		1 ₃	1 ₁					1 ₂₄	
row5					X				
row6		1 ₄	1 ₂						1 ₁₃
row7				X					
row8	X								
row9							X		

2 133 Q1

	col 2	col 3	col 8	col 9
row1	1 ₁₂	1 ₃₄		
row3			1 ₁₃	1 ₂₄
row4	1 ₃	1 ₁	1 ₂₄	
row6	1 ₄	1 ₂		1 ₁₃

2 134 S

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					X				
row2								5 ₂₄	5 ₁₃
row3		X							
row4	5 ₃₄			5 ₁		5 ₂			
row5	5 ₁₂			5 ₃		5 ₄			
row6							X		
row7			X						
row8						5 ₁₃			5 ₂₄
row9				5 ₂₄				5 ₁₃	

2 134 S

	col 1	col 4	col 6	col 8	col 9
row2				5 ₂₄	5 ₁₃
row4	5 ₃₄	5 ₁	5 ₂		
row5	5 ₁₂	5 ₃	5 ₄		
row8			5 ₁₃		5 ₂₄
row9		5 ₂₄		5 ₁₃	

2 135 Q

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	8 ₁₂								8 ₃₄
row2	8 ₃₄						8 ₁₂		
row3				X					
row4					X				
row5		X							
row6								X	
row7			8 ₂₄				8 ₃		8 ₁
row8			8 ₁₃				8 ₄		8 ₂
row9						X			

2 135 Q

	col 1	col 3	col 7	col 9
row1	8 ₁₂			8 ₃₄
row2	8 ₃₄		8 ₁₂	
row7		8 ₂₄	8 ₃	8 ₁
row8		8 ₁₃	8 ₄	8 ₂

2 136 O

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	1 ₁₂		1 ₃					1 ₄	
row2				X					
row3			1 ₄				1 ₁	1 ₂₃	
row4		X							
row5					X				
row6									X
row7			1 ₁₂				1 ₃₄		
row8	1 ₃₄					1 ₁₂			
row9						1 ₃₄	1 ₂	1 ₁	

2 136 O

	col 1	col 3	col 6	col 7	col 8
row1	1 ₁₂	1 ₃			1 ₄
row3		1 ₄		1 ₁	1 ₂₃
row7		1 ₁₂		1 ₃₄	
row8	1 ₃₄		1 ₁₂		
row9			1 ₃₄	1 ₂	1 ₁

2 137 Q

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	5 ₁₂								5 ₃₄
row2					X				
row3	5 ₃₄							5 ₁₂	
row4							X		
row5				X					
row6			X						
row7		5 ₂₄						5 ₃	5 ₁
row8		5 ₁₃						5 ₄	5 ₂
row9						X			

2 137 Q

	col 1	col 2	col 8	col 9
row1	5 ₁₂			5 ₃₄
row3	5 ₃₄		5 ₁₂	
row7		5 ₂₄	5 ₃	5 ₁
row8		5 ₁₃	5 ₄	5 ₂

2 138 L3

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					7 ₁₂	7 ₃₄			
row2	X								
row3							X		
row4			7 ₂₃			7 ₁		7 ₄	
row5					7 ₃₄			7 ₁₂	
row6			7 ₁₄			7 ₂		7 ₃	
row7		X							
row8				X					
row9									X

2 138 L3

	col 3	col 5	col 6	col 8
row1		7 ₁₂	7 ₃₄	
row4	7 ₂₃		7 ₁	7 ₄
row5		7 ₃₄		7 ₁₂
row6	7 ₁₄		7 ₂	7 ₃

2 139 ML

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		3 ₁			3 ₃₄			3 ₂	
row2	3 ₂₃								3 ₁₄
row3		3 ₄			3 ₁₂			3 ₃	
row4				X					
row5							X		
row6			X						
row7		3 ₂₃						3 ₁₄	
row8						X			
row9	3 ₁₄								3 ₂₃

2 139 ML

	col 1	col 2	col 5	col 8	col 9
row1		3 ₁	3 ₃₄	3 ₂	
row2	3 ₂₃				3 ₁₄
row3		3 ₄	3 ₁₂	3 ₃	
row7		3 ₂₃		3 ₁₄	
row9	3 ₁₄				3 ₂₃

2 140 X4

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	2 ₁₂						2 ₃₄		
row2	2 ₃				2 ₂₄			2 ₁	
row3	2 ₄				2 ₁₃			2 ₂	
row4							2 ₁₂		2 ₃₄
row5						X			
row6			X						
row7		X							
row8								2 ₃₄	2 ₁₂
row9				X					

2 140 X4

	col 1	col 5	col 7	col 8	col 9
row1	2 ₁₂		2 ₃₄		
row2	2 ₃	2 ₂₄		2 ₁	
row3	2 ₄	2 ₁₃		2 ₂	
row4			2 ₁₂		2 ₃₄
row8				2 ₃₄	2 ₁₂

2 141 Q

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2					X				
row3		X							
row4							7 ₂₄	7 ₁₃	
row5				X					
row6	7 ₁₂		7 ₃₄						
row7			7 ₁₂				7 ₃	7 ₄	
row8	7 ₃₄						7 ₁	7 ₂	
row9						X			

2 141 Q

	col 1	col 3	col 7	col 8
row4			7 ₂₄	7 ₁₃
row6	7 ₁₂	7 ₃₄		
row7		7 ₁₂	7 ₃	7 ₄
row8	7 ₃₄		7 ₁	7 ₂

2 142 X1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						X			
row2								X	
row3		X							
row4			5 ₁		5 ₃		5 ₂₄		
row5			5 ₂		5 ₄		5 ₁₃		
row6			5 ₃₄		5 ₁₂				
row7	X								
row8									X
row9				X					

2 142 X1

	col 3	col 5	col 7
row4	5 ₁	5 ₃	5 ₂₄
row5	5 ₂	5 ₄	5 ₁₃
row6	5 ₃₄	5 ₁₂	

2 143 G6

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					X				
row2	5 ₃						5 ₁₂		
row3	5 ₁₂								5 ₃
row4				5 ₃					5 ₁₂
row5		5 ₁	5 ₂				5 ₃		
row6		5 ₃				5 ₁₂			
row7				5 ₁₂		5 ₃			
row8		5 ₂	5 ₁₃						
row9								X	

2 143 G6

	col 1	col 2	col 3	col 4	col 6	col 7	col 9
row2	5 ₃					5 ₁₂	
row3	5 ₁₂						5 ₃
row4				5 ₃			5 ₁₂
row5		5 ₁	5 ₂			5 ₃	
row6		5 ₃			5 ₁₂		
row7				5 ₁₂	5 ₃		
row8		5 ₂	5 ₁₃				

2 144 ML

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		3 ₃₄		3 ₁₂					
row2							X		
row3			3 ₁₂			3 ₃₄			
row4			3 ₃			3 ₁			3 ₂₄
row5			3 ₄			3 ₂			3 ₁₃
row6		3 ₁₂		3 ₃₄					
row7								X	
row8					X				
row9	X								

2 144 ML

	col 2	col 3	col 4	col 6	col 9
row1	3 ₃₄		3 ₁₂		
row3		3 ₁₂		3 ₃₄	
row4		3 ₃		3 ₁	3 ₂₄
row5		3 ₄		3 ₂	3 ₁₃
row6	3 ₁₂		3 ₃₄		

2 145 A1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			1 ₂₃				1 ₁		
row2				X					
row3			1 ₁				1 ₂		1 ₃
row4								X	
row5						X			
row6		X							
row7							1 ₃		1 ₁₂
row8					X				
row9	X								

2 145 A1

	col 3	col 7	col 9
row1	1 ₂₃	1 ₁	
row3	1 ₁	1 ₂	1 ₃
row7		1 ₃	1 ₁₂

2 146 A5

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					2 ₃	2 ₁₂			
row2							2 ₂		2 ₁₃
row3		X							
row4				2 ₃	2 ₁₂				
row5								X	
row6	X								
row7			X						
row8				2 ₁		2 ₃			2 ₂
row9				2 ₂			2 ₁₃		

2 146 E

	col 4	col 5	col 6	col 7	col 9
row1		2 ₃	2 ₁₂		
row2				2 ₂	2 ₁₃
row4	2 ₃	2 ₁₂			
row8	2 ₁		2 ₃		2 ₂
row9	2 ₂			2 ₁₃	

2 147 ML

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			2 ₃₄				2 ₁		2 ₂
row2				X					
row3		2 ₁₂						2 ₃₄	
row4							2 ₂₄		2 ₁₃
row5	X								
row6					X				
row7		2 ₃₄						2 ₁₂	
row8						X			
row9			2 ₁₂				2 ₃		2 ₄

2 147 ML

	col 2	col 3	col 7	col 8	col 9
row1		2 ₃₄	2 ₁		2 ₂
row3	2 ₁₂			2 ₃₄	
row4			2 ₂₄		2 ₁₃
row7	2 ₃₄			2 ₁₂	
row9		2 ₁₂	2 ₃		2 ₄

2 148 T

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				X					
row2	9 ₁		9 ₂						9 ₃₄
row3		9 ₃	9 ₄						9 ₁₂
row4		9 ₂₄	9 ₁₃						
row5								X	
row6						X			
row7	9 ₂₃₄	9 ₁							
row8					X				
row9							X		

2 148 T

	col 1	col 2	col 3	col 9
row2	9 ₁		9 ₂	9 ₃₄
row3		9 ₃	9 ₄	9 ₁₂
row4		9 ₂₄	9 ₁₃	
row7	9 ₂₃₄	9 ₁		

2 149 T

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2						X			
row3								1 ₂₃	1 ₁₄
row4							1 ₁₂₄		1 ₃
row5	X								
row6				X					
row7					1 ₃₄			1 ₁	1 ₂
row8					1 ₁₂		1 ₃	1 ₄	
row9		X							

2 149 T

	col 5	col 7	col 8	col 9
row3			1 ₂₃	1 ₁₄
row4		1 ₁₂₄		1 ₃
row7	1 ₃₄		1 ₁	1 ₂
row8	1 ₁₂	1 ₃	1 ₄	

2150

G2

L

col 1col 2col 3col 4col 5col 6col 7col 8col 9

row1			X						
row2					X				
row3							X		
row4				4 ₂₃				4 ₁	
row5	4 ₁₃								4 ₂
row6		4 ₂		4 ₁				4 ₃	
row7		4 ₁₃						4 ₂	
row8	4 ₂								4 ₁₃
row9						X			

2150

G2

L

col 1col 2col 4col 8col 9

row4			4 ₂₃	4 ₁	
row5	4 ₁₃				4 ₂
row6		4 ₂	4 ₁	4 ₃	
row7		4 ₁₃		4 ₂	
row8	4 ₂				4 ₁₃

2 151 G3

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			8 ₂				8 ₁₃		
row2						X			
row3	8 ₁₃								8 ₂
row4	8 ₂		8 ₁₃						
row5				X					
row6								X	
row7		8 ₂₃							8 ₁
row8		8 ₁					8 ₂		8 ₃
row9					X				

2 151 G3

	col 1	col 2	col 3	col 7	col 9
row1			8 ₂	8 ₁₃	
row3	8 ₁₃				8 ₂
row4	8 ₂		8 ₁₃		
row7		8 ₂₃			8 ₁
row8		8 ₁		8 ₂	8 ₃

2 152 D

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					1 ₁	1 ₂		1 ₃	
row2		X							
row3						1 ₃			1 ₁₂
row4				X					
row5			X						
row6								1 ₁₂	1 ₃
row7							X		
row8					1 ₂₃	1 ₁			
row9	X								

2 152 D

	col 5	col 6	col 8	col 9
row1	1 ₁	1 ₂	1 ₃	
row3		1 ₃		1 ₁₂
row6			1 ₁₂	1 ₃
row8	1 ₂₃	1 ₁		

2 153 M

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				X					
row2							X		
row3	X								
row4		1 ₁			1 ₂			1 ₃₄	
row5			1 ₂₃			1 ₁₄			
row6		1 ₄			1 ₃			1 ₁₂	
row7									X
row8			1 ₁₄			1 ₂₃			
row9		1 ₂₃			1 ₁₄				

2 153 M

	col 2	col 3	col 5	col 6	col 8
row4	1 ₁		1 ₂		1 ₃₄
row5		1 ₂₃		1 ₁₄	
row6	1 ₄		1 ₃		1 ₁₂
row8		1 ₁₄		1 ₂₃	
row9	1 ₂₃		1 ₁₄		

2 154 D

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		1 ₃				1 ₁₂			
row2			1 ₁₂			1 ₃			
row3							X		
row4	X								
row5									X
row6				X					
row7		1 ₁						1 ₂₃	
row8					X				
row9		1 ₂	1 ₃					1 ₁	

2 154 D

	col 2	col 3	col 6	col 8
row1	1 ₃		1 ₁₂	
row2		1 ₁₂	1 ₃	
row7	1 ₁			1 ₂₃
row9	1 ₂	1 ₃		1 ₁

2 155 L3

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				4 ₃	4 ₁₂	4 ₄			
row2								X	
row3			X						
row4	4 ₃₄			4 ₁		4 ₂			
row5	4 ₁₂				4 ₃₄				
row6							X		
row7									X
row8		X							
row9				4 ₂₄		4 ₁₃			

2 155 L3

	col 1	col 4	col 5	col 6
row1		4 ₃	4 ₁₂	4 ₄
row4	4 ₃₄	4 ₁		4 ₂
row5	4 ₁₂		4 ₃₄	
row9		4 ₂₄		4 ₁₃

2156

G7

L

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1		1 ₂₃			1 ₁			
row2			1 ₁	1 ₂		1 ₃		
row3						X		
row4		1 ₁					1 ₂₃	
row5			1 ₂₃			1 ₁		
row6					1 ₂₃		1 ₁	
row7								X
row8				1 ₁₃		1 ₂		
row9	X							

2156

G7

L

col 2

col 3

col 4

col 5

col 6

col 8

row1	1 ₂₃			1 ₁		
row2		1 ₁	1 ₂		1 ₃	
row4	1 ₁					1 ₂₃
row5		1 ₂₃			1 ₁	
row6				1 ₂₃		1 ₁
row8			1 ₁₃		1 ₂	

2 157 C9

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2	3 ₁				3 ₃₄				
row3		3 ₃₄		3 ₁₂					
row4						X			
row5								X	
row6	3 ₂₃		3 ₁₄						
row7							X		
row8	3 ₄		3 ₃		3 ₁₂				
row9		3 ₁₂							

2 157 C9

	col 1	col 2	col 3	col 4	col 5
row2	3 ₁				3 ₃₄
row3		3 ₃₄		3 ₁₂	
row6	3 ₂₃		3 ₁₄		
row8	3 ₄		3 ₃		3 ₁₂
row9		3 ₁₂			

2 158	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
new row 1								X	
row 2			2 ₂₄		2 ₁₃				
row 3	2 ₁₃	2 _K			2 ₂₄	2 _K			
row 4						2 ₁₂			2 ₃₄
row 5		X			2 _K				
row 6	2 _K					2 ₃₄			2 ₁₂
row 7							X		
row 8				X					
row 9	2 ₂₄		2 ₁₃						

	col 1	col 3	col 5	col 6	col 9
row2		2 ₂₄	2 ₁₃		
row3	2 ₁₃		2 ₂₄	2 _K	
row4				2 ₁₂	2 ₃₄
row6	2 _K			2 ₃₄	2 ₁₂
row9	2 ₂₄	2 ₁₃			

2 159

ne
w

col 1 col 2 col 3 col 4 col 5 col 6 col 7 col 8 col 9

row1			X					
row2						1 ₁₂	1 ₃₄	
row3					1 ₃₄			1 ₁₂
row4		X						
row5							X	
row6				X				
row7	1 ₂₄					1 ₃	1 ₁	
row8	1 ₁₃					1 ₄	1 ₂	
row9					1 ₁₂			1 ₃₄

2 159

ne
w

col 1 col 5 col 6 col 7 col 9

row2			1 ₁₂	1 ₃₄	
row3		1 ₃₄			1 ₁₂
row7	1 ₂₄		1 ₃	1 ₁	
row8	1 ₁₃		1 ₄	1 ₂	
row9		1 ₁₂			1 ₃₄

2160

ne	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
w									
row1									X
row2	3 ₁		3 ₂		3 ₃₄				
row3		3 ₃₄		3 ₁₂					
row4						X			
row5								X	
row6	3 ₂₃		3 ₁₄						
row7							X		
row8	3 ₄		3 ₃		3 ₁₂				
row9		3 ₁₂		3 ₃₄					

2160

ne	col 1	col 2	col 3	col 4	col 5
w					
row2	3 ₁		3 ₂		3 ₃₄
row3		3 ₃₄		3 ₁₂	
row6	3 ₂₃		3 ₁₄		
row8	3 ₄		3 ₃		3 ₁₂
row9		3 ₁₂		3 ₃₄	

2 161

ne		col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
w									X	
row1									X	
row2						X				
row3			X							
row4		4 ₃₄								4 ₁₂
row5			4 ₁₂					4 ₃₄		
row6				X						
row7		4 ₁				4 ₂₄				4 ₃
row8		4 ₂				4 ₁₃				4 ₄
row9			4 ₃₄					4 ₁₂		

2 161

ne		col 1	col 2	col 5	col 7	col 9
w		4 ₃₄				4 ₁₂
row4		4 ₃₄				4 ₁₂
row5			4 ₁₂		4 ₃₄	
row7		4 ₁		4 ₂₄		4 ₃
row8		4 ₂		4 ₁₃		4 ₄
row9			4 ₃₄		4 ₁₂	

2

162

ne
w

col 1col 2col 3col 4col 5col 6col 7col 8col 9

row1			3 ₁	3 ₂	3 ₃				
row2						X			
row3	3 ₂₃				3 ₁				
row4						X			
row5			3 ₂₃					3 ₁	
row6	3 ₁							3 ₂₃	
row7		X							
row8									X
row9				3 ₁₃	3 ₂				

2 162

ne
w

col 1 col 3 col 4 col 5 col 8

row1		3 ₁	3 ₂	3 ₃	
row3	3 ₂₃			3 ₁	
row5		3 ₂₃			3 ₁
row6	3 ₁				3 ₂₃
row9			3 ₁₃	3 ₂	

2 163

ne	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
w				X					
row1				X					
row2			1 ₃					1 ₁₂	
row3		1 ₁	1 ₂				1 ₃		
row4	X								
row5						X			
row6									X
row7					X				
row8		1 ₂₃					1 ₁		
row9			1 ₁				1 ₂	1 ₃	

2 163

ne	col 2	col 3	col 7	col 8
w		1 ₃		1 ₁₂
row2		1 ₃		1 ₁₂
row3	1 ₁	1 ₂	1 ₃	
row8	1 ₂₃		1 ₁	
row9		1 ₁	1 ₂	1 ₃

PATTERN FILE 3

3
E1

001

col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	6 ₄		6 ₁	6 ₂		6 ₃		
row2			6 ₃			6 ₁₂₄		
row3	6 ₁₂₃			6 ₄				
row4					X			
row5		X						
row6							X	
row7								X
row8	X							
row9			6 ₂₄	6 ₁₃				

3
E1

001

col 2	col 4	col 5	col 7
row1	6 ₄	6 ₁	6 ₂
row2		6 ₃	6 ₁₂₄
row3	6 ₁₂₃		6 ₄
row9		6 ₂₄	6 ₁₃

3
F2

002

col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
							X	
		X						
				3 ₃₅	3 ₁₂₄			
						3 ₁₂₃		3 ₄₅
X								
			X					
	3 ₂₃			3 ₁		3 ₄₅		
	3 ₁₄₅			3 ₂	3 ₃			
				3 ₄	3 ₅			3 ₁₂₃

3

002

col 2	col 5	col 6	col 7	col 9
	3 ₃₅	3 ₁₂₄		
			3 ₁₂₃	3 ₄₅
3 ₂₃	3 ₁		3 ₄₅	
3 ₁₄₅	3 ₂	3 ₃		
	3 ₄	3 ₅		3 ₁₂₃

3 003
G1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	2 ₂₅							2 ₁₄	2 ₃
row2						X			
row3			2 ₁₃₄					2 ₂₅	
row4				X					
row5	2 ₁		2 ₂					2 ₃	2 ₄₅
row6	2 ₃₄		2 ₅						2 ₁₂
row7					X				
row8		X							
row9							X		

3 003
G1

	col 1	col 3	col 8	col 9
row1	2 ₂₅		2 ₁₄	2 ₃
row3		2 ₁₃₄	2 ₂₅	
row5	2 ₁	2 ₂	2 ₃	2 ₄₅
row6	2 ₃₄	2 ₅		2 ₁₂

3 004
C8

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							2 ₂₃₄	2 ₁	
row2					X				
row3	X								
row4				X					
row5			2 ₁₂						2 ₃₄
row6		2 ₃₄					2 ₁	2 ₂	
row7		2 ₁₂						2 ₃₄	
row8			2 ₃			2 ₄			2 ₁₂
row9			2 ₄			2 ₁₂₃			

3 004
C8

	col 2	col 3	col 6	col 7	col 8	col 9
row1				2 ₂₃₄	2 ₁	
row5		2 ₁₂				2 ₃₄
row6	2 ₃₄			2 ₁	2 ₂	
row7	2 ₁₂				2 ₃₄	
row8		2 ₃	2 ₄			2 ₁₂
row9		2 ₄	2 ₁₂₃			

3
A5

005	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					X				
row2			X						
row3							5 ₁		5 ₂₃₄
row4				5 ₁			5 ₂₃₄		
row5	X								
row6				5 ₂		5 ₃₄			5 ₁
row7		5 ₄		5 ₃		5 ₁₂			
row8		5 ₁₂₃		5 ₄					
row9								X	

3

005	col 2	col 4	col 6	col 7	col 9
row3				5 ₁	5 ₂₃₄
row4		5 ₁		5 ₂₃₄	
row6		5 ₂	5 ₃₄		5 ₁
row7	5 ₄	5 ₃	5 ₁₂		
row8	5 ₁₂₃	5 ₄			

3
D1

006	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2					X				
row3		X							
row4	X								
row5				1 ₁₂		1 ₃	1 ₄		
row6				1 ₄			1 ₁₃	1 ₂	
row7			X						
row8				1 ₃		1 ₁₄	1 ₂		
row9						1 ₂		1 ₁₃₄	

equivalent to 2.085

3	006	col 4	col 6	col 7	col 8
	row5	1 ₁₂	1 ₃	1 ₄	
	row6	1 ₄		1 ₁₃	1 ₂
	row8	1 ₃	1 ₁₄	1 ₂	
	row9		1 ₂		1 ₁₃₄

3
E1

007	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						7 ₃₄	7 ₁	7 ₂	
row2		X							
row3						7 ₁₂		7 ₃	7 ₄
row4							7 ₂₃₄	7 ₁	
row5			X						
row6					X				
row7								7 ₄	7 ₁₂₃
row8				X					
row9	X								

3
E1

007	col 6	col 7	col 8	col 9
row1	7 ₃₄	7 ₁	7 ₂	
row3	7 ₁₂		7 ₃	7 ₄
row4		7 ₂₃₄	7 ₁	
row7			7 ₄	7 ₁₂₃

3
A2

008

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				9 ₂₃					9 ₁
row2		X							
row3				9 ₁			9 ₂₃		
row4					X				
row5								X	
row6			X						
row7						X			
row8	9 ₃						9 ₁		9 ₂
row9	9 ₁₂								9 ₃

3
A2

008

	col 1	col 4	col 7	col 9
row1		9 ₂₃		9 ₁
row3		9 ₁	9 ₂₃	
row8	9 ₃		9 ₁	9 ₂
row9	9 ₁₂			9 ₃

3
B4

009

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				1 ₄₅	1 ₁₂₃				
row2	X								
row3								X	
row4							1 ₃₅		1 ₁₂₄
row5						X			
row6		X							
row7				1 ₁			1 ₂₄		1 ₃₅
row8			X						
row9				1 ₂₃	1 ₄₅		1 ₁		

3
B4

009

	col 4	col 5	col 7	col 9
row1	1 ₄₅	1 ₁₂₃		
row4			1 ₃₅	1 ₁₂₄
row7	1 ₁		1 ₂₄	1 ₃₅
row9	1 ₂₃	1 ₄₅	1 ₁	

3
B4

010

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			1 ₁₂		1 ₃₄₅				
row2		1 ₃	1 ₄₅		1 ₁₂				
row3							X		
row4	X								
row5						X			
row6									X
row7		1 ₁₄						1 ₂₃₅	
row8		1 ₂₅	1 ₃					1 ₁₄	
row9				X					

3
B4

010

	col 2	col 3	col 5	col 8
row1		1 ₁₂	1 ₃₄₅	
row2	1 ₃	1 ₄₅	1 ₁₂	
row7	1 ₁₄			1 ₂₃₅
row8	1 ₂₅	1 ₃		1 ₁₄

3
A4

011

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	8 ₂								8 ₁₃₄
row2						X			
row3		8 ₁₃₄							8 ₂
row4	8 ₃		8 ₁₂	8 ₄					
row5	8 ₄			8 ₁₂₃					
row6								X	
row7					X				
row8							X		
row9	8 ₁	8 ₂	8 ₃₄						

3
A4

011

	col 1	col 2	col 3	col 4	col 9
row1	8 ₂				8 ₁₃₄
row3		8 ₁₃₄			8 ₂
row4	8 ₃		8 ₁₂	8 ₄	
row5	8 ₄			8 ₁₂₃	
row9	8 ₁	8 ₂	8 ₃₄		

3
A6

012	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2				8 ₃₄					8 ₁₂₅
row3						8 ₁₂₅		8 ₃₄	
row4							X		
row5	8 ₅			8 ₁₂		8 ₃₄			
row6	8 ₁₃	8 ₂₄		8 ₅					
row7	8 ₂₄	8 ₁₃₅							
row8					X				
row9								8 ₁₂₅	8 ₃₄

3

012	col 1	col 2	col 4	col 6	col 8	col 9
row2			8 ₃₄			8 ₁₂₅
row3				8 ₁₂₅	8 ₃₄	
row5	8 ₅		8 ₁₂	8 ₃₄		
row6	8 ₁₃	8 ₂₄	8 ₅			
row7	8 ₂₄	8 ₁₃₅				

3

013

col 1col 2col 3col 4col 5col 6col 7col 8col 9

F2

row1			4 ₁₃	4 ₂₄₅					
row2	4 ₂₄₅			4 ₁₃					
row3								X	
row4						X			
row5	4 ₁	4 ₂							4 ₃₄₅
row6	4 ₃	4 ₄	4 ₅						4 ₁₂
row7									
row8							X		
row9		4 ₁₃₅	4 ₂₄						

3

013

col 1col 2col 3col 4col 9

F2

row1			4 ₁₃	4 ₂₄₅	
row2	4 ₂₄₅			4 ₁₃	
row5	4 ₁	4 ₂			4 ₃₄₅
row6	4 ₃	4 ₄	4 ₅		4 ₁₂
row9		4 ₁₃₅	4 ₂₄		

3
E7

014

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		8 ₁₂₃					8 _K	8 ₄	
row2						X			
row3	8 ₄								8 ₁₂₃
row4					X				
row5		8 ₄					8 ₃	8 ₁₂	
row6	8 ₁₂₃						8 ₄		
row7				8 ₂₃			8 ₁		8 ₄
row8			X						
row9				8 ₁₄			8 ₂	8 ₃	

3
E7

014

	col 1	col 2	col 4	col 7	col 8	col 9
row1		8 ₁₂₃		8 _K	8 ₄	
row3	8 ₄					8 ₁₂₃
row5		8 ₄		8 ₃	8 ₁₂	
row6	8 ₁₂₃			8 ₄		
row7			8 ₂₃	8 ₁		8 ₄
row9			8 ₁₄	8 ₂	8 ₃	

3
B4

015

col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
X								
						8 ₂₄₅	8 ₁₃	
	8 ₃₄	8 ₁₂₅						
	8 ₁₂	8 ₃₄					8 ₅	
	8 ₅					8 ₁₃	8 ₂₄	

3

015

col 2	col 3	col 7	col 8
		8 ₂₄₅	8 ₁₃
8 ₃₄	8 ₁₂₅		
8 ₁₂	8 ₃₄		8 ₅
8 ₅		8 ₁₃	8 ₂₄

3
F2

016	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			4 ₁₂	4 ₃₄₅					
row2	4 ₃₄₅			4 ₁₂					
row3								X	
row4						X			
row5	4 ₁	4 ₃							4 ₂₄₅
row6	4 ₂	4 ₄	4 ₅						4 ₁₃
row7							X		
row8					X				
row9		4 ₁₂₅	4 ₃₄						

3
F2

016	col 1	col 2	col 3	col 4	col 9
row1			4 ₁₂	4 ₃₄₅	
row2	4 ₃₄₅			4 ₁₂	
row5	4 ₁	4 ₃			4 ₂₄₅
row6	4 ₂	4 ₄	4 ₅		4 ₁₃
row9		4 ₁₂₅	4 ₃₄		

3
C9

017	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						X			
row2								X	
row3		2 ₄	2 ₁₂₃						
row4		2 ₁₂							2 ₃₄
row5				2 ₂₃₄			2 ₁		
row6	2 ₃₄			2 ₁			2 ₂		
row7	2 ₁₂						2 ₃₄		
row8					X				
row9		2 ₃	2 ₄						2 ₁₂

3

017	col 1	col 2	col 3	col 4	col 7	col 9
row3		2 ₄	2 ₁₂₃			
row4		2 ₁₂				2 ₃₄
row5				2 ₂₃₄	2 ₁	
row6	2 ₃₄			2 ₁	2 ₂	
row7	2 ₁₂				2 ₃₄	
row9		2 ₃	2 ₄			2 ₁₂

3
B4

018

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	X								
row2						X			
row3							8 ₂₄₅	8 ₁₃	
row4		8 ₃₄	8 ₁₂₅						
row5				X					
row6									X
row7					X				
row8		8 ₁₂	8 ₃₄					8 ₅	
row9		8 ₅					8 ₁₃	8 ₂₄	

3

018

	col 2	col 3	col 7	col 8
row3			8 ₂₄₅	8 ₁₃
row4	8 ₃₄	8 ₁₂₅		
row8	8 ₁₂	8 ₃₄		8 ₅
row9	8 ₅		8 ₁₃	8 ₂₄

3
D1

019	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1								X	
row2				X					
row3			X						
row4		X							
row5						3 ₁₂			3 ₃₄
row6					3 ₃	3 ₄	3 ₁		3 ₂
row7	X								
row8					3 ₁		3 ₂₃₄		
row9					3 ₂₄	3 ₃			3 ₁

3

019	col 5	col 6	col 7	col 9
row5		3 ₁₂		3 ₃₄
row6	3 ₃	3 ₄	3 ₁	3 ₂
row8	3 ₁		3 ₂₃₄	
row9	3 ₂₄	3 ₃		3 ₁

3
A4

020	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				X					
row2			X						
row3							9 ₁₂	9 ₃	9 ₄
row4						X			
row5	9 ₁₄								9 ₂₃
row6	9 ₂₃							9 ₁₄	
row7					9 ₂₃				9 ₁
row8		X							
row9					9 ₁		9 ₃₄	9 ₂	

3

020	col 1	col 5	col 7	col 8	col 9
row3			9 ₁₂	9 ₃	9 ₄
row5	9 ₁₄				9 ₂₃
row6	9 ₂₃			9 ₁₄	
row7		9 ₂₃			9 ₁
row9		9 ₁	9 ₃₄	9 ₂	

3
D1

021	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2		X							
row3						X			
row4	1 ₂		1 ₃₄				1 ₁		
row5			1 ₁				1 ₂₃	1 ₄	
row6					X				
row7	1 ₁₃₄							1 ₂	
row8				X					
row9			1 ₂				1 ₄	1 ₁₃	

3

021	col 1	col 3	col 7	col 8
row4	1 ₂	1 ₃₄	1 ₁	
row5		1 ₁	1 ₂₃	1 ₄
row7	1 ₁₃₄			1 ₂
row9		1 ₂	1 ₄	1 ₁₃

3
E1

022	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				9 ₂₄	9 ₁₃				
row2								X	
row3			X						
row4					9 ₄	9 ₁₂₃			
row5		X							
row6									X
row7				9 ₁	9 ₂		9 ₃₄		
row8				9 ₃		9 ₄	9 ₁₂		
row9	X								

3
E1

022	col 4	col 5	col 6	col 7
row1	9 ₂₄	9 ₁₃		
row4		9 ₄	9 ₁₂₃	
row7	9 ₁	9 ₂		9 ₃₄
row8	9 ₃		9 ₄	9 ₁₂

3
D1

023

col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		4 ₁		4 ₂₄	4 ₃			
row2								X
row3		4 ₂₃	4 ₄		4 ₁			
row4	X							
row5							X	
row6			X					
row7		4 ₄			4 ₃	4 ₁₂		
row8			4 ₁₂₃		4 ₄			
row9						X		

3
D1

023

col 2	col 3	col 5	col 6
row1	4 ₁	4 ₂₄	4 ₃
row3	4 ₂₃	4 ₄	4 ₁
row7	4 ₄	4 ₃	4 ₁₂
row8	4 ₁₂₃		4 ₄

3
C8

024	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1								1 ₂	1 ₁₃₄
row2			X						
row3						X			
row4				X					
row5	1 ₁₂						1 ₃₄		
row6		1 ₃₄						1 ₁	1 ₂
row7	1 ₃				1 ₄		1 ₁₂		
row8		1 ₁₂						1 ₃₄	
row9	1 ₄				1 ₁₂₃				

3
C8

024	col 1	col 2	col 5	col 7	col 8	col 9
row1					1 ₂	1 ₁₃₄
row5	1 ₁₂			1 ₃₄		
row6		1 ₃₄			1 ₁	1 ₂
row7	1 ₃		1 ₄	1 ₁₂		
row8		1 ₁₂			1 ₃₄	
row9	1 ₄		1 ₁₂₃			

3
D2

025

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	1 ₁₂						1 ₃₄₅		
row2						X			
row3	1 ₃₄	1 ₅							1 ₁₂
row4								X	
row5			1 ₁₃		1 ₂₄₅				
row6	1 ₅		1 ₂₄		1 ₁₃				
row7		1 ₁₂							1 ₃₄₅
row8		1 ₃₄	1 ₅				1 ₁₂		
row9				X					

3
D2

025

	col 1	col 2	col 3	col 5	col 7	col 8	col 9
row1	1 ₁₂				1 ₃₄₅		
row3	1 ₃₄	1 ₅					1 ₁₂
row5			1 ₁₃	1 ₂₄₅			
row6	1 ₅		1 ₂₄	1 ₁₃			
row7		1 ₁₂					1 ₃₄₅
row8		1 ₃₄	1 ₅		1 ₁₂		

3
D3

026

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		1 ₁₂		1 ₅				1 ₃₄	
row2	1 ₃			1 ₁₄					1 ₂₅
row3		1 ₄₅		1 ₂₃					1 ₁
row4						X			
row5							X		
row6			X						
row7	1 ₄	1 ₃						1 ₁₂₅	
row8	1 ₁₂₅								1 ₃₄
row9					X				

3
D3

026

	col 1	col 2	col 4	col 8	col 9
row1		1 ₁₂	1 ₅	1 ₃₄	
row2	1 ₃		1 ₁₄		1 ₂₅
row3		1 ₄₅	1 ₂₃		1 ₁
row7	1 ₄	1 ₃		1 ₁₂₅	
row8	1 ₁₂₅				1 ₃₄

3
E8

027	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						9 ₃	9 ₂	9 ₁₄	
row2		X							
row3				9 ₁₂₄				9 ₃	
row4			9 ₃₄					9 _K	9 ₁₂
row5					X				
row6	9 ₁₂						9 ₃₄		
row7	9 ₃₄						9 ₁	9 ₂	
row8						9 ₁₂₄			9 ₃
row9			9 ₁₂	9 ₃					9 ₄

3
E8

027	col 1	col 3	col 4	col 6	col 7	col 8	col 9
row1				9 ₃	9 ₂	9 ₁₄	
row3			9 ₁₂₄			9 ₃	
row4		9 ₃₄				9 _K	9 ₁₂
row6	9 ₁₂				9 ₃₄		
row7	9 ₃₄				9 ₁	9 ₂	
row8				9 ₁₂₄			9 ₃
row9		9 ₁₂	9 ₃				9 ₄

3
D1

028	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2		X							
row3						X			
row4	1 ₂		1 ₃₄				1 ₁		
row5			1 ₁				1 ₂₃	1 ₄	
row6					X				
row7	1 ₁₃₄							1 ₂	
row8				X					
row9			1 ₂				1 ₄	1 ₁₃	

3

028	col 1	col 3	col 7	col 8
row4	1 ₂	1 ₃₄	1 ₁	
row5		1 ₁	1 ₂₃	1 ₄
row7	1 ₁₃₄			1 ₂
row9		1 ₂	1 ₄	1 ₁₃

3
B3

029

col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		2 ₁		2 ₂₄				2 ₃
row2		2 ₂		2 ₁₃			2 ₄	
row3		2 ₃₄					2 ₁₂	
row4						X		
row5			X					
row6		X						
row7							2 ₃	2 ₁₂₄
row8	X							
row9					X			

3
B3

029

col 3	col 5	col 8	col 9
row1	2 ₁	2 ₂₄	2 ₃
row2	2 ₂	2 ₁₃	2 ₄
row3	2 ₃₄		2 ₁₂
row7			2 ₃

3
A7

030	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					X				
row2		X							
row3							1 ₄		1 ₁₂₃
row4	1 ₁		1 ₂			1 ₃₄			
row5			1 ₃₄				1 ₁₂		
row6				1 ₁₂			1 ₃		1 ₄
row7	1 ₂₃₄		1 ₁						
row8				1 ₃₄		1 ₁₂			
row9								X	

3

030	col 1	col 3	col 4	col 6	col 7	col 9
row3					1 ₄	1 ₁₂₃
row4	1 ₁	1 ₂		1 ₃₄		
row5		1 ₃₄			1 ₁₂	
row6			1 ₁₂		1 ₃	1 ₄
row7	1 ₂₃₄	1 ₁				
row8			1 ₃₄	1 ₁₂		

3
A8

031	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							X		
row2				X					
row3			X						
row4	1 ₃₄					1 ₁₂			
row5	1 ₁	1 ₂				1 ₃			1 ₄
row6						1 ₄			1 ₁₂₃
row7					X				
row8	1 ₂	1 ₁₃₄							
row9								X	

3

031	col 1	col 2	col 6	col 9
row4	1 ₃₄		1 ₁₂	
row5	1 ₁	1 ₂	1 ₃	1 ₄
row6			1 ₄	1 ₁₂₃
row8	1 ₂	1 ₁₃₄		

3
A9

032

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	5 ₂₃₄				5 ₁				
row2	5 ₁			5 ₃₄	5 ₂				
row3									X
row4						X			
row5		X							
row6								X	
row7					5 ₃		5 ₁₂₄		
row8				5 ₁₂	5 ₄		5 ₃		
row9			X						

3
A9

032

	col 1	col 4	col 5	col 7
row1	5 ₂₃₄		5 ₁	
row2	5 ₁	5 ₃₄	5 ₂	
row7			5 ₃	5 ₁₂₄
row8		5 ₁₂	5 ₄	5 ₃

3
G3

033

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				X					
row2		8 ₂					8 ₁		8 ₃₄
row3		8 ₁₃₄						8 ₂	
row4					8 ₁₂₄			8 ₃	
row5			X						
row6					8 ₃		8 ₄		8 ₁₂
row7	X								
row8						X			
row9							8 ₂₃	8 ₁₄	

3

033

	col 2	col 5	col 7	col 8	col 9
row2	8 ₂		8 ₁		8 ₃₄
row3	8 ₁₃₄			8 ₂	
row4		8 ₁₂₄		8 ₃	
row6		8 ₃	8 ₄		8 ₁₂
row9			8 ₂₃	8 ₁₄	

3
F1

034

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				2 ₃₅		2 ₁₂₄			
row2			X						
row3							X		
row4				2 ₁	2 ₂	2 ₃		2 ₄₅	
row5					2 ₄	2 ₅		2 ₁₂₃	
row6		X							
row7				2 ₂₄	2 ₁₃₅				
row8									X
row9	X								

3
F1

034

	col 4	col 5	col 6	col 8
row1	2 ₃₅		2 ₁₂₄	
row4	2 ₁	2 ₂	2 ₃	2 ₄₅
row5		2 ₄	2 ₅	2 ₁₂₃
row7	2 ₂₄	2 ₁₃₅		

3
B4

035

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							2 ₁₂₄		2 ₃
row2	X								
row3				X					
row4					2 ₁	2 ₂	2 ₃		2 ₄
row5			X						
row6					2 ₃₄				2 ₁₂
row7								X	
row8					2 ₂	2 ₁₃₄			
row9		X							

3
B4

035

	col 5	col 6	col 7	col 9
row1			2 ₁₂₄	2 ₃
row4	2 ₁	2 ₂	2 ₃	2 ₄
row6	2 ₃₄			2 ₁₂
row8	2 ₂	2 ₁₃₄		

3
D1

036

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					X				
row2							X		
row3			X						
row4		X							
row5				2 ₁₂		2 ₃		2 ₄	
row6				2 ₄					2 ₁₂₃
row7						2 ₂₄		2 ₁₃	
row8	X								
row9				2 ₃		2 ₁		2 ₂	2 ₄

3

036

	col 4	col 6	col 8	col 9
row5	2 ₁₂	2 ₃	2 ₄	
row6	2 ₄			2 ₁₂₃
row7		2 ₂₄	2 ₁₃	
row9	2 ₃	2 ₁	2 ₂	2 ₄

3
B4

037

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					2 ₁		2 ₂₃		2 ₄
row2		X							
row3					2 ₂₃₄				2 ₁
row4			X						
row5				X					
row6								X	
row7						X			
row8	2 ₁₃₄								2 ₂
row9	2 ₂						2 ₁₄		2 ₃

3
B4

037

	col 1	col 5	col 7	col 9
row1		2 ₁	2 ₂₃	2 ₄
row3		2 ₂₃₄		2 ₁
row8	2 ₁₃₄			2 ₂
row9	2 ₂		2 ₁₄	2 ₃

3

G4

038

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	4 ₁				4 ₂			4 ₃	4 ₄
row2	4 ₂₃₄				4 ₁				
row3					4 ₃₄				4 ₁₂
row4				X					
row5		X							
row6							X		
row7						4 ₁₂₄			4 ₃
row8			X						
row9						4 ₃		4 ₁₂₄	

3

G4

038

	col 1	col 5	col 6	col 8	col 9
row1	4 ₁	4 ₂		4 ₃	4 ₄
row2	4 ₂₃₄	4 ₁			
row3		4 ₃₄			4 ₁₂
row7			4 ₁₂₄		4 ₃
row9			4 ₃	4 ₁₂₄	

3
B4

039

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						X			
row2	1 ₁₂	1 ₃							1 ₄₅
row3	1 ₄₅								1 ₁₂₃
row4								X	
row5					X				
row6			X						
row7				X					
row8	1 ₃	1 ₁₄					1 ₂₅		
row9		1 ₂₅					1 ₁₃₄		

3

039

	col 1	col 2	col 7	col 9
row2	1 ₁₂	1 ₃		1 ₄₅
row3	1 ₄₅			1 ₁₂₃
row8	1 ₃	1 ₁₄	1 ₂₅	
row9		1 ₂₅	1 ₁₃₄	

3
G5

040	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		X							
row2							X		
row3				X					
row4						7 ₁₃₄		7 ₂	
row5			7 ₁₂					7 ₃	7 ₄
row6			7 ₃₄			7 ₂			7 ₁
row7					7 ₁₄				7 ₂₃
row8					7 ₂₃			7 ₁₄	
row9	X								

3

040	col 3	col 5	col 6	col 8	col 9
row4			7 ₁₃₄	7 ₂	
row5	7 ₁₂			7 ₃	7 ₄
row6	7 ₃₄		7 ₂		7 ₁
row7		7 ₁₄			7 ₂₃
row8		7 ₂₃		7 ₁₄	

3
B4

041	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2							X		
row3				X					
row4									
row5								1 ₄	1 ₁₂₃
row6	1 ₁	1 ₂₃₄							
row7					X				
row8	1 ₂	1 ₁						1 ₃	1 ₄
row9	1 ₃₄							1 ₁₂	

3

041	col 1	col 2	col 8	col 9
row5			1 ₄	1 ₁₂₃
row6	1 ₁	1 ₂₃₄		
row8	1 ₂	1 ₁	1 ₃	1 ₄
row9	1 ₃₄		1 ₁₂	

3
G6

042

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	7 ₁₂₃								7 ₄
row2						X			
row3			7 ₄				7 ₁₂		7 ₃
row4				X					
row5								7 ₂₃₄	7 ₁
row6	7 ₄		7 ₁₂₃						
row7					X				
row8							7 ₃₄	7 ₁	7 ₂
row9		X							

3
G6

042

	col 1	col 3	col 7	col 8	col 9
row1	7 ₁₂₃				7 ₄
row3		7 ₄	7 ₁₂		7 ₃
row5				7 ₂₃₄	7 ₁
row6	7 ₄	7 ₁₂₃			
row8			7 ₃₄	7 ₁	7 ₂

3
B3

043

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2				2 ₁			2 ₂₃₄		
row3					2 ₂	2 ₃₄	2 ₁		
row4				2 ₃	2 ₄	2 ₁₂			
row5									X
row6		X							
row7				2 ₂₄	2 ₁₃				
row8	X								
row9								X	

3

043

	col 4	col 5	col 6	col 7
row2	2 ₁			2 ₂₃₄
row3		2 ₂	2 ₃₄	2 ₁
row4	2 ₃	2 ₄	2 ₁₂	
row7	2 ₂₄	2 ₁₃		

3
B3

044

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		4 ₁₂₃		4 ₄					
row2							X		
row3		4 ₄		4 ₁	4 ₂₃				
row4			X						
row5								X	
row6				4 ₂	4 ₁₄	4 ₃			
row7									X
row8				4 ₃		4 ₁₂₄			
row9	X								

3
B3

044

	col 2	col 4	col 5	col 6
row1	4 ₁₂₃	4 ₄		
row3	4 ₄	4 ₁	4 ₂₃	
row6		4 ₂	4 ₁₄	4 ₃
row8		4 ₃		4 ₁₂₄

3
B5

045	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							X		
row2		X							
row3				4 ₁₂₃	4 ₄				
row4					4 ₁₂			4 ₃₄	
row5				4 ₄		4 ₃		4 ₁	4 ₂
row6			X						
row7								4 ₂	4 ₁₃₄
row8					4 ₃	4 ₁₂₄			
row9	X								

3

045	col 4	col 5	col 6	col 8	col 9
row3	4 ₁₂₃	4 ₄			
row4		4 ₁₂		4 ₃₄	
row5	4 ₄		4 ₃	4 ₁	4 ₂
row7				4 ₂	4 ₁₃₄
row8		4 ₃	4 ₁₂₄		

3
B5

046

col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
						X		
				9 ₂₄	9 ₁₃₅			
9 ₁₂	9 ₃₄₅							
		X						
							X	
			9 ₂₄₅	9 ₁₃				
								X
9 ₃₄	9 ₁₂			9 ₅				
9 ₅			9 ₁₃		9 ₂₄			

3

046

col 1	col 2	col 4	col 5	col 6
			9 ₂₄	9 ₁₃₅
9 ₁₂	9 ₃₄₅			
		9 ₂₄₅	9 ₁₃	
9 ₃₄	9 ₁₂		9 ₅	
9 ₅		9 ₁₃		9 ₂₄

3
B4

047	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					X				
row2							X		
row3			X						
row4									X
row5	1 ₁₂			1 ₃		1 ₄₅			
row6	1 ₃₄₅					1 ₁₂			
row7				1 ₁₄		1 ₃		1 ₂₅	
row8		X							
row9				1 ₂₅				1 ₁₃₄	

3

047	col 1	col 4	col 6	col 8
row5	1 ₁₂	1 ₃	1 ₄₅	
row6	1 ₃₄₅		1 ₁₂	
row7		1 ₁₄	1 ₃	1 ₂₅
row9		1 ₂₅		1 ₁₃₄

3

048	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		9 ₁₂						9 ₃₄	
row2	9 ₃					9 ₂₄	9 ₁		
row3		9 ₄				9 ₁₃	9 ₂		
row4							9 ₃₄	9 ₁₂	
row5	9 ₁₂₄	9 ₃							
row6					X				
row7			X						
row8									X
row9				X					

3

048	col 1	col 2	col 6	col 7	col 8
row1		9 ₁₂			9 ₃₄
row2	9 ₃		9 ₂₄	9 ₁	
row3		9 ₄	9 ₁₃	9 ₂	
row4				9 ₃₄	9 ₁₂
row5	9 ₁₂₄	9 ₃			

3
E1

049

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		X							
row2								X	
row3					3 ₁₂₄	3 ₃			
row4	3 ₂					3 ₁	3 ₃₄		
row5	3 ₁₃₄					3 ₂			
row6					3 ₃	3 ₄	3 ₁₂		
row7				X					
row8			X						
row9									X

3

049

	col 1	col 5	col 6	col 7
row3		3 ₁₂₄	3 ₃	
row4	3 ₂		3 ₁	3 ₃₄
row5	3 ₁₃₄		3 ₂	
row6		3 ₃	3 ₄	3 ₁₂

3
B4

050

col 1

col 2

col 3

col 4

col 5

col 6

col 7

col 8

col 9

row1							X		
row2						X			
row3			X						
row4									X
row5	3 ₁₂			3 ₃₄	3 ₅				
row6	3 ₃₄₅			3 ₁₂					
row7		3 ₂₄₅			3 ₁₃				
row8		3 ₁₃		3 ₅	3 ₂₄				
row9							X		

3

050

col 1

col 2

col 4

col 5

row5	3 ₁₂		3 ₃₄	3 ₅
row6	3 ₃₄₅		3 ₁₂	
row7		3 ₂₄₅		3 ₁₃
row8		3 ₁₃	3 ₅	3 ₂₄

3
B4

051	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1								X	
row2						X			
row3			X						
row4		X							
row5				5 ₁₂	5 ₃₄		5 ₅		
row6				5 ₅			5 ₁₃		5 ₂₄
row7							5 ₂₄		5 ₁₃₅
row8	X								
row9				5 ₃₄	5 ₁₂₅				

3

051	col 4	col 5	col 7	col 9
row5	5 ₁₂	5 ₃₄	5 ₅	
row6	5 ₅		5 ₁₃	5 ₂₄
row7			5 ₂₄	5 ₁₃₅
row9	5 ₃₄	5 ₁₂₅		

3
E9

052

col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			3 ₁₄				3 ₂₃₅₆	
row2						X		
row3	3 ₃₆		3 ₂₅				3 ₁₄	
row4							X	
row5	3 ₁₂		3 ₃	3 ₄₅₆				
row6	3 ₄₅		3 ₆		3 ₁₂₃			
row7				3 ₁₂₃	3 ₄₅₆			
row8								X
row9		X						

3
E9

052

col 1	col 3	col 4	col 5	col 7	
row1		3 ₁₄			3 ₂₃₅₆
row3	3 ₃₆	3 ₂₅			3 ₁₄
row5	3 ₁₂	3 ₃	3 ₄₅₆		
row6	3 ₄₅	3 ₆		3 ₁₂₃	
row7			3 ₁₂₃	3 ₄₅₆	

3
G1

053

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	4 ₁₂	4 ₃₄							4 ₅
row2					X				
row3		4 ₅					4 ₁₃		4 ₂₄
row4								X	
row5			X						
row6						X			
row7	4 ₃	4 ₁					4 ₂₄₅		
row8				X					
row9	4 ₄₅	4 ₂							4 ₁₃

3
G1

053

	col 1	col 2	col 7	col 9
row1	4 ₁₂	4 ₃₄		4 ₅
row3		4 ₅	4 ₁₃	4 ₂₄
row7	4 ₃	4 ₁	4 ₂₄₅	
row9	4 ₄₅	4 ₂		4 ₁₃

3
B8

054

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			8 ₁₂					8 ₃₄₅	
row2		8 ₃₄				8 ₅		8 ₁₂	
row3		8 ₅		8 ₁₃		8 ₂₄			
row4					X				
row5		8 ₁₂	8 ₃₄₅						
row6							X		
row7				8 ₂₄₅		8 ₁₃			
row8									X
row9	X								

3
B8

054

	col 2	col 3	col 4	col 6	col 8
row1		8 ₁₂			8 ₃₄₅
row2	8 ₃₄			8 ₅	8 ₁₂
row3	8 ₅		8 ₁₃	8 ₂₄	
row5	8 ₁₂	8 ₃₄₅			
row7			8 ₂₄₅	8 ₁₃	

3
E9

055

col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			3 ₁₄				3 ₂₃₅₆	
row2						X		
row3	3 ₃₆		3 ₂₅				3 ₁₄	
row4							X	
row5	3 ₁₂		3 ₃	3 ₄₅₆				
row6	3 ₄₅		3 ₆		3 ₁₂₃			
row7				3 ₁₂₃	3 ₄₅₆			
row8								X
row9		X						

3
E9

055

col 1	col 3	col 4	col 5	col 7
row1	3 ₁₄			3 ₂₃₅₆
row3	3 ₃₆	3 ₂₅		3 ₁₄
row5	3 ₁₂	3 ₃	3 ₄₅₆	
row6	3 ₄₅	3 ₆		3 ₁₂₃
row7			3 ₁₂₃	3 ₄₅₆

3
E4

056	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				X					
row2		X							
row3								4 ₂₅₆	4 ₁₃₄
row4	4 ₂₃₅				4 ₄₆			4 ₁	
row5	4 ₁₄₆				4 ₃₅				4 ₂
row6					4 ₁₂			4 ₃₄	4 ₅₆
row7							X		
row8						X			
row9			X						

3

056	col 1	col 5	col 8	col 9
row3			4 ₂₅₆	4 ₁₃₄
row4	4 ₂₃₅	4 ₄₆	4 ₁	
row5	4 ₁₄₆	4 ₃₅		4 ₂
row6		4 ₁₂	4 ₃₄	4 ₅₆

3 057
E6

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							X		
row2	8 ₁		8 ₃	8 ₂₅		8 ₄			
row3			8 ₂₄₅			8 ₁₃			
row4			8 ₁			8 ₂		8 ₃₄₅	
row5	8 ₂		8 _K	8 ₁₃₄		8 ₅			
row6	8 ₃₄₅							8 ₁₂	
row7									X
row8		X							
row9					X				

3 057

	col 1	col 3	col 4	col 6	col 8
row2	8 ₁	8 ₃	8 ₂₅	8 ₄	
row3		8 ₂₄₅		8 ₁₃	
row4		8 ₁		8 ₂	8 ₃₄₅
row5	8 ₂	8 _K	8 ₁₃₄	8 ₅	
row6	8 ₃₄₅				8 ₁₂

3 058
E6

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									X
row2	8 ₁		8 ₂	8 ₃₄		8 ₅			
row3			8 ₃₄₅			8 ₁₂			
row4			8 ₁			8 ₃		8 ₂₄₅	
row5	8 ₃		8 _K	8 ₁₂₅		8 ₄			
row6	8 ₂₄₅							8 ₁₃	
row7					X				
row8		X							
row9							X		

3 058

	col 1	col 3	col 4	col 6	col 8
row2	8 ₁	8 ₂	8 ₃₄	8 ₅	
row3		8 ₃₄₅		8 ₁₂	
row4		8 ₁		8 ₃	8 ₂₄₅
row5	8 ₃	8 _K	8 ₁₂₅	8 ₄	
row6	8 ₂₄₅				8 ₁₃

3
C9

059	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							1 ₁₂₄	1 ₃	
row2		X							
row3						X			
row4			1 ₁	1 ₂					1 ₃₄
row5			1 ₂	1 ₁₃₄					
row6	1 ₃₄							1 ₁₂	
row7	1 ₁₂						1 ₃	1 ₄	
row8					X				
row9			1 ₃₄						1 ₁₂

3
C9

059	col 1	col 3	col 4	col 7	col 8	col 9
row1				1 ₁₂₄	1 ₃	
row4		1 ₁	1 ₂			1 ₃₄
row5		1 ₂	1 ₁₃₄			
row6	1 ₃₄				1 ₁₂	
row7	1 ₁₂			1 ₃	1 ₄	
row9		1 ₃₄				1 ₁₂

3 060
G8

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				2 ₃₄			2 ₁	2 ₂	
row2	2 ₄				2 ₁₂				2 ₃
row3	2 ₁₂₃								2 ₄
row4		X							
row5				2 ₁₂				2 ₃₄	
row6					2 ₃₄				2 ₁₂
row7			X						
row8						X			
row9							2 ₂₃₄	2 ₁	

3 060
G8

	col 1	col 4	col 5	col 7	col 8	col 9
row1		2 ₃₄		2 ₁	2 ₂	
row2	2 ₄		2 ₁₂			2 ₃
row3	2 ₁₂₃					2 ₄
row5		2 ₁₂			2 ₃₄	
row6			2 ₃₄			2 ₁₂
row9				2 ₂₃₄	2 ₁	

3 061
A3

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		8 ₁			8 ₃₄		8 ₂		
row2		8 ₂₃					8 ₁₄		
row3	8 ₄				8 ₁₂				8 ₃
row4	8 ₁₂₃	8 ₄							
row5								X	
row6				X					
row7			X						
row8						8 ₃			8 ₁₂₄
row9						8 ₁₂₄	8 ₃		

3 061
A3

	col 1	col 2	col 5	col 6	col 7	col 9
row1		8 ₁	8 ₃₄		8 ₂	
row2		8 ₂₃			8 ₁₄	
row3	8 ₄		8 ₁₂			8 ₃
row4	8 ₁₂₃	8 ₄				
row8				8 ₃		8 ₁₂₄
row9				8 ₁₂₄	8 ₃	

3
E5

062

col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			2 ₃₆		2 ₁₄		2 ₂₅	
row2					2 ₂₅		2 ₁₃₄₆	
row3	X							
row4				X				
row5		X						
row6								X
row7		2 ₄₅₆		2 ₁₂		2 ₃		
row8		2 ₁₂₃		2 ₄₅		2 ₆		
row9						X		

3
E5

062

col 2	col 4	col 6	col 8
row1	2 ₃₆	2 ₁₄	2 ₂₅
row2		2 ₂₅	2 ₁₃₄₆
row7	2 ₄₅₆	2 ₁₂	2 ₃
row8	2 ₁₂₃	2 ₄₅	2 ₆

PATTERN FILE 4

4 001	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C8									
row 1							1 ₃₄₅₈	1 ₁₂₆₇	
row 2	X								
row 3				X					
row 4					X				
row 5			1 ₅₆₇₈						1 ₁₂₃₄
row 6		1 ₁₂₃₄					1 ₆₇	1 ₅₈	
row 7		1 ₅₆₇₈					1 ₁₂	1 ₃₄	
row 8			1 ₁₃			1 ₂₄₇₈			1 ₅₆
row 9			1 ₂₄			1 ₁₃₅₆			1 ₇₈

4 001	col 2	col 3	col 6	col 7	col 8	col 9
C8						
row 1				1 ₃₄₅₈	1 ₁₂₆₇	
row 5		1 ₅₆₇₈				1 ₁₂₃₄
row 6	1 ₁₂₃₄			1 ₆₇	1 ₅₈	
row 7	1 ₅₆₇₈			1 ₁₂	1 ₃₄	
row 8		1 ₁₃	1 ₂₄₇₈			1 ₅₆
row 9		1 ₂₄	1 ₁₃₅₆			1 ₇₈

4 002	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C0									
row 1		X							
row 2									X
row 3				4 ₁₄₅₆		4 ₂₃			
row 4			4 ₃₅₆		4 ₁		4 ₂₄		
row 5				4 ₂₃		4 ₄₅		4 ₁₆	
row 6			4 ₁₂₄		4 ₆		4 ₃₅		
row 7						4 ₁₆		4 ₂₃₄₅	
row 8	X								
row 9					4 ₂₃₄₅		4 ₁₆		

4 002	col 3	col 4	col 5	col 6	col 7	col 8
row 3		4 ₁₄₅₆		4 ₂₃		
row 4	4 ₃₅₆		4 ₁		4 ₂₄	
row 5		4 ₂₃		4 ₄₅		4 ₁₆
row 6	4 ₁₂₄		4 ₆		4 ₃₅	
row 7				4 ₁₆		4 ₂₃₄₅
row 9			4 ₂₃₄₅		4 ₁₆	

4 003	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
B1									
row 1					2 ₂₄₅₆	2 ₁₃			
row 2		X							
row 3									X
row 4			X						
row 5								X	
row 6				2 ₅₆	2 ₁₃	2 ₂₄			
row 7				2 ₁₂		2 ₅	2 ₃₄₆		
row 8				2 ₃₄		2 ₆	2 ₁₂₅		
row 9	X								

4 003	col 4	col 5	col 6	col 7
B1				
row 1		2 ₂₄₅₆	2 ₁₃	
row 6	2 ₅₆	2 ₁₃	2 ₂₄	
row 7	2 ₁₂		2 ₅	2 ₃₄₆
row 8	2 ₃₄		2 ₆	2 ₁₂₅

4 004	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A6									
row 1									X
row 2			5 ₅	5 ₁₂₃		5 ₄			
row 3			5 ₁₂₃₄			5 ₅			
row 4				5 ₄₅			5 ₁₂	5 ₃	
row 5	X								
row 6						5 ₁₂₃		5 ₄₅	
row 7		5 ₂					5 ₃₄₅	5 ₁	
row 8					X				
row 9		5 ₁₃₄₅						5 ₂	

4 004	col 2	col 3	col 4	col 6	col 7	col 8
row 2		5 ₅	5 ₁₂₃	5 ₄		
row 3		5 ₁₂₃₄		5 ₅		
row 4			5 ₄₅		5 ₁₂	5 ₃
row 6				5 ₁₂₃		5 ₄₅
row 7	5 ₂				5 ₃₄₅	5 ₁
row 9	5 ₁₃₄₅					5 ₂

4	005	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C4	row 1	2 ₃							2 ₁₅	2 ₂₄
	row 2	2 ₄₅		2 ₁₂						2 ₃
	row 3					X				
	row 4		X							
	row 5				X					
	row 6							2 ₂₃₄₅		2 ₁
	row 7			2 ₃₄₅				2 ₁	2 ₂	
	row 8						X			
	row 9	2 ₁₂							2 ₃₄	2 ₅

4	005	col 1	col 3	col 7	col 8	col 9
C4	row1	2 ₃			2 ₁₅	2 ₂₄
	row2	2 ₄₅	2 ₁₂			2 ₃
	row6			2 ₂₃₄₅		2 ₁
	row7		2 ₃₄₅	2 ₁	2 ₂	
	row9	2 ₁₂			2 ₃₄	2 ₅

4

006	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					5 ₂₃			5 ₁₄₅	
row2						5 ₁₄₅		5 ₂₃	
row3		X							
row4							X		
row5	5 ₁₂₃₅		5 ₄						
row6				X					
row7			5 ₅		5 ₁	5 ₂			5 ₃₄
row8	5 ₄					5 ₃			5 ₁₂₅
row9			5 ₁₂₃		5 ₄₅				

	col 1	col 3	col 5	col 6	col 8	col 9
row1			5 ₂₃		5 ₁₄₅	
row2				5 ₁₄₅	5 ₂₃	
row5	5 ₁₂₃₅	5 ₄				
row7		5 ₅	5 ₁	5 ₂		5 ₃₄
row8	5 ₄			5 ₃		5 ₁₂₅
row9		5 ₁₂₃	5 ₄₅			

4 007	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C9									
row 1				5 ₂₅		5 ₁₃	5 ₄₆		
row 2					5 ₄₆			5 ₁₂₃₅	
row 3			X						
row 4					5 ₁₂₃₅			5 ₄₆	
row 5		5 ₁₂₃₅		5 ₆		5 ₄			
row 6	5 ₄₆						5 ₁₂₃₅		
row 7	5 ₃₅	5 ₄₆		5 ₁		5 ₂			
row 8									X
row 9	5 ₁₂			5 ₃₄		5 ₅₆			

4 007	col 1	col 2	col 4	col 5	col 6	col 7	col 8
C9							
row 1			5 ₂₅		5 ₁₃	5 ₄₆	
row 2				5 ₄₆			5 ₁₂₃₅
row 4				5 ₁₂₃₅			5 ₄₆
row 5		5 ₁₂₃₅	5 ₆		5 ₄		
row 6	5 ₄₆					5 ₁₂₃₅	
row 7	5 ₃₅	5 ₄₆	5 ₁		5 ₂		
row 9	5 ₁₂		5 ₃₄		5 ₅₆		

4 008	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A8									
row 1		4 ₁					4 ₂₃₄₅		
row 2					X				
row 3		4 ₂₃	4 ₄₅						4 ₁
row 4	X								
row 5								X	
row 6				X					
row 7		4 ₅				4 ₂₃₄	4 ₁		
row 8						4 ₁₅			4 ₂₃₄
row 9		4 ₄	4 ₁₂₃						4 ₅

4 008	col 2	col 3	col 6	col 7	col 9
A8					
row1	4 ₁			4 ₂₃₄₅	
row3	4 ₂₃	4 ₄₅			4 ₁
row7	4 ₅		4 ₂₃₄	4 ₁	
row8			4 ₁₅		4 ₂₃₄
row9	4 ₄	4 ₁₂₃			4 ₅

4

009	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	2 ₁₂			2 ₅₇			2 ₃₄₆₈		
row2	2 ₃₄			2 ₆₈			2 ₁₂₅₇		
row3		2 ₅₆	2 ₇₈			2 ₁₂₃₄			
row4		2 ₁₃	2 ₂₄			2 ₅₆₇₈			
row5							X		
row6	2 ₅₆₇₈			2 ₁₂₃₄					
row7									X
row8					X				
row9		2 ₂₄₇₈	2 ₁₃₅₆						

4

C8

009	col 1	col 2	col 3	col 4	col 6	col 7
row1	2 ₁₂			2 ₅₇		2 ₃₄₆₈
row2	2 ₃₄			2 ₆₈		2 ₁₂₅₇
row3		2 ₅₆	2 ₇₈		2 ₁₂₃₄	
row4		2 ₁₃	2 ₂₄		2 ₅₆₇₈	
row6	2 ₅₆₇₈			2 ₁₂₃₄		
row9		2 ₂₄₇₈	2 ₁₃₅₆			

4 010 D1

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	1 ₂₆							1 ₁₃₄₅	
row2				X					
row3			1 ₁₃₄₅					1 ₂₆	
row4	1 ₁		1 ₂		1 ₄₅₆				1 ₃
row5	1 ₃₄								1 ₁₂₅₆
row6	1 ₅		1 ₆		1 ₁₂₃				1 ₄
row7							X		
row8						X			
row9		X							

4 010 D1

	col 1	col 3	col 5	col 8	col 9
row 1	1 ₂₆			1 ₁₃₄₅	
row 3		1 ₁₃₄₅		1 ₂₆	
row 4	1 ₁	1 ₂	1 ₄₅₆		1 ₃
row 5	1 ₃₄				1 ₁₂₅₆
row 6	1 ₅	1 ₆	1 ₁₂₃		1 ₄

4 011 A8

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		4 ₁					4 ₂₃₄₅		
row2					X				
row3		4 ₂₃	4 ₄₅						4 ₁
row4				X					
row5								X	
row6	X								
row7		4 ₅				4 ₂₃₄	4 ₁		
row8						4 ₁₅			4 ₂₃₄
row9		4 ₄	4 ₁₂₃						4 ₅

4 011 A8

	col 2	col 3	col 6	col 7	col 9
row 1	4 ₁			4 ₂₃₄₅	
row 3	4 ₂₃	4 ₄₅			4 ₁
row 7	4 ₅		4 ₂₃₄	4 ₁	
row 8			4 ₁₅		4 ₂₃₄
row 9	4 ₄	4 ₁₂₃			4 ₅

4
C3

012

col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	8 ₁₂	8 ₃		8 ₄₅				
row2							X	
row3		8 ₄	8 ₅		8 ₁₂₃			
row4		8 ₁₂₅	8 ₃₄					
row5						X		
row6					X			
row7								X
row8	8 ₃₄₅		8 ₁	8 ₂				
row9			8 ₂	8 ₁₃₄₅				

4
C3

012

col 1	col 2	col 3	col 4	col 5
row1	8 ₁₂	8 ₃		8 ₄₅
row3		8 ₄	8 ₅	8 ₁₂₃
row4		8 ₁₂₅	8 ₃₄	
row8	8 ₃₄₅		8 ₁	8 ₂
row9			8 ₂	8 ₁₃₄₅

4 013	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C7									
row 1			5 ₂₄₅₇				5 ₁₃₆₈		
row 2	5 ₁₃₆₈								5 ₂₄₅₇
row 3					X				
row 4		X							
row 5				5 ₃₄₇₈		5 ₁₂₅₆			
row 6								X	
row 7			5 ₆₈	5 ₁₂		5 ₃₄	5 ₅₇		
row 8	5 ₂₄₅₇								5 ₁₃₆₈
row 9			5 ₁₃	5 ₅₆		5 ₇₈	5 ₂₄		

4 013	col 1	col 3	col 4	col 6	col 7	col 9
C7						
row 1		5 ₂₄₅₇			5 ₁₃₆₈	
row 2	5 ₁₃₆₈					5 ₂₄₅₇
row 5			5 ₃₄₇₈	5 ₁₂₅₆		
row 7		5 ₆₈	5 ₁₂	5 ₃₄	5 ₅₇	
row 8	5 ₂₄₅₇					5 ₁₃₆₈
row 9		5 ₁₃	5 ₅₆	5 ₇₈	5 ₂₄	

4 014	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
C7									
row 1						X			
row 2	6 ₁₂		6 ₃₄				6 ₅₆₇₈		
row 3		6 ₅₆₇₈						6 ₁₂₃₄	
row 4	6 ₃₇		6 ₁₅		6 ₂₄₆₈				
row 5									X
row 6	6 ₄₈		6 ₂₆		6 ₁₃₅₇				
row 7				X					
row 8	6 ₅₆		6 ₇₈				6 ₁₂₃₄		
row 9		6 ₁₂₃₄						6 ₅₆₇₈	

4 014	col 1	col 2	col 3	col 5	col 7	col 8
row 2	6 ₁₂		6 ₃₄		6 ₅₆₇₈	
row 3		6 ₅₆₇₈				6 ₁₂₃₄
row 4	6 ₃₇		6 ₁₅	6 ₂₄₆₈		
row 6	6 ₄₈		6 ₂₆	6 ₁₃₅₇		
row 8	6 ₅₆		6 ₇₈		6 ₁₂₃₄	
row 9		6 ₁₂₃₄				6 ₅₆₇₈

4
D3

015	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	7 ₂₄₆	7 ₁₃₅							
row2									X
row3				X					
row4						7 ₃₄₅₆	7 ₁₂		
row5	7 ₅	7 ₆	7 ₁₂₃₄						
row6						7 ₁₂		7 ₃₄₅₆	
row7					X				
row8	7 ₁	7 ₂					7 ₃₄₅₆		
row9	7 ₃	7 ₄	7 ₅₆					7 ₁₂	

4
D3

015	col 1	col 2	col 3	col 6	col 7	col 8
row1	7 ₂₄₆	7 ₁₃₅				
row4				7 ₃₄₅₆	7 ₁₂	
row5	7 ₅	7 ₆	7 ₁₂₃₄			
row6				7 ₁₂		7 ₃₄₅₆
row8	7 ₁	7 ₂			7 ₃₄₅₆	
row9	7 ₃	7 ₄	7 ₅₆			7 ₁₂

4
B1

016	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	X								
row2								X	
row3					X				
row4		1 ₃₄₅₆	1 ₁₂						
row5						X			
row6									X
row7			1 ₃	1 ₁₄			1 ₂₅₆		
row8		1 ₁₂	1 ₄₅	1 ₃₆					
row9			1 ₆	1 ₂₅			1 ₁₃₄		

4

016	col 2	col 3	col 4	col 7
row4	1 ₃₄₅₆	1 ₁₂		
row7		1 ₃	1 ₁₄	1 ₂₅₆
row8	1 ₁₂	1 ₄₅	1 ₃₆	
row9		1 ₆	1 ₂₅	1 ₁₃₄

4
B4

017

col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1								X
row2					1 ₂₅₆	1 ₁₃₄		
row3			X					
row4				X				
row5	1 ₃₅	1 ₁₂					1 ₄₆	
row6	1 ₄₆						1 ₁₂₃₅	
row7		1 ₃₄₅₆			1 ₁	1 ₂		
row8	1 ₁₂				1 ₃₄	1 ₅₆		
row9							X	

4

017

col 1	col 2	col 5	col 6	col 8
row2		1 ₂₅₆	1 ₁₃₄	
row5	1 ₃₅	1 ₁₂		1 ₄₆
row6	1 ₄₆			1 ₁₂₃₅
row7		1 ₃₄₅₆	1 ₁	1 ₂
row8	1 ₁₂		1 ₃₄	1 ₅₆

4
C5

018	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	X								
row2				9 ₁				9 ₂₃₄₅	
row3				9 ₂	9 ₃	9 ₄₅			9 ₁
row4		X							
row5					9 ₁₂₄				9 ₃₅
row6				9 ₃₅				9 ₁	9 ₂₄
row7				9 ₄	9 ₅	9 ₁₂₃			
row8			X						
row9							X		

4

018	col 4	col 5	col 6	col 8	col 9
row2	9 ₁			9 ₂₃₄₅	
row3	9 ₂	9 ₃	9 ₄₅		9 ₁
row5		9 ₁₂₄			9 ₃₅
row6	9 ₃₅			9 ₁	9 ₂₄
row7	9 ₄	9 ₅	9 ₁₂₃		

4
A3

019	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X						
row2							X		
row3						X			
row4		3 ₅		3 ₁₂₃	3 ₄				
row5									X
row6		3 ₁₂₃₄			3 ₅				
row7	3 ₁				3 ₃			3 ₂₄₅	
row8	3 ₂			3 ₄₅				3 ₁₃	
row9	3 ₃₄₅				3 ₁₂				

4

019	col 1	col 2	col 4	col 5	col 8
row4		3 ₅	3 ₁₂₃	3 ₄	
row6		3 ₁₂₃₄		3 ₅	
row7	3 ₁			3 ₃	3 ₂₄₅
row8	3 ₂		3 ₄₅		3 ₁₃
row9	3 ₃₄₅			3 ₁₂	

4
A4

020

col 1col 2col 3col 4col 5col 6col 7col 8col 9

row1				X					
row2		2 ₁					2 ₂₃₄₅		
row3		2 ₂₃	2 ₄₅						2 ₁
row4		2 ₄₅	2 ₁₂₃						
row5						X			
row6								X	
row7					2 ₃₅		2 ₁		2 ₂₄
row8					2 ₁₂₄				2 ₃₅
row9	X								

4

020

col 2col 3col 5col 7col 9

row2	2 ₁			2 ₂₃₄₅	
row3	2 ₂₃	2 ₄₅			2 ₁
row4	2 ₄₅	2 ₁₂₃			
row7			2 ₃₅	2 ₁	2 ₂₄
row8			2 ₁₂₄		2 ₃₅

4
B6

021

col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	4 ₁₂		4 ₃	4 ₄₅₆				
row2	4 ₄₅		4 ₆	4 ₁₂₃				
row3						X		
row4			4 ₁₂₄₅					4 ₃₆
row5					X			
row6	4 ₃₆						4 ₁₄	4 ₂₅
row7		X						
row8							4 ₂₃₅₆	4 ₁₄
row9						X		

4
B6

021

col 1	col 3	col 4	col 8	col 9
row1	4 ₁₂	4 ₃	4 ₄₅₆	
row2	4 ₄₅	4 ₆	4 ₁₂₃	
row4		4 ₁₂₄₅		4 ₃₆
row6	4 ₃₆		4 ₁₄	4 ₂₅
row8			4 ₂₃₅₆	4 ₁₄

4
B1

022

col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						1 ₁₅	1 ₃₆	1 ₂₄
row2			X					
row3				X				
row4		1 ₁₂				1 ₃	1 ₄₅	1 ₆
row5		1 ₃₄₅₆					1 ₁₂	
row6						X		
row7	X							
row8						1 ₂₄₆		1 ₁₃₅
row9				X				

4
B1

022

col 2	col 7	col 8	col 9
row1	1 ₁₅	1 ₃₆	1 ₂₄
row4	1 ₁₂	1 ₃	1 ₄₅
row5	1 ₃₄₅₆	1 ₁₂	
row8	1 ₂₄₆		1 ₁₃₅

4
B5

023

col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						2 ₂₅₆	2 ₁₃₄	
row2	X							
row3				X				
row4						X		
row5			2 ₃₄₅₆				2 ₁	2 ₂
row6			2 ₁₂				2 ₃	2 ₄₅₆
row7		2 ₁₂₃₆					2 ₄	2 ₅
row8		2 ₄₅					2 ₆	2 ₁₂₃
row9			X					

4
B5

col 2	col 3	col 7	col 8	col 9
		2 ₂₅₆	2 ₁₃₄	
	2 ₃₄₅₆	2 ₁	2 ₂	
	2 ₁₂	2 ₃		2 ₄₅₆
2 ₁₂₃₆		2 ₄	2 ₅	
2 ₄₅			2 ₆	2 ₁₂₃

4
B8

024	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				X					
row2									X
row3	X								
row4		6 ₂₅				6 ₁₄		6 ₃₆	
row5			6 ₁₄			6 ₂₃₅₆			
row6		6 ₃₆						6 ₁₂₄₅	
row7		6 ₁	6 ₂₃				6 ₄₅₆		
row8		6 ₄	6 ₅₆				6 ₁₂₃		
row9					X				

4

024	col 2	col 3	col 6	col 7	col 8
row4	6 ₂₅		6 ₁₄		6 ₃₆
row5		6 ₁₄	6 ₂₃₅₆		
row6	6 ₃₆				6 ₁₂₄₅
row7	6 ₁	6 ₂₃		6 ₄₅₆	
row8	6 ₄	6 ₅₆		6 ₁₂₃	

4
C2

025

col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				7 ₆₇		7 ₁₂₃		7 ₄₅
row2				7 ₁₄	7 ₂₃₅	7 ₆		7 ₇
row3		X						
row4			X					
row5							X	
row6				X				
row7				7 ₂₅	7 ₁₄₆₇			7 ₃
row8	X							
row9				7 ₃		7 ₄₅₇		7 ₁₂₆

4
C2

025

col 5	col 6	col 7	col 9	
row1	7 ₆₇		7 ₁₂₃ 7 ₄₅	
row2	7 ₁₄	7 ₂₃₅	7 ₆ 7 ₇	
row7	7 ₂₅	7 ₁₄₆₇		7 ₃
row9	7 ₃		7 ₄₅₇	7 ₁₂₆

4
B3

026

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	9 ₂	9 ₁₄₅						9 ₃	
row2						X			
row3	9 ₃							9 ₁₂₄₅	
row4									X
row5	9 ₁	9 ₂₃	9 ₄		9 ₅				
row6			9 ₅		9 ₁₂₃₄				
row7	9 ₄₅		9 ₁₂₃						
row8							X		
row9				X					

4
B3

026

	col 1	col 2	col 3	col 5	col 8
row1	9 ₂	9 ₁₄₅			9 ₃
row3	9 ₃				9 ₁₂₄₅
row5	9 ₁	9 ₂₃	9 ₄	9 ₅	
row6			9 ₅	9 ₁₂₃₄	
row7	9 ₄₅		9 ₁₂₃		

4
B2

027

col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	3 ₁₂₄₆	3 ₃₅						
row2						X		
row3					X			
row4	3 ₃₅	3 ₄₆		3 ₁	3 ₂			
row5								X
row6		3 ₁₂		3 ₃₄	3 ₅₆			
row7							X	
row8				3 ₂₅₆	3 ₁₃₄			
row9			X					

4
B2

027

col 1	col 2	col 4	col 5
row1	3 ₁₂₄₆	3 ₃₅	
row4	3 ₃₅	3 ₄₆	3 ₁
row6		3 ₁₂	3 ₃₄
row8			3 ₂₅₆

4
B3

028	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1				2 ₅		2 ₆			2 ₁₂₃₄
row2	2 ₁₂		2 ₃₄						2 ₅₆
row3	2 ₅₆			2 ₁₃		2 ₂₄			
row4		X							
row5				2 ₂₄₆		2 ₁₃₅			
row6								X	
row7					X				
row8							X		
row9	2 ₃₄		2 ₁₂₅₆						

4
B3

028	col 1	col 3	col 4	col 6	col 9
row1			2 ₅	2 ₆	2 ₁₂₃₄
row2	2 ₁₂	2 ₃₄			2 ₅₆
row3	2 ₅₆		2 ₁₃	2 ₂₄	
row5			2 ₂₄₆	2 ₁₃₅	
row9	2 ₃₄	2 ₁₂₅₆			

4
B7

029

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1								X	
row2	8 ₂	8 ₁₃₄₅							
row3					X				
row4									X
row5				8 ₅		8 ₁₂₃₄			
row6	8 ₃₄₅		8 ₁₂						
row7	8 ₁	8 ₂	8 ₃	8 ₄		8 ₅			
row8							X		
row9			8 ₄₅	8 ₁₂₃					

4

029

	col 1	col 2	col 3	col 4	col 6
row2	8 ₂	8 ₁₃₄₅			
row5				8 ₅	8 ₁₂₃₄
row6	8 ₃₄₅		8 ₁₂		
row7	8 ₁	8 ₂	8 ₃	8 ₄	8 ₅
row9			8 ₄₅	8 ₁₂₃	

4
C1

030

col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			X					
row2			1 ₃				1 ₁₂	
row3		1 ₁	1 ₂				1 ₃	
row4								X
row5					X			
row6	X							
row7						X		
row8		1 ₂₃					1 ₁	1 _K
row9			1 ₁				1 ₂	1 ₃

4

030

col 2	col 3	col 7	col 8
row2	1 ₃		1 ₁₂
row3	1 ₁	1 ₂	1 ₃
row8	1 ₂₃	1 ₁	1 _K
row9	1 ₁	1 ₂	1 ₃

4
A8

031

col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	4 ₁					4 ₂₃	4 ₄₅	
row2		4 ₂₃₄₅						4 ₁
row3				X				
row4							4 ₄₅	4 ₁₂₃
row5				X				
row6					X			
row7	4 ₃₅	4 ₁						4 ₂₄
row8						X		
row9	4 ₂₄						4 ₁	4 ₃₅

4
A8

031

col 1	col 2	col 7	col 8	col 9
row1	4 ₁		4 ₂₃	4 ₄₅
row2		4 ₂₃₄₅		4 ₁
row4			4 ₄₅	4 ₁₂₃
row7	4 ₃₅	4 ₁		4 ₂₄
row9	4 ₂₄		4 ₁	4 ₃₅

4
C2

032

col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	8 ₁₂	8 ₃₄₅			8 ₆₇			
row2	8 ₆	8 ₇		8 ₂₅	8 ₁₃₄			
row3							X	
row4	8 ₃₇			8 ₁₄₆	8 ₂₅			
row5	8 ₄₅	8 ₁₂₆		8 ₃₇				
row6								X
row7						X		
row8			X					
row9	X							

4
C2

032

col 2	col 3	col 5	col 6
row1	8 ₁₂	8 ₃₄₅	8 ₆₇
row2	8 ₆	8 ₇	8 ₁₃₄
row4	8 ₃₇	8 ₁₄₆	8 ₂₅
row5	8 ₄₅	8 ₁₂₆	8 ₃₇

4
B3

033

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					6 ₅	6 ₁₂₃₄			
row2		X							
row3								X	
row4	6 ₁				6 ₃				6 ₂₄₅
row5			6 ₃₄₅		6 ₁₂				
row6	6 ₂				6 ₄	6 ₅			6 ₁₃
row7				X					
row8	6 ₃₄₅		6 ₁₂						
row9							X		

4
B3

033

	col 1	col 3	col 5	col 6	col 9
row1			6 ₅	6 ₁₂₃₄	
row4	6 ₁		6 ₃		6 ₂₄₅
row5		6 ₃₄₅	6 ₁₂		
row6	6 ₂		6 ₄	6 ₅	6 ₁₃
row8	6 ₃₄₅	6 ₁₂			

4
B5

034

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	7 ₁₂₃₅	7 ₄₆							
row2							X		
row3				7 ₂₃	7 ₁₄₅₆				
row4			X						
row5						X			
row6								X	
row7		7 ₁₂₃		7 ₄₅₆					
row8	7 ₆				7 ₃				7 ₁₂₄₅
row9	7 ₄	7 ₅		7 ₁	7 ₂				7 ₃₆

4
B5

034

	col 1	col 2	col 4	col 5	col 9
row1	7 ₁₂₃₅	7 ₄₆			
row3			7 ₂₃	7 ₁₄₅₆	
row7		7 ₁₂₃	7 ₄₅₆		
row8	7 ₆			7 ₃	7 ₁₂₄₅
row9	7 ₄	7 ₅	7 ₁	7 ₂	7 ₃₆

4
D2

035	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					X				
row2		8 ₅₆₇₈						8 ₁₂₃₄	
row3	8 ₁₂₃₄						8 ₅₇		8 ₆₈
row4	8 ₅₆			8 ₃₄₇₈			8 ₁		8 ₂
row5		8 ₁₂₃₄						8 ₅₆₇₈	
row6	8 ₇₈			8 ₁₂₅₆			8 ₃		8 ₄
row7						X			
row8			X						
row9							8 ₂₄₆₈		8 ₁₃₅₇

4

035	col 1	col 2	col 4	col 7	col 8	col 9
row2		8 ₅₆₇₈			8 ₁₂₃₄	
row3	8 ₁₂₃₄			8 ₅₇		8 ₆₈
row4	8 ₅₆		8 ₃₄₇₈	8 ₁		8 ₂
row5		8 ₁₂₃₄			8 ₅₆₇₈	
row6	8 ₇₈		8 ₁₂₅₆	8 ₃		8 ₄
row9				8 ₂₄₆₈		8 ₁₃₅₇

4
A5

036

col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			2 ₁₂₃	2 ₄₅		2 ₆₇		
row2	X							
row3				2 ₆₇		2 ₁₂₃₄₅		
row4		2 ₁₃₅₇	2 ₂₄₆					
row5						X		
row6							X	
row7		2 ₂₄₆	2 ₃₅₇	2 ₁				
row8								X
row9			2 ₁	2 ₄₅₆₇	2 ₂₃			

4
A5

036

col 2	col 3	col 4	col 5	col 7
row1		2 ₁₂₃	2 ₄₅	2 ₆₇
row3			2 ₆₇	2 ₁₂₃₄₅
row4	2 ₁₃₅₇	2 ₂₄₆		
row7	2 ₂₄₆	2 ₃₅₇	2 ₁	
row9		2 ₁	2 ₄₅₆₇	2 ₂₃

4
A7

037

	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1						2 ₅₆	2 ₁₂₃₄		
row2	X								
row3				2 ₁₂₃₄					2 ₅₆
row4								X	
row5		X							
row6					2 ₃₄₅₆	2 ₁₂			
row7					2 ₁₂	2 ₃₄	2 ₅₆		
row8			2 ₂₄₆	2 ₅					2 ₁₃
row9			2 ₁₃₅	2 ₆					2 ₂₄

4
A7

037

	col 3	col 4	col 5	col 6	col 7	col 9
row1				2 ₅₆	2 ₁₂₃₄	
row3		2 ₁₂₃₄				2 ₅₆
row6			2 ₃₄₅₆	2 ₁₂		
row7			2 ₁₂	2 ₃₄	2 ₅₆	
row8	2 ₂₄₆	2 ₅				2 ₁₃
row9	2 ₁₃₅	2 ₆				2 ₂₄

4
B2

038	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1					X				
row2									X
row3		3 ₂₄₅₆	3 ₁₃						
row4		3 ₁	3 ₂	3 ₃₄		3 ₅₆			
row5							X		
row6		3 ₃	3 ₄₅₆	3 ₁₂					
row7								X	
row8				3 ₅₆		3 ₁₂₃₄			
row9	X								

4

038	col 2	col 3	col 4	col 6
row3	3 ₂₄₅₆	3 ₁₃		
row4	3 ₁	3 ₂	3 ₃₄	3 ₅₆
row6	3 ₃	3 ₄₅₆	3 ₁₂	
row8			3 ₅₆	3 ₁₂₃₄

4 039	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
A9									
row 1									X
row 2	8 ₄₅	8 ₁₂₃							
row 3				8 ₃₅		8 ₁₂₄			
row 4			8 ₁			8 ₃₅	8 ₂₄		
row 5	8 ₂₃	8 ₄₅						8 ₁	
row 6				8 ₁₂₄			8 ₃₅		
row 7					X				
row 8	8 ₁							8 ₂₃₄₅	
row 9			8 ₂₃₄₅				8 ₁		

4 039	col 1	col 2	col 3	col 4	col 6	col 7	col 8
row 2	8 ₄₅	8 ₁₂₃					
row 3				8 ₃₅	8 ₁₂₄		
row 4			8 ₁		8 ₃₅	8 ₂₄	
row 5	8 ₂₃	8 ₄₅					8 ₁
row 6				8 ₁₂₄		8 ₃₅	
row 8	8 ₁						8 ₂₃₄₅
row 9			8 ₂₃₄₅			8 ₁	

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5 001	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row 1									X
row 2				X					
row 3		X							
row 4					2 ₂₃₄₅₆			2 ₁	
row 5	2 ₁₄₅₆						2 ₂₃		
row 6	2 ₂₃				2 ₁		2 ₄₅	2 ₆	
row 7			2 ₁₃₅₆					2 ₂₄	
row 8			2 ₂₄				2 ₁₆	2 ₃₅	
row 9						X			

5 002	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row 1	9 ₁₂		9 ₃₄				9 ₅₆₇₈		
row 2					X				
row 3	9 ₅₆		9 ₇₈				9 ₁₂₃₄		
row 4	9 ₃₄₇₈			9 ₁₅₆		9 ₂			
row 5								X	
row 6			9 ₁₂₅₆	9 ₃₇		9 ₄₈			
row 7		X							
row 8				9 ₂₄₈		9 ₁₃₅₆₇			
row 9									X

5

003	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1							2 ₂	2 ₃	2 ₁₄₅₆₇
row2				2 ₄₆		2 ₁₂₃₅₇			
row3									
row4									
row5							2 ₃₆₇	2 ₁₂₄₅	
row6									
row7	2 ₄₆			2 ₁₂₃₅₇					
row8	2 ₅₇					2 ₄₆	2 ₁		2 ₂₃
row9	2 ₁₂₃						2 ₄₅	2 ₆₇	

5

004	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1		2 ₁₂	2 ₃₄				2 ₅₆₇₈		
row2									
row3	2 ₅₆		2 ₇₈				2 ₁₂₃₄		
row4	2 ₁₃₇	2 ₅							2 ₂₄₆₈
row5									
row6	2 ₂₄₈		2 ₆						2 ₁₃₅₇
row7									
row8		2 ₃₄₆₇₈	2 ₁₂₅						
row9									

5

006	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									
row2			6 ₁₂				6 ₃₄	6 ₅₆	
row3			6 ₃₄₅₆					6 ₁₂	
row4							6 ₁₅	6 ₃	6 ₄
row5									
row6				6 ₁₃₄₅			6 ₂₆		
row7								6 ₄	6 ₁₂₃₅₆
row8									
row9									

5

007	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			4 ₂₃₄₅₆		4 ₁				
row2			4 ₁	4 ₂₃	4 ₄	4 ₅₆			
row3									
row4				4 ₅₆		4 ₁₂₃₄			
row5									
row6									
row7				4 ₁₄	4 ₂₅		4 ₃₆		
row8									
row9					4 ₃₆		4 ₁₂₄₅		

5

008	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	1 ₁	1 ₂		1 ₃₄				1 ₅	1 ₆
row2	1 ₃₅₆							1 ₁₂₄	
row3	1 ₄			1 ₁₂₅₆					1 ₃
row4									
row5									
row6	1 ₂	1 ₁₃₄₅₆							
row7									
row8								1 ₃₆	1 ₁₂₄₅
row9									

5

009	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	4 ₁₂₃			4 ₄₇₈				4 ₅	4 ₆
row2	4 ₄₅₆						4 ₁₂₇	4 ₃₈	
row3	4 ₇₈			4 ₁₂₃₅₆					4 ₄
row4								4 ₂₄₆	4 ₁₃₅₇₈
row5									
row6									
row7									
row8							4 ₃₄₅₆₈	4 ₁₇	4 ₂
row9									

5

010	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1									
row2	1 ₁₂₃₄		1 ₅						
row3									
row4						1 ₄	1 ₃		1 ₁₂₅
row5						1 ₁₂₃₅	1 ₄		
row6									
row7	1 ₅		1 ₁				1 ₂		1 ₃₄
row8									
row9			1 ₂₃₄				1 ₁₅		

5

011	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1	4 ₁		4 ₂₃					4 ₄₅₆₇	
row2	4 ₄		4 ₅₆	4 ₁₂₃₇					
row3	4 ₇			4 ₄₅₆				4 ₁₂₃	
row4									
row5									
row6									
row7									
row8	4 ₂₅		4 ₁₄₇		4 ₃₆				
row9	4 ₃₆				4 ₁₂₄₅₇				

5

012	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row1			6 ₁₂₃				6 ₄		
row2									
row3	6 ₄							6 ₁	6 ₂₃
row4			6 ₄				6 ₁₂₃		
row5				6 ₁₂	6 ₃			6 _K	6 ₄
row6	6 ₁₂₃				6 ₄				
row7				6 ₃₄				6 ₂	6 ₁
row8					6 ₁₂			6 ₃₄	
row9									

5 0 1 3	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row 1	1 ₁	1 ₁₂				1 ₃₄₅₆₇	1 ₁	1 ₂	
row 2									1 ₃₄
row 3			1 ₃₄	1 ₁₂					1 ₅₆₇
row 4				1 ₃₄₅₆₇					1 ₁₂
row 5		X							
row 6						1 ₁₂	1 ₃₅₆	1 ₄₇	
row 7							1 ₂₄₇	1 ₁₃₅₆	
row 8					X				
row 9	X								

PATTERN FILE 6

6 001	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row 1			9 ₄₅₆			9 ₇₈	9 ₁₂	9 ₃	
row 2			9 ₁₂₃₇₈				9 ₄₅		9 ₆
row 3						9 ₁₂₃₄₅₆		9 ₇	9 ₈
row 4					9 ₂₅		9 ₃₆₇₈		9 ₁₄
row 5					9 ₁₃₄₆₇₈				9 ₂₅
row 6		X							
row 7								9 ₁₂₄₅₆₈	9 ₃₇
row 8				X					
row 9	X								

6 002	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row 1							X		
row 2			8 ₃₄₈	8 ₅₆₉		8 ₁₂₇			
row 3			8 ₁₂₅₆₇₉			8 ₃₄₈			
row 4				8 ₁₂₃₄		8 ₅₆		8 ₇₈₉	
row 5		X							
row 6				8 ₇₈		8 ₉		8 ₁₃₅	8 ₂₄₆
row 7								8 ₂₄₆	8 ₁₃₅₇₈₉
row 8					X				
row 9	X								

6 003	col 1	col 2	col 3	col 4	col 5	col 6	col 7	col 8	col 9
row 1			1 ₃₄₅₆	1 ₁		1 ₂	1 ₇₈		
row 2			1 ₁₂₇₈	1 ₃	1 ₄₅	1 ₆			
row 3					1 ₇₈				1 ₁₂₃₄₅₆
row 4							1 ₁₂₃₄₅₆		1 ₇₈
row 5				1 ₂₅₆₇		1 ₁₃₄₈			
row 6		X							
row 7								X	
row 8				1 ₄₈	1 ₁₂₃₆	1 ₅₇			
row 9	X								

PATTERN
DESCRIPTION
CODES 1

Pattern Description Codes 1:

A1 2 – 2 – 2 **017, 033.**

A2 2 – 2 **006, 032.**
 |
 2

A4 2 – 2 **020, 035.**
 |
 2 – 2

A5 2 – 2 – 2 **034**
 |
 2 – 2

A6 2 **024**
 |
 2 – 2
 |
 2

A7 2 – 2 **009**
 |
 2 – 2
 |
 2

B1 2 – 2 **002, 005, 013, 015, 019, 021, 022, 029, 036.**
 | |
 2 – 2

B2 2 – 2 – 2 **008, 023, 030.**
 | |
 2 – 2

B3 2 **038**
 |
 2 – 2 – 2
 | |
 2 – 2

Pattern Description Codes 1:

B9

2

2

|

2-2

|

2-2

001, 003, 007, 010, 011, 012, 014, 016, 025, 026, 028, 031, 039.

C0

3-2

|

2

037

C1

2

|

3-3-2

|

2-2

027

C2

3

3

|

2-2

|

2-2

004

C8

3-2

|

3-2

|

3-----2

014

C3

3

3

|

2-2

|

3-2

018

PATTERN DESCRIPTION CODES 2

Pattern Description Codes 2:

A0	$\begin{array}{c} 2-2 \\ \\ 2-2 \end{array}$	see K1
A1	$\begin{array}{c} 3-2 \\ \\ 2 \end{array}$	S 023, 038, 047, 048, 056, 066, 068, 091, 092, 093, 094, 096, 105, 145, 170, 171, 179.
A6	$\begin{array}{c} 3-2 \\ \\ 2 \end{array}$	168
A3	3-2-2	030, 102. (Straight three)
A4	$\begin{array}{c} 3-2-2 \\ \\ 2 \end{array}$	S 110, 113, 114, 127. L 020, 039, 051, 070, 072, 079, 095, 107, 110, 120, 123.
A6	$\begin{array}{c} 3-2-2 \\ \\ 2 \end{array}$	X 104
A5	$\begin{array}{c} 3-2-2 \\ \\ 2-2 \end{array}$	L 097 S 111, 119, 146
D	$\begin{array}{c} 2 \\ \\ 3-2 \\ \\ 2 \end{array}$	S 002, 003, 006, 010, 011, 050, 078, 080, 089, 098, 099, 103, 106, 115, 118, 122, 124, 152, 154
D1	$\begin{array}{c} 2-2 \\ \\ 3-2 \\ \\ 2 \end{array}$	172
E.	$\begin{array}{c} 2 \\ \\ 3-2 \\ \\ 2-2 \end{array}$	subgroup: S 004, 026, 073.

Pattern Description Codes 2:

F **2 - 2** **S 008, 044, 071, 117, 151, 162.**

 |

3 - 2

 |

2

G1 **3 - 2**

 | |

2 - 2

G2 **3 - 2 - 2** **L 007, 015, 017, 019, 021, 027, 029, 031, 046, 049, 059, 062, 063,**
 | | **067, 074, 075, 077, 082, 083, 088, 108, 150, 164, 166, 167, 176,**
 2 - 2 **183.**

G3 **3 - 2** **S 151**
 | | **L 076**
 2 - 2 - 2

G4 **3 - 2 - 2** **L 036**
 | |
 2 - 2
 |
 2

G7 **3 - 2 - 2** **L 156**
 | |
 2 - 2
 |
 2

G5 **3 - 2** **L 045**
 | |
 2 - 2 - 2
 |
 2

G6 **2 - 2** **143**
 |
 3 - 2 - 2
 | |
 | **2**
 2

Pattern Description Codes 2:

G7	$ \begin{array}{c} 2 \\ \\ 3-2-2 \\ \quad \quad \\ \quad 2-2 \end{array} $	169, 187.
L1	$ \begin{array}{c} 3-3 \\ \\ 2-2 \end{array} $	
K1	$ \begin{array}{c} 3-3 \\ \quad \\ K-3-2 \\ \\ 2 \end{array} $	158 (= A0 after killers removed)
L2	$ \begin{array}{c} 3-3 \\ \quad \\ 2-2 \end{array} $	053, 109.
L1	$ \begin{array}{c} 3-3-2 \\ \quad \\ 2-2 \end{array} $	185. 188.
L3	$ \begin{array}{c} 3-3-2 \\ \\ 2 \end{array} $	138
L4	$ \begin{array}{c} 3-2 \\ \quad \\ 2-3 \end{array} $	163
ML.	$ \begin{array}{c} 3-3-2 \\ \quad \\ 2-2 \end{array} $	001, 005, 016, 022, 024, 034, 035, 040, 042, 043, 054, 055, 060, 069, 084, 086, 139, 144, 147, 153 159 160, 161, 165, 177, 180.
NS	$ \begin{array}{c} 3-3 \\ \quad \\ 3-2 \end{array} $	085, 087.
OS	$ \begin{array}{c} 3-3 \\ \quad \\ 3-2-2 \end{array} $	136

Pattern Description Codes 2:

P1 4 – 2 013, 028, 052, 101, 126, 130, 132.

|

2

Q1 2
 |
 4 – 2

Q 2 018, 041, 057, 064, 112, 125, 137, 141, 178, 184, 186.

|

4 – 2

|

2

R 4 – 2 – 2 058, 181.

|

2

S 2 – 2 134.

|

4 – 2

|

2

T 4 – 2 – 2 148, 149.

|

2

T4 2 – 4 173

|

2 – 2 – 2

|

|

2 – 2

U 4 – 2 – 2 065

|

|

3 – 2

U2 4 – 3 – 2

|

|

2 – 2

Pattern Description Codes 2:

U3 4 - 3 - 2 **037**
 | |
 3 - 2

U5 4 - 3 - 2 **174**
 | |
 2 - 3

U4 4 - 3 - 2 **014**
 | |
 3 - 3

V1 4 - 2
 | |
 2 - 2

 2
 |
V2 4 - 2 - 2 **182**
 | |
 2 - 3

W1 3 - 3 - 2 **100, 102.**

W2 3 - 2 - 2 **061, 116, 121.**
 |
 2

W3 3 - 2 - 2 **129**
 |
 2
 |
 2

W4 2
 |
 3 - 2
 |
 2

W5 3 - 2 - 2 **090**
 |
 2-----2

Pattern Description Codes 2:

W6 3 - 2 - 2 **012**
 | | |
 2 - 2 |
 | |
 2-----2

W7 3 - 3 - 2 **032**
 | | |
 | 2 - 2
 | |
 2 - 2

X1 3 - 3 - 2 **081, 142.**

X2 3 - 3 - 2 **009 (all straight)**
 |
 2

X3 3 - 3 - 2 **131 (mixed 3's)**
 |
 2

X4 3 - 3 - 2 **140 (mixed 3's)**
 |
 2
 |
 2

W8 4 - 2 - 2 **033**
 | | |
 3 - 2 |
 | |
 2-----2

Y1 3 - 3 - 3 **128**

Y2 3 - 3 - 2
 | |
 3 2

Pattern Description Codes 2:

Y3 3 – 3 – 2 014, 037.
 | |
 3 – 2

PATTERN
DESCRIPTION
CODES 3

Pattern Description Codes 3:

A2	$ \begin{array}{c} 2 \\ \\ 3-2 \\ \\ 2 \end{array} $	subgroup 1 (small ells): 008, 032. subgroup 2 (large ells): no members
A8	$ \begin{array}{c} 3-3-2 \\ \\ 2 \end{array} $	031
A4	$ \begin{array}{c} 2 \\ \\ 3-3-2 \\ \\ 2 \end{array} $	011, 020
G3	$ \begin{array}{c} 2 \\ \\ 3-3-2 \\ \\ 2 \end{array} $	033
B2	$ \begin{array}{c} 3-2-2 \\ \quad \\ 2-3 \\ \\ 2 \end{array} $	024
B3	$ \begin{array}{c} 3-3-2 \\ \\ 2 \end{array} $	029, 031, 043, 044.
B4	$ \begin{array}{c} 2 \\ \\ 3-3 \\ \\ 2 \end{array} $	subgroup 1: 009, 010, 015, 018, 039, 047, 050, 051 subgroup 2: 035, 041, 037
B5	$ \begin{array}{c} 3-2-2 \\ \\ 2-3 \end{array} $	045, 046

Pattern Description Codes 3:

G6

2

3-3-2

2

042

B6

3-3-2

|

2-2

038

A5 $\begin{array}{c} 2 \\ | \\ 3-3 \\ | \\ 2 \end{array}$ 005

B7 $\begin{array}{c} 2 \\ | \\ 3-3-2 \\ | \\ 2 \end{array}$ **011, 020.**

B8 $\begin{array}{c} 2 \\ | \\ 3-3-2 \\ | \\ 2 \end{array}$ **033, 048, 054.**

B9 $\begin{array}{c} 2-2 \\ | \\ 3-3 \\ | \\ 2 \end{array}$ **005**

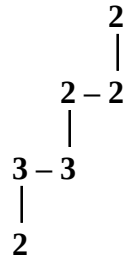
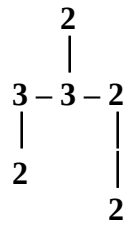
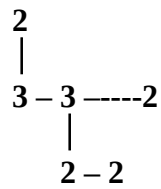
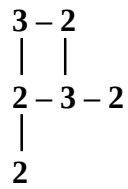
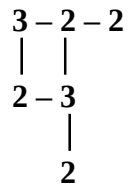
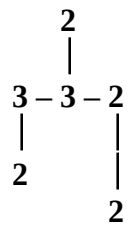
G4

3-3-2

|

2-2

038

Pattern Description Codes 3:**A6** **012****A7** **030****A3** **061****C2** **004, 024****C3** **017****C4** **030**

Pattern Description Codes 3:

C5 3 – 2 – 2 **059**
 | |
 2 – 3
 |
 2

C6 2 **061**
 |
 3 – 2 – 3
 |
 2 – 2

C7 2 **012**
 |
 2 – 2
 |
 3 – 3
 |
 2

D1 3 – 3 **006, 019, 021, 023, 028, 036.**
 | |
 3 – 2 **subgroup 1 (24 possibilities): 006, 021, 023, 028**
 subgroup 2:(24 possibilities): 019, 036

C9 3 – 2 **017, 059.**
 | |
 2 – 3 – 2
 |
 2

D2 2 **025**
 |
 3 – 3 – 3
 | |
 2 – 2

D3 3 – 3 – 3 **026**
 | |
 3 – 2

Pattern Description Codes 3:

E1 4 - 2 - 2 **001, 007, 022, 049.**

 |

 2

G5 4 - 2 - 2 **040**

 |

 2 - 2

E3 4 - 2 - 2 **060**

 | |

 2 - 2

 |

 2

E4 4 - 3 - 2 **056**

 |

 2

E5 2 **062**

 |

 4 - 3

 |

 2

G1 4 - 3 **003, 053.**

 | |

 2 - 3

E6 4 - 3 - 2 **057, 058.**

 | |

 3 - 3

E8 4 - 3 - 3 **027**

 | | |

 2 - 2 |

 | |

 2-----2

F1 5 - 2 - 2 **034**

 |

 2

Pattern Description Codes 3:

F2 **2** **002, 013, 016.**
 |
 5 - 2 - 2
 |
 2

PATTERN
DESCRIPTION
CODES 4

Pattern Description Codes 4:

A3 $\begin{array}{c} 3-3-2 \\ | \\ 2-3 \end{array}$ **019**

A4 $\begin{array}{c} 3-2 \\ | \\ 3-2 \\ | \\ 2 \end{array}$ **020**

A5 $\begin{array}{c} 3-2 \\ | \\ 3-3 \\ | \\ 2 \end{array}$ **036**

A6 $\begin{array}{c} 3-2 \\ | \\ 3-2 \\ | \\ 2-3 \end{array}$ **004**

A8 $\begin{array}{c} 3-3-2 \\ | \quad | \\ 3-2 \end{array}$ **008, 011, 031.**

A9 $\begin{array}{c} 2 \\ | \\ 3-3-2 \\ | \quad | \\ 2-2 \\ | \\ 2 \end{array}$ **039**

A7 $\begin{array}{c} 2 \\ | \\ 4-2-2 \\ | \quad | \\ 2-2 \end{array}$ **037**

B1 $\begin{array}{c} 4-3-2 \\ | \\ 2 \end{array}$ **003, 016, 022.**

Pattern Description Codes 4:**B2** 2 **027, 038.**

$$\begin{array}{c}
 | \\
 4-3 \\
 | \\
 2
 \end{array}$$
B3 2 **026, 028, 033**

$$\begin{array}{c}
 | \\
 4-3-2 \\
 | \\
 2
 \end{array}$$
B4 3-2 **017**

$$\begin{array}{c}
 | \\
 4-2 \\
 | \\
 2
 \end{array}$$
B5 2 **023, 034.**

$$\begin{array}{c}
 | \\
 4-4-2 \\
 | \\
 2
 \end{array}$$
B6 4-2 **021**

$$\begin{array}{c}
 | \\
 3-2 \\
 | \\
 2
 \end{array}$$
B7 4-2-2 **029**

$$\begin{array}{c}
 | \\
 2-3
 \end{array}$$
B8 2-4 **024**

$$\begin{array}{c}
 | \\
 3-2-2
 \end{array}$$
C1 4-2 **030**

$$\begin{array}{cc}
 | & | \\
 2-3
 \end{array}$$

Pattern Description Codes 4:

C2 4 – 3 **025, 032.**
 | |
 3 – 3

C3 2 **012**
 |
 4 – 3 – 2
 |
 2

C0 4 – 3 – 2 **002**
 | |
 2 – 2
 |
 2

C4 4 – 3 – 2 **005**
 | |
 2 – 3

C5 4 – 2 – 3 **018**
 | |
 2 – 3

C6 2 – 2 **006**
 |
 4 – 3 – 2
 |
 2

C7 2 **013, 014**
 |
 4 – 3 – 3
 | |
 2 – 2

C8 4 – 3 – 2 **001, 009.**
 | |
 3 – 2
 |
 2

Pattern Description Codes 4:

C9 4 -----3 007
 | |
 3 - 2 |
 | |
 3 - 2 - 2

D1 5 - 3 - 2 010
 |
 2 - 2

D2 5 - 3 - 2 035
 | |
 3 - 2

D3 5 - 3 - 2 015
 |
 2 - 2
 |
 2